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## LAMPIRAN

### LAMPIRAN1. Titik Kesetimbangan Adanya Perokok

```

> restart :
> with(linalg) : with(DEtools) : with(LinearAlgebra) : with(VectorCalculus) :
#misalkan:#p + μ = Ω1
#τ2u2 = Ω2
#η + ω + μ = Ω3
#τ1 u1 = Ω4
#γ + μ = Ω5
#γ (1 + u2) δ = Ω6
#α (1 - u1) = Ω7
#γ (1 + u2) (1 - δ) = Ω8
> Pdot := Lambda - beta1·P·S - mu·P
                -PSβ1 - Pμ + Λ
> Sdot := beta1·P·S - beta2·S·X - (Omega1)·S + Omega2·Y
                PSβ1 - SXβ2 - Ω1S + Ω2Y
> Xdot := beta2·S·X - (Omega3)·X - Omega4·X
                SXβ2 - Ω3X - Ω4X
> Ydot := omega·X - (Omega5)·Y + Omega7·Qt - Omega2·Y
                -Ω2Y - Ω5Y + Ω7Qt + Xω
> Qtdot := Omega6·Y - mu·Qt - (Omega7)·Qt
                Ω6Y - Ω7Qt - Qtμ
> Qpdot := Omega8·Y - mu·Qp
                Ω8Y - Qpμ

#dari per3
> Sbintang := solve(Xdot, S)
                
$$\frac{\Omega3 + \Omega4}{\beta2}$$


#dari pers.1
> p := solve(Pdot, P)
                
$$\frac{\Lambda}{S\beta1 + \mu}$$


> Pbintang := 
$$\frac{\text{Lambda}}{\text{Sbintang} \cdot \text{beta1} + \text{mu}}$$

                
$$\frac{\Lambda}{\frac{(\Omega3 + \Omega4) \beta1}{\beta2} + \mu}$$


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#dari pers2

>  $y := \text{solve}(S\text{dot}, Y)$

$$\frac{S(-P\beta_1 + X\beta_2 + \Omega_1)}{\Omega_2}$$

>  $Y_{\text{bintang}} := \frac{S_{\text{bintang}}(-P_{\text{bintang}}\beta_1 + X\beta_2 + \Omega_1)}{\Omega_2}$

$$\frac{(\Omega_3 + \Omega_4) \left( -\frac{\Lambda\beta_1}{\frac{(\Omega_3 + \Omega_4)\beta_1}{\beta_2} + \mu} + X\beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2}$$

#dari pers5

>  $qt := \text{solve}(Q\text{t}\text{dot}, Qt)$

$$\frac{\Omega_6 Y}{\Omega_7 + \mu}$$

>  $Q_{\text{t}\text{bintang}} := \frac{\Omega_6 Y_{\text{bintang}}}{\Omega_7 + \mu}$

$$\frac{\Omega_6 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda\beta_1}{\frac{(\Omega_3 + \Omega_4)\beta_1}{\beta_2} + \mu} + X\beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2 (\Omega_7 + \mu)}$$

#dari pers6

>  $qp := \text{solve}(Qp\text{dot}, Qp)$

$$\frac{\Omega_8 Y}{\mu}$$

>  $Q_{p\text{bintang}} := \frac{\Omega_8 Y_{\text{bintang}}}{\mu}$

$$\frac{\Omega_8 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda\beta_1}{\frac{(\Omega_3 + \Omega_4)\beta_1}{\beta_2} + \mu} + X\beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2 \mu}$$

#substitusi semua nilai yang diperoleh pada persamaan 4

# $Y\text{dot} := \omega \cdot X - (\Omega_5) \cdot Y + \Omega_7 \cdot Qt - \Omega_2 \cdot Y$

>  $\text{subs\_semuanilai} := \omega \cdot X - (\Omega_5) \cdot Y_{\text{bintang}} + \Omega_7 \cdot Q_{\text{t}\text{bintang}} - \Omega_2 \cdot Y_{\text{bintang}}$

$$\omega X - \frac{\Omega_5 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{(\Omega_3 + \Omega_4) \beta_1} + X \beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2}$$

$$+ \frac{\Omega_7 \Omega_6 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{(\Omega_3 + \Omega_4) \beta_1} + X \beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2 (\Omega_7 + \mu)}$$

$$- \frac{(\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{(\Omega_3 + \Omega_4) \beta_1} + X \beta_2 + \Omega_1 \right)}{\beta_2}$$

> *Xbintang* := solve( subs\_semuanilai, X)

$$\left( (\Omega_3 + \Omega_4) (\Lambda \beta_1 \beta_2 - \Omega_1 \Omega_3 \beta_1 - \Omega_1 \Omega_4 \beta_1 - \Omega_1 \beta_2 \mu) (\Omega_2 \Omega_7 + \Omega_2 \mu + \Omega_5 \Omega_7 + \Omega_5 \mu - \Omega_6 \Omega_7) \right) / \left( \beta_2 (\Omega_3 \beta_1 + \Omega_4 \beta_1 + \beta_2 \mu) (\Omega_2 \Omega_3 \Omega_7 + \Omega_2 \Omega_3 \mu + \Omega_2 \Omega_4 \Omega_7 + \Omega_2 \Omega_4 \mu - \Omega_2 \Omega_7 \omega - \Omega_2 \mu \omega + \Omega_3 \Omega_5 \Omega_7 + \Omega_3 \Omega_5 \mu - \Omega_3 \Omega_6 \Omega_7 + \Omega_4 \Omega_5 \Omega_7 + \Omega_4 \Omega_5 \mu - \Omega_4 \Omega_6 \Omega_7) \right)$$

## LAMPIRAN 2. Linearisasi dan Kestabilan Titik Kesetimbangan Bebas

### Perokok

> restart

> with(linalg) : with(DEtools) : with(LinearAlgebra) : with(VectorCalculus) : with(linalg) :  
with(VectorCalculus) : with(Student[LinearAlgebra]) :

> f1 := Lambda - beta1·P·S - mu·P

$$-P S \beta 1 - P \mu + \Lambda$$

> f2 := beta1·P·S - beta2·S·X - (Omega1)·S + Omega2·Y

$$P S \beta 1 - S X \beta 2 - \Omega 1 S + \Omega 2 Y$$

> f3 := beta2·S·X - (Omega3)·X - Omega4·X

$$S X \beta 2 - \Omega 3 X - \Omega 4 X$$

> f4 := omega·X - (Omega5)·Y + Omega7·Qt - Omega2·Y

$$- \Omega 2 Y - \Omega 5 Y + \Omega 7 Q t + X \omega$$

> f5 := Omega6·Y - mu·Qt - (Omega7)·Qt

$$\Omega 6 Y - \Omega 7 Q t - Q t \mu$$

> f6 := Omega8·Y - mu·Qp

$$\Omega 8 Y - Q p \mu$$

> J := Jacobian((f1, f2, f3, f4, f5, f6), [P, S, X, Y, Qt, Qp])

