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LAMPIRAN


Lampiran 1. Log Book Penelitian



Judul Penelitian : Studi Perkuatan Lentur Balok Beton Bertulang Pasca Korosi dengan Grouting dan GFRP Sheet

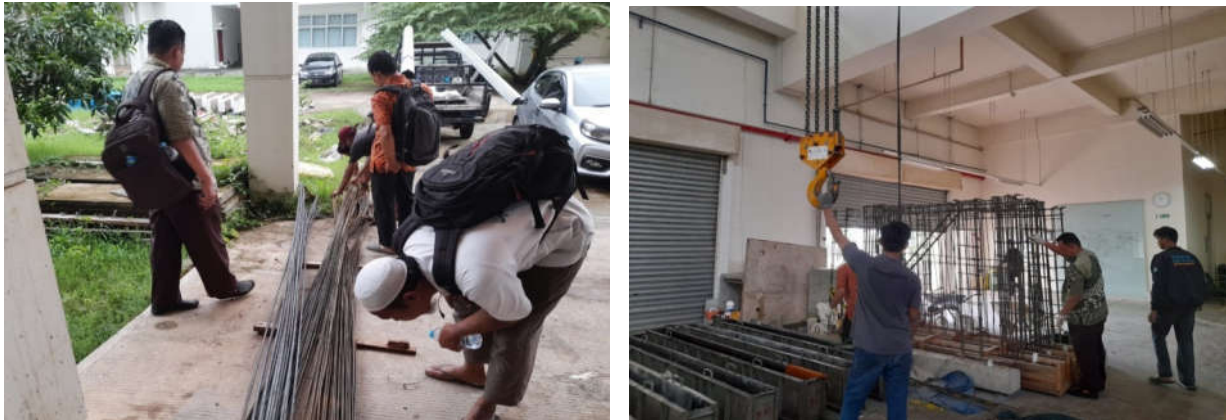
Nama Peneliti : Sugira Said

No.	Tanggal	Kegiatan	Hasil, Problem dan Solusi
1	14 Januari 2022	Pertemuan dan diskusi dengan tim penelitian dan mengurus administrasi mengenai perizinan penggunaan Laboratorium Struktur dan Bahan	Hasil: Problem : Solusi :
Progres : Dokumentasi :			
2	18 Januari 2022	Pertemuan dan diskusi dengan tim penelitian membahas : <ul style="list-style-type: none"> - Persiapan pembuatan benda uji - Kelengkapan material 	Hasil : Problem : Solusi :
Progres : Dokumentasi :			



3	19 Januari 2022	Perakitan Bekisting untuk benda uji balok	Hasil: Problem : Solusi :
Progres : Dokumentasi : 			

4	20 Januari 2022	Pertemuan dan diskusi dengan tim penelitian	Hasil: Problem : Solusi :
Progres : Dokumentasi :			
			

5	21 Januari 2022	<p>Pertemuan dan diskusi dengan tim penelitian membahas :</p> <ul style="list-style-type: none">- Persiapan pembuatan benda uji- Kelengkapan material dalam hal ini adalah pengadaan besi <p>Pengangkatan sampel di Laboratorium Struktur dan Bahan</p> <p>Melanjutan perakitan Bekisting untuk benda uji balok</p>	<p>Hasil:</p> <p>Problem : -</p> <p>Solusi : -</p>
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="390 659 995 1117"></div> <div data-bbox="1010 659 1619 1117"></div>			



6	22 Januari 2022	Melanjutkan Perakitan bekisting (pengencangan baut-baut pada bekisting) Pemotongan besi untuk tulangan balok	Hasil: 8 set bekisting selesai Problem : Solusi :
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Progres :			
Dokumentasi :			



7

23 Januari 2022

Melanjutkan pembuatan set tulangan

Hasil: 3 set tulangan selesai**Problem :****Solusi :****Progres :****Dokumentasi :**

8	24 Januari 2022	Melanjutkan pembuatan set tulangan	Hasil: 3 Set tulangan selesai, total 6 set tulangan selesai Problem : Solusi :
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Progres :

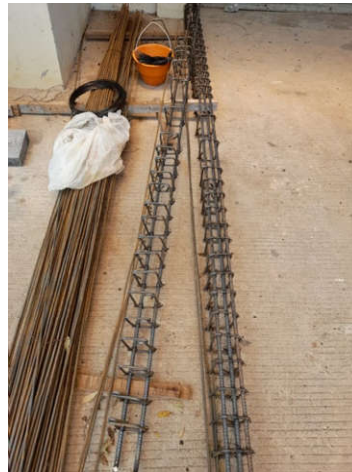
Dokumentasi :