$$\begin{bmatrix} -S \beta 1 - \mu & -\beta 1 P & 0 & 0 & 0 & 0 \\ S \beta 1 & P \beta 1 - X \beta 2 - \Omega 1 & -\beta 2 S & \Omega 2 & 0 & 0 \\ 0 & X \beta 2 & S \beta 2 - \Omega 3 - \Omega 4 & 0 & 0 & 0 \\ 0 & 0 & \omega & -\Omega 2 - \Omega 5 & \Omega 7 & 0 \\ 0 & 0 & 0 & \Omega 6 & -\Omega 7 - \mu & 0 \\ 0 & 0 & 0 & \Omega 8 & 0 & -\mu \end{bmatrix}$$

> TKfix :=  $\left[ P = \frac{\text{Lambda}}{\text{mu}}, S = 0, X = 0, Y = 0, Q t = 0, Q p = 0 \right]$

$$\left[ P = \frac{\Lambda}{\mu}, S = 0, X = 0, Y = 0, Q t = 0, Q p = 0 \right]$$

>  $Jac\_bintang := subs(TKfix, J)$

$$\begin{bmatrix}
 -\mu & -\frac{\beta I \Lambda}{\mu} & 0 & 0 & 0 & 0 \\
 0 & \frac{\beta I \Lambda}{\mu} - \Omega I & 0 & \Omega 2 & 0 & 0 \\
 0 & 0 & -\Omega 3 - \Omega 4 & 0 & 0 & 0 \\
 0 & 0 & \omega & -\Omega 2 - \Omega 5 & \Omega 7 & 0 \\
 0 & 0 & 0 & \Omega 6 & -\Omega 7 - \mu & 0 \\
 0 & 0 & 0 & \Omega 8 & 0 & -\mu
 \end{bmatrix}$$

$$La := \begin{bmatrix}
 \text{lambd} & 0 & 0 & 0 & 0 & 0 \\
 0 & \text{lambd} & 0 & 0 & 0 & 0 \\
 0 & 0 & \text{lambd} & 0 & 0 & 0 \\
 0 & 0 & 0 & \text{lambd} & 0 & 0 \\
 0 & 0 & 0 & 0 & \text{lambd} & 0 \\
 0 & 0 & 0 & 0 & 0 & \text{lambd}
 \end{bmatrix} :$$

>  $Jac\_bintang - La$

$$\begin{bmatrix}
 -\mu - \lambda & -\frac{\beta I \Lambda}{\mu} & 0 & 0 & 0 & 0 \\
 0 & \frac{\beta I \Lambda}{\mu} - \Omega I - \lambda & 0 & \Omega 2 & 0 & 0 \\
 0 & 0 & -\Omega 3 - \Omega 4 - \lambda & 0 & 0 & 0 \\
 0 & 0 & \omega & -\Omega 2 - \Omega 5 - \lambda & \Omega 7 & 0 \\
 0 & 0 & 0 & \Omega 6 & -\Omega 7 - \mu - \lambda & 0 \\
 0 & 0 & 0 & \Omega 8 & 0 & -\mu - \lambda
 \end{bmatrix}$$

>  $Determinant(Jac\_bintang - La)$

$$\frac{1}{\mu} \left( (-\Omega 3 - \Omega 4 - \lambda) (\Omega 2 \Omega 7 + \Omega 2 \lambda + \Omega 2 \mu + \Omega 5 \Omega 7 + \Omega 5 \lambda + \Omega 5 \mu - \Omega 6 \Omega 7 + \Omega 7 \lambda + \lambda^2 + \lambda \mu) (\Lambda \beta I - \Omega I \mu - \lambda \mu) (-\mu - \lambda)^2 \right)$$

>  $eigenvalues(Jac\_bintang)$

$$-\Omega 3 - \Omega 4, \frac{\Lambda \beta I - \Omega I \mu}{\mu}, -\frac{1}{2} \Omega 2 - \frac{1}{2} \Omega 5 - \frac{1}{2} \Omega 7 - \frac{1}{2} \mu$$

$$+ \frac{1}{2} \left( \Omega 2^2 + 2 \Omega 2 \Omega 5 - 2 \Omega 2 \Omega 7 - 2 \Omega 2 \mu + \Omega 5^2 - 2 \Omega 5 \Omega 7 - 2 \Omega 5 \mu + 4 \Omega 6 \Omega 7 + \Omega 7^2 + 2 \Omega 7 \mu + \mu^2 \right)^{1/2}, -\frac{1}{2} \Omega 2 - \frac{1}{2} \Omega 5 - \frac{1}{2} \Omega 7 - \frac{1}{2} \mu$$

$$- \frac{1}{2} \left( \Omega 2^2 + 2 \Omega 2 \Omega 5 - 2 \Omega 2 \Omega 7 - 2 \Omega 2 \mu + \Omega 5^2 - 2 \Omega 5 \Omega 7 - 2 \Omega 5 \mu + 4 \Omega 6 \Omega 7 + \Omega 7^2 + 2 \Omega 7 \mu + \mu^2 \right)^{1/2}, -\mu, -\mu$$



### LAMPIRAN 3. Linearisasi dan Kestabilan Titik Kesetimbangan Adanya Perokok

- > restart :
- > with(linalg) : with(DEtools) : with(LinearAlgebra) : with(VectorCalculus) : with(linalg) :  
with(VectorCalculus) : with(Student[LinearAlgebra]) :
- > f1 := Lambda - beta1·P·S - mu·P  

$$-P S \beta 1 - P \mu + \Lambda$$
- > f2 := beta1·P·S - beta2·S·X - (Omega1)·S + Omega2·Y  

$$P S \beta 1 - S X \beta 2 - \Omega 1 S + \Omega 2 Y$$
- > f3 := beta2·S·X - (Omega3)·X - Omega4·X  

$$S X \beta 2 - \Omega 3 X - \Omega 4 X$$
- > f4 := omega·X - (Omega5)·Y + Omega7·Qt - Omega2·Y  

$$-\Omega 2 Y - \Omega 5 Y + \Omega 7 Q t + X \omega$$
- > f5 := Omega6·Y - mu·Qt - (Omega7)·Qt  

$$\Omega 6 Y - \Omega 7 Q t - Q t \mu$$
- > f6 := Omega8·Y - mu·Qp  

$$\Omega 8 Y - Q p \mu$$
- > J := Jacobian(⟨f1,f2,f3,f4,f5,f6⟩, [P, S, X, Y, Qt, Qp])

$$\begin{bmatrix} -S \beta 1 - \mu & -\beta 1 P & 0 & 0 & 0 & 0 \\ S \beta 1 & P \beta 1 - X \beta 2 - \Omega 1 & -\beta 2 S & \Omega 2 & 0 & 0 \\ 0 & X \beta 2 & S \beta 2 - \Omega 3 - \Omega 4 & 0 & 0 & 0 \\ 0 & 0 & \omega & -\Omega 2 - \Omega 5 & \Omega 7 & 0 \\ 0 & 0 & 0 & \Omega 6 & -\Omega 7 - \mu & 0 \\ 0 & 0 & 0 & \Omega 8 & 0 & -\mu \end{bmatrix}$$

$$\begin{aligned}
> TKfix := & \left[ P = \frac{\Lambda}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu}, S = \frac{\Omega_3 + \Omega_4}{\beta_2}, X = ((\Omega_3 + \Omega_4) (\Lambda \beta_1 \beta_2 - \Omega_1 \Omega_3 \beta_1 \right. \\
& - \Omega_1 \Omega_4 \beta_1 - \Omega_1 \beta_2 \mu) (\Omega_2 \Omega_7 + \Omega_2 \mu + \Omega_5 \Omega_7 + \Omega_5 \mu - \Omega_6 \Omega_7)) / (\beta_2 (\Omega_3 \beta_1 \\
& + \Omega_4 \beta_1 + \beta_2 \mu) (\Omega_2 \Omega_3 \Omega_7 + \Omega_2 \Omega_3 \mu + \Omega_2 \Omega_4 \Omega_7 + \Omega_2 \Omega_4 \mu - \Omega_2 \Omega_7 \omega - \Omega_2 \mu \omega \\
& + \Omega_3 \Omega_5 \Omega_7 + \Omega_3 \Omega_5 \mu - \Omega_3 \Omega_6 \Omega_7 + \Omega_4 \Omega_5 \Omega_7 + \Omega_4 \Omega_5 \mu - \Omega_4 \Omega_6 \Omega_7)), Y \\
& = \frac{(\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu} + X \beta_1 \beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2}, Q_t \\
& = \frac{\Omega_6 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu} + X \beta_1 \beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2 (\Omega_7 + \mu)}, Q_p \\
& = \frac{\Omega_8 (\Omega_3 + \Omega_4) \left( -\frac{\Lambda \beta_1}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu} + X \beta_1 \beta_2 + \Omega_1 \right)}{\beta_2 \Omega_2 \mu} \Bigg] :
\end{aligned}$$

>  $Jac\_bintang := subs(TKfix, J)$

$$\left[ \left[ -\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} - \mu, -\frac{\Lambda \beta_1}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu}, 0, 0, 0, 0 \right], \right. \\ \left[ \frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2}, \frac{\Lambda \beta_1}{\frac{(\Omega_3 + \Omega_4) \beta_1}{\beta_2} + \mu} - ((\Omega_3 + \Omega_4) (\Lambda \beta_1 \beta_2 - \Omega_1 \Omega_3 \beta_1 \right. \\ \left. - \Omega_1 \Omega_4 \beta_1 - \Omega_1 \beta_2 \mu) (\Omega_2 \Omega_7 + \Omega_2 \mu + \Omega_5 \Omega_7 + \Omega_5 \mu - \Omega_6 \Omega_7)) / ((\Omega_3 \beta_1 \right. \\ \left. + \Omega_4 \beta_1 + \beta_2 \mu) (\Omega_2 \Omega_3 \Omega_7 + \Omega_2 \Omega_3 \mu + \Omega_2 \Omega_4 \Omega_7 + \Omega_2 \Omega_4 \mu - \Omega_2 \Omega_7 \omega - \Omega_2 \mu \omega \right. \\ \left. + \Omega_3 \Omega_5 \Omega_7 + \Omega_3 \Omega_5 \mu - \Omega_3 \Omega_6 \Omega_7 + \Omega_4 \Omega_5 \Omega_7 + \Omega_4 \Omega_5 \mu - \Omega_4 \Omega_6 \Omega_7)) - \Omega_1, -\Omega_3 \right. \\ \left. - \Omega_4, \Omega_2, 0, 0 \right], \\ \left[ 0, ((\Omega_3 + \Omega_4) (\Lambda \beta_1 \beta_2 - \Omega_1 \Omega_3 \beta_1 - \Omega_1 \Omega_4 \beta_1 - \Omega_1 \beta_2 \mu) (\Omega_2 \Omega_7 + \Omega_2 \mu \right. \\ \left. + \Omega_5 \Omega_7 + \Omega_5 \mu - \Omega_6 \Omega_7)) / ((\Omega_3 \beta_1 + \Omega_4 \beta_1 + \beta_2 \mu) (\Omega_2 \Omega_3 \Omega_7 + \Omega_2 \Omega_3 \mu \right. \\ \left. + \Omega_2 \Omega_4 \Omega_7 + \Omega_2 \Omega_4 \mu - \Omega_2 \Omega_7 \omega - \Omega_2 \mu \omega + \Omega_3 \Omega_5 \Omega_7 + \Omega_3 \Omega_5 \mu - \Omega_3 \Omega_6 \Omega_7 \right. \\ \left. + \Omega_4 \Omega_5 \Omega_7 + \Omega_4 \Omega_5 \mu - \Omega_4 \Omega_6 \Omega_7)) \right], 0, 0, 0, 0 \right], \\ \left[ 0, 0, \omega, -\Omega_2 - \Omega_5, \Omega_7, 0 \right], \\ \left[ 0, 0, 0, \Omega_6, -\Omega_7 - \mu, 0 \right], \\ \left[ 0, 0, 0, \Omega_8, 0, -\mu \right] \right]$$

$$> La := \begin{bmatrix} \text{lambda} & 0 & 0 & 0 & 0 & 0 \\ 0 & \text{lambda} & 0 & 0 & 0 & 0 \\ 0 & 0 & \text{lambda} & 0 & 0 & 0 \\ 0 & 0 & 0 & \text{lambda} & 0 & 0 \\ 0 & 0 & 0 & 0 & \text{lambda} & 0 \\ 0 & 0 & 0 & 0 & 0 & \text{lambda} \end{bmatrix} :$$

#agar lebih pendek misalkan saja per entry nya

#misalkan

$$\#k11 = \frac{(\Omega3 + \Omega4) \beta1}{\beta2} + \mu$$

$$\#k12 = \frac{\Lambda \beta1}{\frac{(\Omega3 + \Omega4) \beta1}{\beta2} + \mu}$$

$$\#k21 = \frac{(\Omega3 + \Omega4) \beta1}{\beta2}$$

$$\begin{aligned} \#k22 = & \left( (\Omega3 + \Omega4) (\Lambda \beta1 \beta2 - \Omega1 \Omega3 \beta1 - \Omega1 \Omega4 \beta1 - \Omega1 \beta2 \mu) (\Omega2 \Omega7 + \Omega2 \mu + \Omega5 \Omega7 \right. \\ & + \Omega5 \mu - \Omega6 \Omega7) \left. \right) / \left( (\Omega3 \beta1 + \Omega4 \beta1 + \beta2 \mu) (\Omega2 \Omega3 \Omega7 + \Omega2 \Omega3 \mu + \Omega2 \Omega4 \Omega7 \right. \\ & + \Omega2 \Omega4 \mu - \Omega2 \Omega7 \omega - \Omega2 \mu \omega + \Omega3 \Omega5 \Omega7 + \Omega3 \Omega5 \mu - \Omega3 \Omega6 \Omega7 + \Omega4 \Omega5 \Omega7 \\ & \left. + \Omega4 \Omega5 \mu - \Omega4 \Omega6 \Omega7) \right) + \Omega1 - \frac{\Lambda \beta1}{\frac{(\Omega3 + \Omega4) \beta1}{\beta2} + \mu} \end{aligned}$$

$$\#k23 = \Omega3 + \Omega4$$

$$\#k24 = \Omega2$$

$$\begin{aligned} \#k32 = & \left( (\Omega3 + \Omega4) (\Lambda \beta1 \beta2 - \Omega1 \Omega3 \beta1 - \Omega1 \Omega4 \beta1 - \Omega1 \beta2 \mu) (\Omega2 \Omega7 + \Omega2 \mu + \Omega5 \Omega7 \right. \\ & + \Omega5 \mu - \Omega6 \Omega7) \left. \right) / \left( (\Omega3 \beta1 + \Omega4 \beta1 + \beta2 \mu) (\Omega2 \Omega3 \Omega7 + \Omega2 \Omega3 \mu + \Omega2 \Omega4 \Omega7 \right. \\ & + \Omega2 \Omega4 \mu - \Omega2 \Omega7 \omega - \Omega2 \mu \omega + \Omega3 \Omega5 \Omega7 + \Omega3 \Omega5 \mu - \Omega3 \Omega6 \Omega7 + \Omega4 \Omega5 \Omega7 \\ & \left. + \Omega4 \Omega5 \mu - \Omega4 \Omega6 \Omega7) \right) \end{aligned}$$

$$\#k43 = \omega$$

$$\#k44 = \Omega2 + \Omega5$$

$$\#k45 = \Omega7$$

$$\#k54 = \Omega6$$

$$\#k55 = \Omega7 + \mu$$

$$\#k64 = \Omega8$$

$$\#k66 = \mu$$

$$\text{> } Jac\_bintang := \begin{bmatrix} -k11 & -k12 & 0 & 0 & 0 & 0 \\ k21 & -k22 & -k23 & k24 & 0 & 0 \\ 0 & k32 & 0 & 0 & 0 & 0 \\ 0 & 0 & k43 & -k44 & k45 & 0 \\ 0 & 0 & 0 & k54 & -k55 & 0 \\ 0 & 0 & 0 & k64 & 0 & -k66 \end{bmatrix}$$