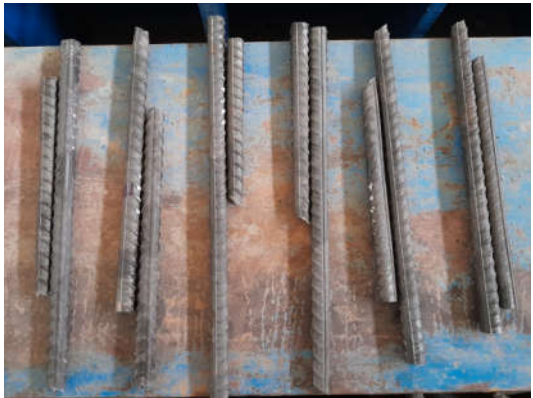
9	25 Januari 2022	Melanjutkan pembuatan set tulangan	Hasil : 3 set tulangan selesai, total 9 set tulangan selesai Problem : Solusi :
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Progres :

Dokumentasi :



10	27 Januari 2021	Pengujian Kuat Tarik Tulangan dan FRP <ul style="list-style-type: none">- 8 buah tulangan D13- 8 buah tulangan 8	Hasil: 8 buah tulangan D13 selesai Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div style="display: flex; justify-content: space-around; align-items: center;"></div>			



11	28 Januari 202	<p>Melanjutkan Pengujian Kuat Tarik Tulangan dan FRP</p> <ul style="list-style-type: none"> - 8 buah tulangan D13 - 8 buah tulangan 8 - 2 buah lapisan GFRP <p>Perakitan Mould Silinder ukuran 10 x 20</p>	<p>Hasil: - 8 buah tulangan 8 selesai, 8 buah tulangan D13 selesai, dan 2 buah GFRP selesai.</p> <p>Problem : -</p> <p>Solusi : -</p>
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Progres :

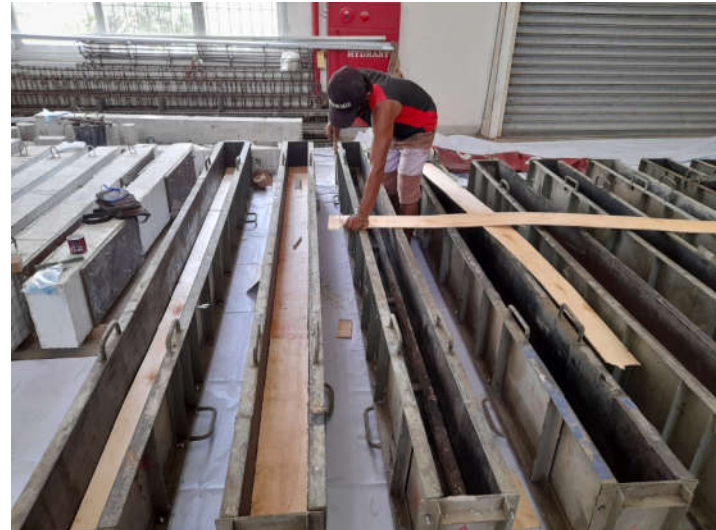
Dokumentasi :



12	30 Januari 2022	<ul style="list-style-type: none">- Pemberian alas pada bekisting- Melanjutkan perakitan Mould Silinder 10 x 20- Perakitan Mould Silinder 15 x 30- Perakitan Mould Balok 10 x 10 x 40	<p>Hasil: 24 set mould silinder 10 x 20 selesai, 13 set mould silinder 15 x 30 selesai dan 8 set mould balok 10 x 10 x 40 selesai</p> <p>Problem : -</p> <p>Solusi : -</p>
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Progres :

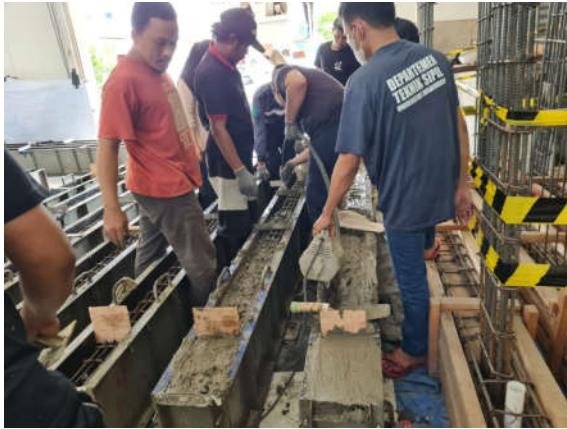
Dokumentasi :



13	31 Januari 2022	Konsultasi mengenai pemasangan Strain Gauge kepada Ibu Dr. Eng. Rita Irmawati, ST., MT	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p>  <p>The four photographs show a group of people, including a man in a blue lab coat and several women in hijabs, working in a laboratory. They are focused on preparing and installing strain gauges on metal reinforcement bars (rebar) within concrete formwork. The man in the blue lab coat is seen explaining the process to the women. The photographs capture various stages of the work, from handling the rebar to the final installation of the strain gauges.</p>			

14	1 Februari 2022	<ul style="list-style-type: none">- Pemasangan Strain Gauge- Persiapan pengecoran	Hasil: 21 tulangan terpasang Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="420 540 1033 886"></div> <div data-bbox="1058 540 1705 886"></div> <div data-bbox="420 927 1033 1271"></div> <div data-bbox="1058 927 1705 1271"></div>			

15	2 Februari 2022	<p>Melakukan pengecoran</p> <ul style="list-style-type: none">- 21 buah balok- 24 buah silinder 10 x 20 (benda uji)- 13 buah silinder 15 x 30 (benda uji)- 8 buah balok 10 x 10 x 40 (benda uji)	<p>Hasil:</p> <p>Problem :</p> <p>Solusi :</p>
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="197 675 758 1099"></div> <div data-bbox="772 675 1333 1099"></div> <div data-bbox="1348 675 1919 1099"></div>			





16	3 Februari 2022	<p>Membuka mould benda uji :</p> <ul style="list-style-type: none"> - 24 buah silinder 10 x 20 - 13 buah silinder 15 x 30 - 8 buah balok 10 x 10 x 40 <p>Melakukan moist curing</p>	<p>Hasil:</p> <p>Problem :</p> <p>Solusi :</p>
<p>Progres :</p>			

Dokumentasi :




17	12 Februari 2022	Melakukan moist curing	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="749 612 1344 1057" data-label="Image"></div>			

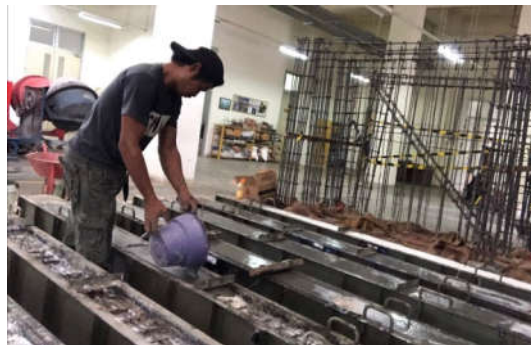
18	14 Februari 2022	Perakitan Mould Silinder ukuran 10 x 20	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="453 578 1062 1036"></div> <div data-bbox="1140 586 1738 1036"></div>			




19	15 Februari 2022	Melakukan pembukaan bekisting	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="371 591 1050 1008"></div> <div data-bbox="1129 591 1801 1008"></div>			

20	16 Februari 2022	Melakukan pemindahan sampel yang ada di Laboratorium Struktur dan Bahan	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="417 553 1075 1047"></div> <div data-bbox="1146 553 1793 1040"></div>			

21	17 Februari 2022	- Pengadaan Bahan Grouting	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="779 521 1434 1008" data-label="Image">A photograph showing a man in a brown uniform pushing a yellow pallet jack. The pallet jack is loaded with several yellow bags of grout material and a cardboard box. The man is standing on a paved area next to the back of a white truck. The truck's license plate is visible and reads 'DY 9958 GO'. The background shows an outdoor setting with trees and a building.</div>			



22	19 Februari 2022	<p>Melakukan pekerjaan grouting</p> <ul style="list-style-type: none">- Pembersihan sampel sebelum dilakukan grouting- Pengolesan Sika bonding agent (cairan sika) dengan perbandingan 1:1- Mixing Sika Grout dengan perbandingan 4L air : 25 kg	<p>Hasil:</p> <p>Problem :</p> <p>Solusi :</p>
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="422 524 993 935"></div> <div data-bbox="1146 532 1801 899"></div> <div data-bbox="751 979 1341 1312"></div>			