>  $Jac\_bintangg - La$

$$\begin{bmatrix} -k_{11} - \lambda & -k_{12} & 0 & 0 & 0 & 0 \\ k_{21} & -k_{22} - \lambda & -k_{23} & k_{24} & 0 & 0 \\ 0 & k_{32} & -\lambda & 0 & 0 & 0 \\ 0 & 0 & k_{43} & -k_{44} - \lambda & k_{45} & 0 \\ 0 & 0 & 0 & k_{54} & -k_{55} - \lambda & 0 \\ 0 & 0 & 0 & k_{64} & 0 & -k_{66} - \lambda \end{bmatrix}$$

>  $Determinant(Jac\_bintangg - La)$

$$\begin{aligned} & (-k_{11}k_{22}k_{44}\lambda^2 - k_{11}k_{22}k_{55}\lambda^2 - k_{11}k_{44}k_{55}\lambda^2 + k_{11}k_{45}k_{54}\lambda^2 - k_{11}k_{23}k_{32}\lambda^2 \\ & - k_{22}k_{44}k_{55}\lambda^2 + k_{22}k_{45}k_{54}\lambda^2 - k_{23}k_{32}k_{44}\lambda^2 - k_{23}k_{32}k_{55}\lambda^2 + k_{24}k_{32}k_{43}\lambda^2 \\ & - k_{12}k_{21}k_{44}\lambda^2 - k_{12}k_{21}k_{55}\lambda^2 - k_{11}k_{22}k_{44}k_{55}\lambda + k_{11}k_{22}k_{45}k_{54}\lambda \\ & - k_{11}k_{23}k_{32}k_{44}k_{55} - k_{11}k_{23}k_{32}k_{44}\lambda + k_{11}k_{23}k_{32}k_{45}k_{54} - k_{11}k_{23}k_{32}k_{55}\lambda \\ & + k_{11}k_{24}k_{32}k_{43}k_{55} + k_{11}k_{24}k_{32}k_{43}\lambda - \lambda k_{23}k_{32}k_{44}k_{55} + \lambda k_{23}k_{32}k_{45}k_{54} \\ & + \lambda k_{24}k_{32}k_{43}k_{55} - k_{12}k_{21}k_{44}k_{55}\lambda + k_{12}k_{21}k_{45}k_{54}\lambda - k_{11}\lambda^4 - k_{22}\lambda^4 - k_{44}\lambda^4 \\ & - k_{55}\lambda^4 - \lambda^5 - k_{11}k_{22}\lambda^3 - k_{11}k_{44}\lambda^3 - k_{11}k_{55}\lambda^3 - k_{22}k_{44}\lambda^3 - k_{22}k_{55}\lambda^3 \\ & - k_{44}k_{55}\lambda^3 + k_{45}k_{54}\lambda^3 - k_{23}k_{32}\lambda^3 - k_{12}k_{21}\lambda^3) (-k_{66} - \lambda) \end{aligned}$$

#### LAMPIRAN 4. State, Costate, dan Syarat Stationer

> restart :

$$\begin{aligned}
 > H := A1 \cdot S + A2 \cdot X + A3 \cdot Y + \frac{B1}{2} \cdot u1^2 + \frac{B2}{2} \cdot u2^2 + \text{lambda1} \cdot (\text{Lambda} - \text{beta1} \cdot P \cdot S - \mu \\
 &\cdot P) + \text{lambda2} \cdot (\text{beta1} \cdot P \cdot S - \text{beta2} \cdot S \cdot X - (\rho + \mu) \cdot S + \tau u2 \cdot u2 \cdot Y) + \text{lambda3} \\
 &\cdot (\text{beta2} \cdot S \cdot X - (\eta + \omega + \mu) \cdot X - \tau u1 \cdot u1 \cdot X) + \text{lambda4} \cdot (\omega \cdot X - (\gamma + \mu) \cdot Y \\
 &+ \alpha \cdot (1 - u1) \cdot Q_t - \tau u2 \cdot u2 \cdot Y) + \text{lambda5} \cdot (\gamma \cdot (1 + u2) \cdot \delta \cdot Y \\
 &- (\mu + \alpha \cdot (1 - u1)) \cdot Q_t) + \text{lambda6} \cdot (\gamma \cdot (1 + u2) \cdot (1 - \delta) \cdot Y - \mu \cdot Q_p)
 \end{aligned}$$

#state

$$> \frac{\partial}{\partial \lambda 1} H$$

$$-P S \beta 1 - P \mu + \Lambda$$

$$> \frac{\partial}{\partial \lambda 2} H$$

$$\beta 1 P S - \beta 2 S X - (\rho + \mu) S + \tau u 2 Y$$

$$> \frac{\partial}{\partial \lambda 3} H$$

$$\beta 2 S X - (\eta + \omega + \mu) X - \tau u 1 X$$

$$> \frac{\partial}{\partial \lambda 4} H$$

$$\omega X - (\gamma + \mu) Y + \alpha (1 - u 1) Q_t - \tau u 2 Y$$

$$> \frac{\partial}{\partial \lambda 5} H$$

$$\gamma (1 + u 2) \delta Y - (\mu + \alpha (1 - u 1)) Q_t$$

$$> \frac{\partial}{\partial \lambda 6} H$$

$$\gamma (1 + u 2) (1 - \delta) Y - \mu Q_p$$

#costate

$$> -\frac{\partial}{\partial P} H$$

$$-\lambda 1 (-S \beta 1 - \mu) - \lambda 2 \beta 1 S$$

$$> -\frac{\partial}{\partial S} H$$

$$-A 1 + \lambda 1 \beta 1 P - \lambda 2 (P \beta 1 - X \beta 2 - \mu - \rho) - \lambda 3 \beta 2 X$$

$$> -\frac{\partial}{\partial X} H$$

$$-A 2 + \lambda 2 \beta 2 S - \lambda 3 (S \beta 2 - \tau u 1 - \eta - \mu - \omega) - \lambda 4 \omega$$

$$> -\frac{\partial}{\partial Y} H$$

$$-A 3 - \lambda 2 \tau u 2 - \lambda 4 (-\tau u 2 - \gamma - \mu) - \lambda 5 \gamma (1 + u 2) \delta - \lambda 6 \gamma (1 + u 2) (1 - \delta)$$

$$\begin{aligned} &> -\frac{\partial}{\partial Q_t} H && -\lambda_4 \alpha (1 - u_l) - \lambda_5 (-\mu - \alpha (1 - u_l)) \end{aligned}$$

$$\begin{aligned} &> -\frac{\partial}{\partial Q_p} H && \lambda_6 \mu \end{aligned}$$

#syarat stationer

$$\begin{aligned} &> Hu_1 := \frac{\partial}{\partial u_1} H && -Q_t \alpha \lambda_4 + Q_t \alpha \lambda_5 - X \lambda_3 \tau_l + B_1 u_l \end{aligned}$$

$$\begin{aligned} &> solve(Hu_1, u_1) && \frac{Q_t \alpha \lambda_4 - Q_t \alpha \lambda_5 + X \lambda_3 \tau_l}{B_1} \end{aligned}$$

$$\begin{aligned} &> Hu_2 := \frac{\partial}{\partial u_2} H && B_2 u_2 + \lambda_2 \tau_2 Y - \lambda_4 \tau_2 Y + \lambda_5 \gamma \delta Y + \lambda_6 \gamma (1 - \delta) Y \end{aligned}$$

$$\begin{aligned} &> solve(Hu_2, u_2) && \frac{Y (\delta \gamma \lambda_5 - \delta \gamma \lambda_6 + \gamma \lambda_6 + \lambda_2 \tau_2 - \lambda_4 \tau_2)}{B_2} \end{aligned}$$

## LAMPIRAN 5. Simulasi Numerik

### - Subprogram