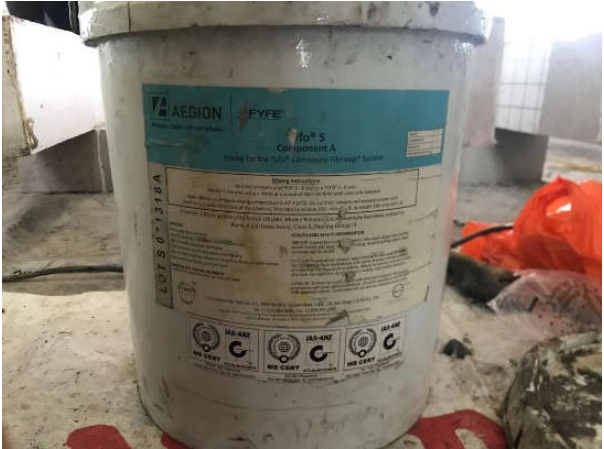


23	21 Februari 2022	Membuka mould benda uji : <ul style="list-style-type: none">- 24 buah silinder 10 x 20- 13 buah silinder 15 x 30 Melakukan moist curing	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="415 545 947 943"></div> <div data-bbox="1178 537 1713 943"></div> <div data-bbox="825 963 1297 1317"></div>			


24	3 Maret 2022	Melakukan Pengujian Kuat Tekan Silinder	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="466 545 991 922"></div> <div data-bbox="1241 537 1751 919"></div> <div data-bbox="835 935 1346 1317"></div>			



25	29 Maret 2022	Pemasangan GFRP pada balok	Hasil: Problem : Solusi :
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="499 558 976 915"></div> <div data-bbox="1131 565 1612 922"></div> <div data-bbox="810 956 1287 1312"></div>			

26	30 Maret 2022	Pemasangan GFRP pada balok	Hasil: Problem : Solusi :
Progres : Dokumentasi :  			

27	13 April 2022	Pengujian Kuat Lentur Balok Kontrol	Hasil: Problem : - Solusi : -
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="422 480 1016 878"></div> <div data-bbox="1045 483 1640 878"></div> <div data-bbox="760 909 1314 1300"></div>			

28	14 April 2022	Pengujian Kuat Lentur Balok Grouting	Hasil: Problem : - Solusi : -
Progres : Dokumentasi : 			

29	19 April 2022	Pengujian kuat lentur balok grouting dan GFRP sheet (BGRS)	Hasil: Problem : - Solusi : -
<p>Progres :</p> <p>Dokumentasi :</p> 			

30	21 April 2022	Pengujian kuat lentur balok BGRSF dan balok BGRST	Hasil: Problem : - Solusi : -
<p>Progres :</p> <p>Dokumentasi :</p> <div data-bbox="573 521 1045 873"></div> <div data-bbox="1058 521 1530 873"></div> <div data-bbox="573 951 1045 1304"></div> <div data-bbox="1058 951 1530 1304"></div>			

Lampiran 2. Perhitungan Kapasitas Momen - Balok Kontrol (BK)

1. Data Perencanaan

Kuat tekan beton	f_c	=	20.0	MPa
Kuat leleh tulangan tarik	f_y	=	280	MPa
Kuat leleh tulangan tekan	f_y	=	280.0	MPa
Kuat leleh tulangan transversal	f_y	=	280	MPa
Modulus elastisitas beton	E_c	=	21533.0	MPa
Modulus elastisitas baja	E_s	=	200000	MPa
Berat jenis beton	γ_c	=	2400	kg/m ³
Lebar penampang	b	=	150	mm
Tinggi penampang	h	=	200	mm
Tinggi efektif penampang	d	=	155.50	mm
Jarak tulangan tekan ke serat tekan terluar	d'	=	42.00	mm
Luas tulangan tarik	A_s	=	3 D 13	= 398.20 mm ²
Luas tulangan tekan	A_s'	=	2 D 8	= 100.53 mm ²
Luas tulangan sengkang	A_{vs}	=	2 D 8	= 100.53mm ²

2. Momen Retak Pertama (M_{cr})

Pada kondisi retak pertama, momen retak (M_{crack}) terjadi pada saat serattarik penampang balok mencapai modulus keruntuhan (F_r). Oleh SNI 2847.2013 pasal 9.5.2.3 diberikan persamaan sebagai berikut

$$M_{crack} = \frac{I_g \cdot f_r}{y_t}$$

Diketahui:

Hasil uji modulus keruntuhan $f_r = 0.7 \times F_c^{0.5} = 3.21$ MPa

Momen inersia penampang bruto :

$$I_g = \frac{b h^3}{12} = 112435956.7 \text{ mm}^4$$

$$y_{\text{bawah}} = h - y_{\text{atas}} = 96.05 \text{ mm}$$

$$M_{\text{crack}} = \frac{I_g f_r}{y_t} = \frac{112435956.7 \cdot 3.21}{96.05} = 3754168.576 \text{ N.mm}$$

$$\boxed{M_{\text{crack}} = 3.7542 \text{ kN.m}}$$

Nilai P_{crack} diperoleh dengan cara substitusi M_{crack} ke persamaan : $M = 0.8019 + 0.6 P$

$$3.7542 = 0.8019 + 0.6P$$

Diperoleh

$$\boxed{P_{\text{cr}} = 4.9204 \text{ kN}}$$

3. Momen Leleh (Myield)

Direncanakan menggunakan tulangan :

$$\begin{aligned} A_s &= 3 \text{ D } 13 = 398.20 \text{ mm}^2 \\ A_s' &= 2 \text{ D } 8 = 100.53 \text{ mm}^2 \end{aligned}$$

Awal tulangan leleh

$$= \frac{E_s}{E_c} = 9.3 \quad ; \quad n_f = \frac{E_f}{E_c} = 0.97$$

$$k = 0.44065$$

$$k_d = 68.521 \text{ mm}$$

Regangan tulangan tarik dari ujung atas balok

$$\varepsilon_y = \frac{f_y}{E_s} = \frac{280}{200000} \quad \boxed{\varepsilon_y = 0.0014}$$

Regangan beton bagian atas

$$\begin{aligned} \varepsilon_c &= \varepsilon_s \left(\frac{kd}{d - kd} \right) \\ &= 0.0014 \left(\frac{68.521}{155.50 - 68.52} \right) \end{aligned} \quad \boxed{\varepsilon_c = 0.001103}$$

Regangan tulangan tekan

$$\begin{aligned} \varepsilon_s' &= \varepsilon_c \left(\frac{kd - d'}{kd} \right) \\ &= 0.0011 \left(\frac{68.521 - 42.00}{68.52} \right) \end{aligned} \quad \boxed{\varepsilon_s' = 0.000427}$$

$$\begin{aligned} f_s' &= E_s \varepsilon_s' \\ &= 200000 \cdot 0.0004 \\ &= 85.376 \text{ MPa} \end{aligned}$$

bila nilai f_s' lebih kecil dari nol gunakan nol $\boxed{f_s' = 85.376 \text{ MPa}}$

Gaya tekan beton

$$\begin{aligned} C_c &= 0.5 f_c b kd \\ &= 0.5 \cdot 20 \cdot 150.00 \cdot 68.52 \end{aligned}$$

$$\boxed{C_c = 107869.30 \text{ N}}$$

Gaya tekan baja

$$\begin{aligned} C_s &= A_s' f_s' \\ &= 100.53 \cdot 85.376 \end{aligned}$$

$$\boxed{C_s = 8582.92 \text{ N}}$$

$$\begin{aligned} T &= C_c + C_s \\ &= 107869.30 + 8582.92 \end{aligned}$$

$$\boxed{T = 116452.22 \text{ N}}$$

$$T = A_s f_y$$

$$= 111495.12 \text{ N}$$

Nilai selisih T harus mendekati nol

$$C_c + C_s - A_s f_y = 0$$

$$116452.22 - 111495.12 = -4957.09718$$

$$= -4957.1$$

$$\mathbf{k = 0.44065}$$

Jarak gaya (c) dari ujung atas (y)

$$y = \frac{C_s d' + C_c \cdot 0.33 \text{ kd}}{T}$$

$$y = \frac{8582.92 \cdot 42.00 + 107869.30 \cdot 22.84}{116452.22}$$

$$y = 24.252 \text{ mm}$$

Jarak pusat total gaya tekan ke pusat tulangan tarik

$$J_d = d - y$$

$$= 155.50 - 24.252$$

$$\mathbf{J_d = 131.25 \text{ mm}}$$

Persamaan momen dan kurvatur

$$M_y = A_s f_y J_d$$

$$= 14633457.53 \text{ N.mm}$$

$$\mathbf{M_y = 14.63 \text{ kN.m}}$$

$$\mathbf{14.63 = 0.8019 + 0.6 P \text{ kN.m}}$$

$$M_y = M_{\text{maks pada tengah bentang}}$$

$$14.63 = 0.8019 + 0.6 P$$

$$13.83 = 0.6 P$$

$$\mathbf{P = 23.05 \text{ kN}}$$

4. Momen Ultimit (Mu)

$$M_u = \Phi M_n$$

$$M_u = \Phi * A_s * f_y * \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur} \quad \Phi = 0.9$$

dimana :

$$\text{Untuk } f_c \leq 20 \text{ MPa}$$

$$\beta_1 = 0.85$$

$$\text{Untuk } f_c > 20 \text{ MPa}$$

$$\beta_1 = 0.85 - \frac{0.05 (f_c - 20)}{7}$$

$$\text{Karena } f_c = 20 \text{ MPa}$$

$$\text{Maka } \beta_1 = 0.85$$

$$a_b = \frac{600 \beta_1 d}{600 + f_y} = \frac{600 \cdot 0.85 \cdot 155.50}{600 + 280.00}$$

$$\boxed{a_b = 90.119 \text{ mm}}$$

$$\rho_b = \frac{A_{s_b}}{b d} = \frac{0.85 f_c a_b}{f_y d} = \frac{0.85 \cdot 20 \cdot 90 \cdot 119}{280 \cdot 155.5}$$

$$\boxed{\rho_b = 3.69\%}$$

$$\rho_{\max} = 0.75 \quad \rho_b = 0.0277$$

$$\boxed{\rho_{\max} = 2.77\%}$$

$$\rho_{\min} = \frac{1.4}{f_y} = 0.005$$

$$\boxed{\rho_{\min} = 0.50\%}$$

$$\rho = \frac{(A_s - A_s')}{b d} = \frac{(398.2 - 100.53)}{280 \cdot 155.5}$$

$$\boxed{\rho = 1.28\%}$$

Kontrol Tulangan Tekan Sudah Leleh atau Belum

$$a = \frac{(A_s - A_s') f_y}{0.85 f_c b}$$

$$= \frac{(398.197 - 100.53096) \cdot 280}{0.85 \cdot 20.99 \cdot 150}$$

a = 31.143 mm

$$a_{\text{min Leleh}} = \frac{600 \beta_1 d'}{600 - f_y}$$

$$= \frac{600 \cdot 0.85 \cdot 42}{600 - 280}$$

a_{min leleh} = 66.938 mm

$$M_n = M_{nc} + M_{ns}$$

M_n = 15006733.09 N.mm

atau

M_n = 1.50067 t.m

Ø M_n = 12005386.47 N.mm

atau

Ø M_n = 1.20054 t.m

$$\text{Ø } M_n = M_{\text{maks}}$$

$$1.2005 = 0.0802 + 0.6 P$$

$$1.1203 = 0.6 P$$

P_{maks} = 1.86725 ton

Untuk beban 0.5 P maka :

0.5 P_{maks} = 0.93362 ton

$$M_n = M_{\text{maks}}$$

$$1.5007 = 0.0802 + 0.6 P$$

$$1.4205 = 0.6 P$$

P_{maks} = 2.36747 ton

Untuk beban 0.5 P maka :

0.5 P_{maks} = 1.18374 ton

P_u = 23.67 kN

Lampiran 3. Perhitungan Kapasitas Momen - Balok Grouting (BGR)

1. Data Perencanaan

Kuat tekan beton	f_c	=	20.0	MPa
Kuat leleh tulangan tarik	f_y	=	280	MPa
Kuat leleh tulangan tekan	f_y	=	280.0	MPa
Kuat leleh tulangan transversal	f_y	=	280	MPa
Modulus elastisitas beton	E_c	=	21532.98	MPa
Modulus elastisitas baja	E_s	=	200000	MPa
Berat jenis beton	γ_c	=	2400	kg/m ³
Lebar penampang	b	=	150	mm
Tinggi penampang	h	=	200	mm
Tinggi efektif penampang	d	=	158.00	mm
Jarak tulangan tekan ke serat tekan terluar	d'	=	42.00	mm
Luas tulangan tarik	A_s	=	3 D 13	= 150.80 mm ²
Luas tulangan tekan	A_s'	=	2 D 8	= 100.53 mm ²
Luas tulangan sengkang	A_{vs}	=	2 D 8	= 100.53mm ²

2. Momen Retak Pertama (M_{cr})

Pada kondisi retak pertama, momen retak (M_{crack}) terjadi pada saat serattarik penampang balok mencapai modulus keruntuhan (F_r). Oleh SNI 2847.2013 pasal 9.5.2.3 diberikan persamaan sebagai berikut

$$M_{crack} = \frac{I_g \cdot f_r}{y_t}$$

Diketahui:

Hasil uji modulus keruntuhan $f_r = 0.7 \times F_c^{0.5} = 3.21$ MPa

Momen inersia penampang bruto :

$$I_g = \frac{b h^3}{12}$$

$$= 106989086.3 \text{ mm}^4$$

$$y_{\text{bawah}} = h - y_{\text{atas}} = 99.25 \text{ mm}$$

$$M_{\text{crack}} = \frac{I_g f_r}{y_t}$$

$$= \frac{106989086.3 \cdot 3.21}{99.25}$$

$$= 3754168.576 \text{ N.mm}$$

$$\boxed{M_{\text{crack}} = 3.4572 \text{ kN.m}}$$

Nilai P_{crack} diperoleh dengan cara substitusi M_{crack} ke persamaan : $M = 0.8019 + 0.6 P$

$$3.4572 = 0.8019 + 0.6P$$

Diperoleh

$$\boxed{P_{\text{cr}} = 4.4255 \text{ kN}}$$

3. Momen Leleh (M_{yield})

Direncanakan menggunakan tulangan :

$$A_s = 3 \text{ D } 13 = 150.80 \text{ mm}^2$$

$$A_s' = 2 \text{ D } 8 = 100.53 \text{ mm}^2$$

Awal tulangan leleh

$$= \frac{E_s}{E_c} = 9.3 \quad ; \quad n_f = \frac{E_f}{E_c} = 0.97$$

$$k = 0.44065$$

$$k_d = 69.623 \text{ mm}$$

Regangan tulangan tarik dari ujung atas balok

$$\epsilon_y = \frac{f_y}{E_s} = \frac{280}{200000} \quad \boxed{\epsilon_y = 0.0014}$$

Regangan beton bagian atas

$$\begin{aligned} \epsilon_c &= \epsilon_s \left(\frac{kd}{d - kd} \right) \\ &= 0.0014 \left(\frac{69.62}{158.00 - 69.62} \right) \end{aligned} \quad \boxed{\epsilon_c = 0.001103}$$

Regangan tulangan tekan

$$\begin{aligned} \epsilon_s' &= \epsilon_c \left(\frac{kd - d'}{kd} \right) \\ &= 0.0011 \frac{69.62 - 42.00}{69.62} \end{aligned} \quad \boxed{\epsilon_s' = 0.000438}$$

$$\begin{aligned} f_s' &= E_s \epsilon_s' \\ &= 200000 \cdot 0.0004 \\ &= 87.515 \text{ MPa} \end{aligned}$$

bila nilai f_s' lebih kecil dari nol gunakan nol **$f_s' = 87.515 \text{ MPa}$**

Gaya tekan beton

$$\begin{aligned} C_c &= 0.5 f_c b kd \\ &= 0.5 \cdot 20 \cdot 150.00 \cdot 69.62 \end{aligned}$$

$$\boxed{C_c = 109603.54 \text{ N}}$$

Gaya tekan baja

$$\begin{aligned} C_s &= A_s' f_s' \\ &= 100.53 \cdot 87.515 \end{aligned}$$

$$\boxed{C_s = 8797.99 \text{ N}}$$

$$\begin{aligned} T &= C_c + C_s \\ &= 109603.54 + 8797.99 \end{aligned}$$

$$\boxed{T = 118401.52 \text{ N}}$$

$$T = A_s f_y$$

$$= 42223.01 \text{ N}$$

Nilai selisih T harus mendekati nol

$$C_c + C_s - A_s f_y = 0$$

$$118401.52 - 42223.01 = -76178.5165$$

$$= -766178.52$$

k	=	0.44065
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Jarak gaya (c) dari ujung atas (y)

$$y = \frac{C_s d' + C_c \cdot 0.33 \text{ kd}}{T}$$

$$y = \frac{8797.99 \cdot 42.00 + 109603.54 \cdot 23.21}{118401.52}$$

$$y = 24.604 \text{ mm}$$

Jarak pusat total gaya tekan ke pusat tulangan tarik

$$J_d = d - y$$

$$= 158.0 - 24.64$$

J_d	=	133.40	mm
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Persamaan momen dan kurvatur

$$M_y = A_s f_y J_d$$

$$= 5632381.53 \text{ N.mm}$$

$$M_y = 5.63 \text{ kN.m}$$

5.63	=	0.8019	+	0.6	P	kN.m
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$$M_y = M_{\text{maks pada tengah bentang}}$$