```
function Kontrol
=simulasi_tesis(lambdaP0, lamda, beta1, beta2, rho, miu, eta, omega, alpha
, gamma, delta, tau1, tau2, u11, u22, u111, u222, A1, A2, A3, B1, B2, P0, S0, X0, Y
0, Qt0, Qp0, TP0, Ta)
M =500;
t=linspace(0, Ta, M+1); %dari waktu ke 0 sampai ke T sebanyak M+1
h=Ta/M; %panjang langkah
h2 = h/2; %panjang langkah dalam RK4

%membentuk matriks baris isinya nol 1 baris, M+1 kolom
P=zeros(1, M+1);
S=zeros(1, M+1);
X=zeros(1, M+1);
Y=zeros(1, M+1);
Qt=zeros(1, M+1);
Qp=zeros(1, M+1);
TP=zeros(1, M+1);

P1=zeros(1, M+1);
S1=zeros(1, M+1);
X1=zeros(1, M+1);
Y1=zeros(1, M+1);
Qt1=zeros(1, M+1);
Qp1=zeros(1, M+1);

P2=zeros(1, M+1);
S2=zeros(1, M+1);
X2=zeros(1, M+1);
Y2=zeros(1, M+1);
Qt2=zeros(1, M+1);
Qp2=zeros(1, M+1);

lambdaP=zeros(1, M+1);
lambdaS=zeros(1, M+1);
lambdaX=zeros(1, M+1);
lambdaY=zeros(1, M+1);
lambdaQt=zeros(1, M+1);
lambdaQp=zeros(1, M+1);

u1=zeros(1, M+1);
u2=zeros(1, M+1);

%nilai awal keadaan
P(1)=P0;
S(1)=S0;
X(1)=X0;
Y(1)=Y0;
Qt(1)=Qt0;
Qp(1)=Qp0;
```



```
P1(1)=P0;  
S1(1)=S0;  
X1(1)=X0;  
Y1(1)=Y0;  
Qt1(1)=Qt0;  
Qp1(1)=Qp0;
```

```
P2(1)=P0;  
S2(1)=S0;  
X2(1)=X0;  
Y2(1)=Y0;  
Qt2(1)=Qt0;  
Qp2(1)=Qp0;
```

```
lambdaP(1)= lambdaP0;
```

```
kk=0  
test=-1 %variabel uji konvergensi  
deta=0.0001; %nilai toleransi
```

```
while (test<0) %supaya diperoleh hasil fungsi tujuan yang non  
negatif
```

```
%nilai awal dari iterasi while  
%mengganti nilai lama dengan nilai yang baru  
oldu1 = u1;  
oldu2 = u2;
```

```
oldP =P;  
oldS =S;  
oldX =X;  
oldY =Y;  
oldQt =Qt;  
oldQp =Qp;
```

```
oldlambdaP =lambdaP;  
oldlambdaS = lambdaS;  
oldlambdaX = lambdaX;  
oldlambdaY = lambdaY;  
oldlambdaQt = lambdaQt;  
oldlambdaQp = lambdaQp;
```

```
for i = 1:M  
kk=kk+1; %menunjukkan setiap kali iterasi selalu bertambah satu  
oldu1 = u1;  
oldu2 = u2;
```

```
fprintf('iterasi ke = %i \n ',kk)
```

```

%STATE
for i = 1:M
m1P = lamda - beta1*P(i)*S(i) - miu*P(i);
m1S = beta1*P(i)*S(i) - beta2*S(i)*X(i) - (rho+miu)*S(i) +
tau2*u2(i)*Y(i);
m1X = beta2*S(i)*X(i)-(eta+omega+miu)*X(i)-tau1*u1(i)*X(i);
m1Y = omega*X(i) - (gamma+miu)*Y(i) + alpha*(1-u1(i))*Qt(i) -
tau2*u2(i)*Y(i);
m1Qt = gamma*(1+u2(i))*delta*Y(i) - (miu + alpha*(1-u1(i)))*Qt(i);
m1Qp= gamma*(1+u2(i))*(1-delta)*Y(i)-miu*Qp(i);

m2P = lamda - beta1*(P(i)+h2*m1P)*(S(i)+h2*m1S)-miu*(P(i)+h2*m1P);
m2S = beta1*(P(i)+h2*m1P)*(S(i)+h2*m1S) -
beta2*(S(i)+h2*m1S)*(X(i)+h2*m1X) - (rho+miu)*(S(i)+h2*m1S) +
tau2*0.5*(u2(i)+u2(i+1))*Y(i)+h2*m1Y);
m2X = beta2*(S(i)+h2*m1S)*(X(i)+h2*m1X)-
(eta+omega+miu)*(X(i)+h2*m1X)-
tau1*0.5*(u1(i)+u1(i+1))*(X(i)+h2*m1X);
m2Y = omega*(X(i)+h2*m1X) - (gamma+miu)*(Y(i)+h2*m1Y) +
alpha*0.5*((1-u1(i))+(1-u1(i+1)))*(Qt(i)+h2*m1Qt) -
tau2*0.5*(u2(i)+u2(i+1))*(Y(i)+h2*m1Y);
m2Qt = gamma*0.5*((1+u2(i))+(1+u2(i+1)))*delta*(Y(i)+h2*m1Y) -
(miu + alpha*0.5*((1-u1(i))+(1-u1(i+1))))*(Qt(i)+h2*m1Qt);
m2Qp= gamma*0.5*((1+u2(i))+(1+u2(i+1)))*(1-delta)*(Y(i)+h2*m1Y)-
miu*(Qp(i)+h2*m1Qp);

m3P = lamda - beta1*(P(i)+h2*m2P)*(S(i)+h2*m2S)-miu*(P(i)+h2*m2P);
m3S = beta1*(P(i)+h2*m2P)*(S(i)+h2*m2S) -
beta2*(S(i)+h2*m2S)*(X(i)+h2*m2X) - (rho+miu)*(S(i)+h2*m2S) +
tau2*0.5*(u2(i)+u2(i+1))*Y(i)+h2*m2Y);
m3X = beta2*(S(i)+h2*m2S)*(X(i)+h2*m2X)-
(eta+omega+miu)*(X(i)+h2*m2X)-
tau1*0.5*(u1(i)+u1(i+1))*(X(i)+h2*m2X);
m3Y = omega*(X(i)+h2*m2X) - (gamma+miu)*(Y(i)+h2*m2Y) +
alpha*0.5*((1-u1(i))+(1-u1(i+1)))*(Qt(i)+h2*m2Qt) -
tau2*0.5*(u2(i)+u2(i+1))*Y(i)+h2*m2Y);
m3Qt = gamma*0.5*((1+u2(i))+(1+u2(i+1)))*delta*(Y(i)+h2*m2Y) -
(miu + alpha*0.5*((1-u1(i))+(1-u1(i+1))))*(Qt(i)+h2*m2Qt);
m3Qp= gamma*0.5*((1+u2(i))+(1+u2(i+1)))*(1-delta)*(Y(i)+h2*m2Y)-
miu*(Qp(i)+h2*m2Qp);

m4P = lamda - beta1*(P(i)+h*m3P)*(S(i)+h*m3S)-miu*(P(i)+h*m3P);
m4S = beta1*(P(i)+h*m3P)*(S(i)+h*m3S) -
beta2*(S(i)+h*m3S)*(X(i)+h*m3X) - (rho+miu)*(S(i)+h*m3S) +
tau2*u2(i+1)*(Y(i)+h*m3Y);
m4X = beta2*(S(i)+h*m3S)*(X(i)+h*m3X)-
(eta+omega+miu)*(X(i)+h*m3X)-tau1*(u1(i+1))*(X(i)+h*m3X);
m4Y = omega*(X(i)+h*m3X) - (gamma+miu)*(Y(i)+h*m3Y) + alpha*(1-
u1(i+1))*(Qt(i)+h*m3Qt) - tau2*u2(i+1)*(Y(i)+h*m3Y);
m4Qt = gamma*(1+u2(i+1))*delta*(Y(i)+h*m3Y) - (miu + alpha*(1-
u1(i+1)))*(Qt(i)+h*m3Qt);
m4Qp= gamma*(1+u2(i+1))*(1-delta)*(Y(i)+h*m3Y)-miu*(Qp(i)+h*m3Qp);

```

```

P(i+1) = P(i) + (h/6)*(m1P + 2*m2P + 2*m3P + m4P);
S(i+1) = S(i) + (h/6)*(m1S + 2*m2S + 2*m3S + m4S);
X(i+1) = X(i) + (h/6)*(m1X + 2*m2X + 2*m3X + m4X);
Y(i+1) = Y(i) + (h/6)*(m1Y + 2*m2Y + 2*m3Y + m4Y);
Qt(i+1) = Qt(i) + (h/6)*(m1Qt + 2*m2Qt + 2*m3Qt + m4Qt);
Qp(i+1) = Qp(i) + (h/6)*(m1Qp + 2*m2Qp + 2*m3Qp + m4Qp);

```

```
end
```

```
%COSTATE
```

```

for i = 1:M
    j = M + 2 - i;
    m1P = -lambdaP(j).*(-beta1*S(j)-miu)-lambdaS(j).*beta1*S(j);
    m1S = -A1+lambdaP(j).*beta1*P(j)-lambdaS(j).(beta1*P(j)-
    beta2*X(j)-miu-rho)-lambdaX(j).*beta2*X(j);
    m1X = -A2+lambdaS(j).*beta2*S(j)-lambdaX(j).(beta2*S(j)-
    tau1*u1(j)-eta-miu-omega)-lambdaY(j)*omega;
    m1Y = -A3-lambdaS(j).*tau2*u2(j)-lambdaY(j).*(-tau2*u2(j)-gamma-
    miu)-lambdaQt(j).*gamma*(1+u2(j))*delta-
    lambdaQp(j).*gamma*(1+u2(j))*(1-delta);
    m1Qt = -lambdaY(j).*alpha*(1-u1(j))-lambdaQt(j).*(-miu-alpha*(1-
    u1(j)));
    m1Qp = lambdaQp(j)*miu;

    m2P = -(lambdaP(j)-h2*m1P).*(-beta1*(S(j)-S(j-1))-miu)-
    (lambdaS(j)-h2*m1S).*beta1*(S(j)+S(j-1));
    m2S = -A1+(lambdaP(j)-h2*m1P).*beta1*(P(j)+P(j-1))-(lambdaS(j)-
    h2*m1S).(beta1*(P(j)+P(j-1))-beta2*(X(j)+X(j-1))-miu-rho)-
    (lambdaX(j)-h2*m1X).*beta2*(X(j)+X(j-1));
    m2X = -A2+(lambdaS(j)-h2*m1S).*beta2*(S(j)+S(j-1))-(lambdaX(j)-
    h2*m1X).(beta2*(S(j)+S(j-1))-tau1*0.5*(u1(j)+u1(j-1))-eta-miu-
    omega)-(lambdaY(j)-h2*m1Y)*omega;
    m2Y = -A3-(lambdaS(j)-h2*m1S).*tau2*0.5*(u2(j)+u2(j-1))-
    (lambdaY(j)-h2*m1Y).*(-tau2*0.5*(u2(j)+u2(j-1))-gamma-miu)-
    (lambdaQt(j)-h2*m1Qt).*gamma*0.5*((1+u2(j))+(1+u2(j-1)))*delta-
    (lambdaQp(j)-h2*m1Qp).*gamma*0.5*((1+u2(j))+(1+u2(j-1)))*(1-
    delta);
    m2Qt = -(lambdaY(j)-h2*m1Y).*alpha*0.5*((1-u1(j))+(1-u1(j-1)))-
    (lambdaQt(j)-h2*m1Qt).*(-miu-alpha*0.5*((1-u1(j))+(1-u1(j-1)))));
    m2Qp = (lambdaQp(j)-h2*m1Qp)*miu;

    m3P = -(lambdaP(j)-h2*m2P).*(-beta1*(S(j)-S(j-1))-miu)-
    (lambdaS(j)-h2*m2S).*beta1*(S(j)+S(j-1));
    m3S = -A1+(lambdaP(j)-h2*m2P).*beta1*(P(j)+P(j-1))-(lambdaS(j)-
    h2*m2S).(beta1*(P(j)+P(j-1))-beta2*(X(j)+X(j-1))-miu-rho)-
    (lambdaX(j)-h2*m2X).*beta2*(X(j)+X(j-1));
    m3X = -A2+(lambdaS(j)-h2*m2S).*beta2*(S(j)+S(j-1))-(lambdaX(j)-
    h2*m2X).(beta2*(S(j)+S(j-1))-tau1*0.5*(u1(j)+u1(j-1))-eta-miu-
    omega)-(lambdaY(j)-h2*m2Y)*omega;
    m3Y = -A3-(lambdaS(j)-h2*m2S).*tau2*0.5*(u2(j)+u2(j-1))-
    (lambdaY(j)-h2*m2Y).*(-tau2*0.5*(u2(j)+u2(j-1))-gamma-miu)-
    (lambdaQt(j)-h2*m2Qt).*gamma*0.5*((1+u2(j))+(1+u2(j-1)))*delta-

```

```

(lambdaQp(j)-h2*m2Qp).*gamma*0.5*((1+u2(j))+(1+u2(j-1)))*(1-
delta);
m3Qt= -(lambdaY(j)-h2*m2Y).*alpha*0.5*((1-u1(j))+(1-u1(j-1)))-
(lambdaQt(j)-h2*m2Qt).*(-miu-alpha*0.5*((1-u1(j))+(1-u1(j-1)))));
m3Qp= (lambdaQp(j)-h2*m2Qp)*miu;

m4P = -(lambdaP(j)-h*m3P).*(-beta1*S(j-1)-miu)-(lambdaS(j)-
h*m3S).*beta1*(S(j-1));
m4S = -A1+(lambdaP(j)-h*m3P).*beta1*(P(j-1))-(lambdaS(j)-
h*m3S).*beta1*(P(j-1))-beta2*(X(j-1))-miu-rho)-(lambdaX(j)-
h*m3X).*beta2*(X(j-1));
m4X = -A2+(lambdaS(j)-h*m3S).*beta2*(S(j-1))-(lambdaX(j)-
h*m3X).*beta2*(S(j-1))-tau1*(u1(j-1))-eta-miu-omega)-(lambdaY(j)-
h*m3Y)*omega;
m4Y = -A3-(lambdaS(j)-h*m3S).*tau2*(u2(j-1))-(lambdaY(j)-
h*m3Y).*(-tau2*(u2(j-1))-gamma-miu)-(lambdaQt(j)-
h*m3Qt).*gamma*(1+u2(j-1))*delta-(lambdaQp(j)-
h*m3Qp).*gamma*(1+u2(j-1))*(1-delta);
m4Qt= -(lambdaY(j)-h*m3Y).*alpha*(1-u1(j-1))-(lambdaQt(j)-
h*m3Qt).*(-miu-alpha*(1-u1(j-1)));
m4Qp= (lambdaQp(j)-h*m3Qp)*miu;

lambdaP(j-1) = lambdaP(j) - (h/6)*(m1P + 2*m2P + 2*m3P + m4P);
lambdaS(j-1) = lambdaS(j) - (h/6)*(m1S + 2*m2S + 2*m3S + m4S);
lambdaX(j-1) = lambdaX(j) - (h/6)*(m1X + 2*m2X + 2*m3X + m4X);
lambdaY(j-1) = lambdaY(j) - (h/6)*(m1Y + 2*m2Y + 2*m3Y + m4Y);
lambdaQt(j-1) = lambdaQt(j) - (h/6)*(m1Qt + 2*m2Qt + 2*m3Qt + m4Qt);
lambdaQp(j-1) = lambdaQp(j) - (h/6)*(m1Qp + 2*m2Qp + 2*m3Qp + m4Qp);

u1(j) = min(1, max((-lambdaQt(j) -
lambdaY(j)).*alpha*Qt(i) + lambdaX(j).*tau1*X(i))/B1));
u2(j) = min(1, max((-lambdaS(j) - lambdaY(j)).*tau2*Y(i) -
(lambdaQt(j)*delta + lambdaQp(j)*(1-delta)).*gamma*Y(i))/B2));

end

for i = 1:M
%LANJUT KE TANPA KONTROL (u11=0, u22=0)

m1P1 = lamda - beta1*P1(i)*S1(i) - miu*P1(i);
m1S1 = beta1*P1(i)*S1(i) - beta2*S1(i)*X1(i) - (rho+miu)*S1(i) +
tau2*u22*Y1(i);
m1X1 = beta2*S1(i)*X1(i) - (eta+omega+miu)*X1(i) - tau1*u11*X1(i);
m1Y1 = omega*X1(i) - (gamma+miu)*Y1(i) + alpha*(1-u11)*Qt1(i) -
tau2*u22*Y1(i);
m1Qt1 = gamma*(1+u22)*delta*Y1(i) - (miu + alpha*(1-u11))*Qt1(i);
m1Qp1 = gamma*(1+u22)*(1-delta)*Y1(i) - miu*Qp1(i);

m2P1 = lamda - beta1*(P1(i)+h2*m1P1)*(S1(i)+h2*m1S1) -
miu*(P1(i)+h2*m1P1);

```

```

m2S1 = beta1*(P1(i)+h2*m1P1)*(S1(i)+h2*m1S1) -
beta2*(S1(i)+h2*m1S1)*(X1(i)+h2*m1X1) - (rho+miu)*(S1(i)+h2*m1S1)
+ tau2*u22*(Y1(i)+h2*m1Y1);
m2X1 = beta2*(S1(i)+h2*m1S1)*(X1(i)+h2*m1X1)-
(eta+omega+miu)*(X1(i)+h2*m1X1)-tau1*u11*(X1(i)+h2*m1X1);
m2Y1 = omega*(X1(i)+h2*m1X1) - (gamma+miu)*(Y1(i)+h2*m1Y1) +
alpha*(1-u11)*(Qt1(i)+h2*m1Qt1) - tau2*u22*(Y1(i)+h2*m1Y1);
m2Qt1 = gamma*(1+u22)*delta*(Y1(i)+h2*m1Y1) - (miu + alpha*(1-
u11))*(Qt1(i)+h2*m1Qt1);
m2Qp1= gamma*(1+u22)*(1-delta)*(Y1(i)+h2*m1Y1)-
miu*(Qp1(i)+h2*m1Qp1);

```

```

m3P1 = lamda - beta1*(P1(i)+h2*m2P1)*(S1(i)+h2*m2S1)-
miu*(P1(i)+h2*m2P1);
m3S1 = beta1*(P1(i)+h2*m2P1)*(S1(i)+h2*m2S1) -
beta2*(S1(i)+h2*m2S1)*(X1(i)+h2*m2X1) - (rho+miu)*(S1(i)+h2*m2S1)
+ tau2*u22*(Y1(i)+h2*m2Y1);
m3X1 = beta2*(S1(i)+h2*m2S1)*(X1(i)+h2*m2X1)-
(eta+omega+miu)*(X1(i)+h2*m2X1)-tau1*u11*(X1(i)+h2*m2X1);
m3Y1 = omega*(X1(i)+h2*m2X1) - (gamma+miu)*(Y1(i)+h2*m2Y1) +
alpha*(1-u11)*(Qt1(i)+h2*m2Qt1) - tau2*u22*(Y1(i)+h2*m2Y1);
m3Qt1 = gamma*u22*delta*(Y1(i)+h2*m2Y1) - (miu + alpha*(1-
u11))*(Qt1(i)+h2*m2Qt1);
m3Qp1= gamma*(1+u22)*(1-delta)*(Y1(i)+h2*m2Y1)-
miu*(Qp1(i)+h2*m2Qp1);

```

```

m4P1 = lamda - beta1*(P1(i)+h*m3P1)*(S1(i)+h*m3S1)-
miu*(P1(i)+h*m3P1);
m4S1 = beta1*(P1(i)+h*m3P1)*(S1(i)+h*m3S1) -
beta2*(S1(i)+h*m3S1)*(X1(i)+h*m3X1) - (rho+miu)*(S1(i)+h*m3S1) +
tau2*u22*(Y1(i)+h*m3Y1);
m4X1 = beta2*(S1(i)+h*m3S1)*(X1(i)+h*m3X1)-
(eta+omega+miu)*(X1(i)+h*m3X1)-tau1*u22*(X1(i)+h*m3X1);
m4Y1 = omega*(X1(i)+h*m3X1) - (gamma+miu)*(Y1(i)+h*m3Y1) +
alpha*(1-u11)*(Qt1(i)+h*m3Qt1) - tau2*u22*(Y1(i)+h*m3Y1);
m4Qt1 = gamma*(1+u22)*delta*(Y1(i)+h*m3Y1) - (miu + alpha*(1-
u11))*(Qt1(i)+h*m3Qt1);
m4Qp1= gamma*(1+u22)*(1-delta)*(Y1(i)+h*m3Y1)-
miu*(Qp1(i)+h*m3Qp1);

```

```

P1(i+1) = P1(i) + (h/6)*(m1P1 + 2*m2P1 + 2*m3P1 + m4P1);
S1(i+1) = S1(i) + (h/6)*(m1S1 + 2*m2S1 + 2*m3S1 + m4S1);
X1(i+1) = X1(i) + (h/6)*(m1X1 + 2*m2X1 + 2*m3X1 + m4X1);
Y1(i+1) = Y1(i) + (h/6)*(m1Y1 + 2*m2Y1 + 2*m3Y1 + m4Y1);
Qt1(i+1) = Qt1(i)+ (h/6)*(m1Qt1+ 2*m2Qt1+ 2*m3Qt1+ m4Qt1);
Qp1(i+1)= Qp1(i)+ (h/6)*(m1Qp1+ 2*m2Qp1+ 2*m3Qp1+ m4Qp1);

```

end

```

%temp1 = nilai u1, temp2 = nilai u2
temp1 = (- (lambdaQt-lambdaY).*alpha.*Qt+lambdaX.*tau1.*X)/B1;

```

```

temp2 = (-(lambdaS-lambdaY).*tau2.*Y-
(lambdaQt.*delta+lambdaQp.*(1-delta).*gamma.*Y))/B2;

%ua = u1*, ub = u2*
ua = min(1,max(0,temp1));
ub = min(1,max(0,temp2));

%u diperbaharui dengan (u_awal+u_baru)/2
u1 = 0.5*(ua + oldu1);
u2 = 0.5*(ub + oldu2);

%uji konvergensi
%tempu1 = solusi optimal dari u1 diuji dengan = delta*||u1||-||u1-
u_lama||>=0
%tempu2 = solusi optimal dari u1 diuji dengan = delta*||u2||-||u2-
u_lama||>=0
tempu1 = deta*sum(abs(u1)) - sum(abs(oldu1 - u1));
tempu2 = deta*sum(abs(u2)) - sum(abs(oldu2 - u2));

tempP = deta*sum(abs(P)) - sum(abs(oldP - P));
tempS = deta*sum(abs(S)) - sum(abs(oldS - S));
tempX = deta*sum(abs(X)) - sum(abs(oldX - X));
tempY = deta*sum(abs(Y)) - sum(abs(oldY - Y));
tempQt= deta*sum(abs(Qt)) - sum(abs(oldQt - Qt));
tempQp= deta*sum(abs(Qp)) - sum(abs(oldQp - Qp));

temp1P = deta*sum(abs(lambdaP)) - sum(abs(olddlambdP -
lambdaP));
temp1S = deta*sum(abs(lambdaS)) - sum(abs(olddlambdS -
lambdaS));
temp1X = deta*sum(abs(lambdaX)) - sum(abs(olddlambdX -
lambdaX));
temp1Y = deta*sum(abs(lambdaY)) - sum(abs(olddlambdY -
lambdaY));
temp1Qt= deta*sum(abs(lambdaQt))- sum(abs(olddlambdQt-
lambdaQt));
temp1Qp= deta*sum(abs(lambdaQp))- sum(abs(olddlambdQp-
lambdaQp));

test = min(tempu1,min(tempu2,min(tempP,min(tempS,
min(tempX,min(tempY, min(tempQt, min(tempQp, min( temp1P,
min(temp1S, min(temp1X, min(temp1Y, min(temp1Qt,
temp1Qp))))))))));
disp(['it: ', num2str(kk), ', Test: ', num2str(test)]);

end
end

fprintf('jumlah iterasi = %i ',kk)
Kontrol(1,:) = t;

Kontrol(2,:) = P;
Kontrol(3,:) = S;

```

```

Kontrol(4,:) = X;
Kontrol(5,:) = Y;
Kontrol(6,:) = Qp;
Kontrol(7,:) = Qt;

Kontrol(8,:) = u1;
Kontrol(9,:) = u2;

Kontrol(10,:) = P1;
Kontrol(11,:) = S1;
Kontrol(12,:) = X1;
Kontrol(13,:) = Y1;
Kontrol(14,:) = Qp1;
Kontrol(15,:) = Qt1;

Kontrol(16,:) = P2;
Kontrol(17,:) = S2;
Kontrol(18,:) = X2;
Kontrol(19,:) = Y2;
Kontrol(20,:) = Qp2;
Kontrol(21,:) = Qt2;

fprintf('Hasil Akhir = Ko(:,end) ')

```

### - Program utama

```

clc
pilih1=0;
pilih2=0;

lamda = 1000;
beta1 =0.003 ;
beta2 =0.002;
rho =0.003;
miu =0.002;
eta =0.003;
omega =0.004;
alpha =1;

gamma =0.1183;

delta =0.5;
tau1 =0.5; %asumsi
tau2 =0.5; %asumsi

TP0=500000;
u11 =0;
u22 =0;

u111 =0.5; %asumsi

```

```

u222 =0.5; %asumsi

A1=20;
A2=20;
A3=60;
B1=50;
B2=50;

P0=3000; %3000
S0=2000; %2000
X0=1000; %1000
Y0=2000; %2000
Qt0=1000; %1000
Qp0=1000; %1000
lambdaP0=0;

Ta=20 ;

Ko =
simulasi_tesis(lambdaP0, lamda, beta1, beta2, rho, miu, eta, omega, alpha,
gamma, delta, tau1, tau2, u11, u22, u111, u222, A1, A2, A3, B1, B2, P0, S0, X0, Y0
, Qt0, Qp0, TP0, Ta);
disp(' ')
clc

while(pilih1==0)
disp(' PILIH GRAFIK HASIL SIMULASI YANG INGIN DI TAMPILKAN')
disp(' ATAU MENGAKHIRI SIMULASI')
disp('=====')
disp('')
disp(' 1. INDIVIDU POTENTIAL SMOKERS (P)')
disp(' 2. INDIVIDU SNUFFING CLASS (S)')
disp(' 3. INDIVIDU IRREGULAR SMOKERS (X)')
disp(' 4. INDIVIDU REGULAR SMOKERS (Y)')
disp(' 5. INDIVIDU TEMPORARY QUITTERS (Qt)')
disp(' 6. INDIVIDU PERMANENT QUITTERS (Qp)')
disp(' 7. TINGKAT KONTROL U1 dan U2 ')
disp(' 8. SELESAI')
disp(' 9. LambdaP')
disp('')
disp('')
pilih2=input('SILAHKAN PILIH 1, 2, 3, 4, 5 , 6, 7 atau 8 :');
disp('')
disp('')

if pilih2==1
figure (1)
plot(Ko(1,:),Ko(2,:), 'blue', 'linewidth',1.5);
hold on
plot(Ko(1,:),Ko(10,:), 'red', 'linewidth',1.5);
xlabel('Waktu (dalam tahun)')
ylabel('P(t)')
legend('P dengan kontrol ', 'P tanpa kontrol')
grid on;

```



```

pilih1=0;
elseif(pilih2==2)
    figure (2)
plot(Ko(1,:),Ko(3,:), 'blue',Ko(1,:),Ko(11,:), 'red', 'linewidth',1.5
);
xlabel('Waktu (dalam tahun)')
ylabel('S(t)')
legend('S dengan kontrol Optimal','S tanpa kontrol')
grid on;

pilih1=0;
elseif(pilih2==3)
    figure (3)
plot(Ko(1,:),Ko(4,:), 'blue',Ko(1,:),Ko(12,:), 'red', 'linewidth',1.5
);
xlabel('Waktu (dalam tahun)')
ylabel('X(t)')
legend('X dengan kontrol Optimal','X tanpa kontrol')
grid on;

pilih1=0;
elseif(pilih2==4)
    figure (4)
plot(Ko(1,:),Ko(5,:), 'blue',Ko(1,:),Ko(13,:), 'red', 'linewidth',1.5
);
xlabel('Waktu (dalam tahun)')
ylabel('Y(t)')
legend('Y dengan kontrol Optimal','Y tanpa kontrol')
grid on;

pilih1=0;
elseif(pilih2==5)
    figure (5)
plot(Ko(1,:),Ko(6,:), 'blue',Ko(1,:),Ko(14,:), 'red', 'linewidth',1.5
);
xlabel('Waktu (dalam tahun)')
ylabel('Qt(t)')
legend('Qt dengan kontrol Optimal','Qt tanpa kontrol')
grid on;

pilih1=0;
elseif(pilih2==6)
    figure (6)
plot(Ko(1,:),Ko(7,:), 'blue',Ko(1,:),Ko(15,:), 'red', 'linewidth',1.5
);
xlabel('Waktu (dalam tahun)')
ylabel('Qp(t)')
legend('Qp dengan kontrol Optimal','Qp tanpa kontrol')
grid on;

pilih1=0;
elseif(pilih2==7)
    figure (7)

```

```

plot(Ko(1,:),Ko(8,:), 'blue',Ko(1,:),Ko(9,:), 'red', 'linewidth',1.5)
;
xlabel('Waktu (dalam tahun)')
ylabel('u1*, u2*')
legend('u1','u2')
grid on;

elseif (pilih2==8)
    pilih1=1;
end
end

%SIMULASI VARIASI PARAMETER,
%simulasi satu per satu, nanti grafiknya tinggal di copy untuk
digabungkan

%CATATAN
%lurus = nilai standar
%...= nilai dibawah tandar
%--- = nilai di atas standar

%clc
%figure (2)
%plot(Ko(1,:),Ko(3,:), 'blue',Ko(1,:),Ko(11,:), 'red', 'linewidth',1.5);
%xlabel('Waktu (dalam tahun)')
%ylabel('S(t)')
%legend('S dengan kontrol Optimal','S tanpa kontrol')
%grid on;

%figure (2)
%plot(Ko(1,:),Ko(4,:), 'blue',Ko(1,:),Ko(12,:), 'red', 'linewidth',1.5);
%xlabel('Waktu (dalam tahun)')
%ylabel('X(t)')
%legend('X dengan kontrol Optimal','X tanpa kontrol')
%grid on;

%figure (2)
%plot(Ko(1,:),Ko(5,:), 'blue',Ko(1,:),Ko(13,:), 'red', 'linewidth',1.5);
%xlabel('Waktu (dalam tahun)')
%ylabel('Y(t)')
%legend('Y dengan kontrol Optimal','Y tanpa kontrol')
%grid on;

disp('')
disp('')
disp('')
disp('')
disp('HASIL AKHIR SIMULASI')
Ko(:,end)
pilih1=1;
disp('SELESAI')

```