$$5.63 = 0.8019 + 0.6 P$$

$$4.83 = 0.6 P$$

$$P = 8.05 \text{ kN}$$

4. Momen Ultimit (Mu)

$$M_u = \Phi M_n$$

$$M_u = \Phi * A_s * f_y * \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur} \quad \Phi = 0.9$$

dimana :

$$\text{Untuk } f_c \leq 20 \text{ MPa}$$

$$\beta_1 = 0.85$$

$$\text{Untuk } f_c > 20 \text{ MPa}$$

$$\beta_1 = 0.85 - \frac{0.05 (f_c - 20)}{7}$$

$$\text{Karena } f_c = 20 \text{ MPa}$$

$$\text{Maka } \beta_1 = 0.85$$

$$a_b = \frac{600 \beta_1 d}{600 + f_y} = \frac{600 \cdot 0.85 \cdot 158.00}{600 + 280.00}$$

$$a_b = 91.568 \text{ mm}$$

$$\rho_b = \frac{A_{s_b}}{b d} = \frac{0.85 f_c a_b}{f_y d} = \frac{0.85 \cdot 20 \cdot 91.568}{280 \cdot 158.0}$$

$$\rho_b = 3.69\%$$

$$\rho_{\max} = 0.75 \rho_b = 0.0277$$

$$\rho_{\max} = 2.77\%$$

$$\rho_{\min} = \frac{1.4}{f_y} = 0.005$$

$$\rho_{\min} = 0.50\%$$

$$\rho = \frac{(A_s - A_s')}{b d} = \frac{(150.8 - 100.53)}{280 \cdot 158.0}$$

$$\rho = 0.21\%$$

Kontrol Tulangan Tekan Sudah Leleh atau Belum

$$a = \frac{(A_s - A_s') f_y}{0.85 f_c b}$$

$$= \frac{(150.796 - 100.53096) \cdot 280}{0.85 \cdot 20 \cdot 150} \quad \boxed{a = 5.259 \text{ mm}}$$

$$a_{\text{min Leleh}} = \frac{600 \beta_1 d'}{600 - f_y}$$

$$= \frac{600 \cdot 0.85 \cdot 42}{600 - 280} \quad \boxed{a_{\text{min leleh}} = 66.938 \text{ mm}}$$

$$M_n = M_{nc} + M_{ns}$$

$$\boxed{M_n = 9800917.405 \text{ N.mm}} \quad \text{atau} \quad \boxed{M_n = 0.98009 \text{ t.m}}$$

$$\boxed{\emptyset M_n = 7840733.924 \text{ N.mm}} \quad \text{atau} \quad \boxed{\emptyset M_n = 0.78407 \text{ t.m}}$$

$$\emptyset M_n = M_{\text{maks}}$$

$$0.7841 = 0.0802 + 0.6 P$$

$$0.7039 = 0.6 P \quad \boxed{P_{\text{maks}} = 1.49984 \text{ ton}}$$

$$\text{Untuk beban } 0.5 P \text{ maka : } \boxed{0.5 P_{\text{maks}} = 0.78407 \text{ ton}}$$

$$M_n = M_{\text{maks}}$$

$$0.9801 = 0.0802 + 0.6 P$$

$$0.8999 = 0.6 P \quad \boxed{P_{\text{maks}} = 1.49984 \text{ ton}}$$

$$\text{Untuk beban } 0.5 P \text{ maka : } \boxed{0.5 P_{\text{maks}} = 0.74992 \text{ ton}}$$

$$\boxed{P_u = 15 \text{ kN}}$$

**Lampiran 4. Perhitungan Kapasitas
Momen - Balok Grouting GFRP
(BGRS)**

1. Data Perencanaan

Kuat tekan beton	f_c	=	20.0	MPa
Kuat leleh tulangan tarik	f_y	=	280	MPa
Kuat leleh tulangan tekan	f_y	=	280.0	MPa
Kuat leleh tulangan transversal	f_y	=	280	MPa
Modulus elastisitas beton	E_c	=	21532.98	MPa
Modulus elastisitas baja	E_s	=	200000	MPa
Berat jenis beton	γ_c	=	2400	kg/m ³
Lebar penampang	b	=	150	mm
Tinggi penampang	h	=	200	mm
Tinggi efektif penampang	d	=	158.00	mm
Jarak tulangan tekan ke serattekan terluar	d'	=	42.00	mm
Luas tulangan tarik	A_s	=	3 D 13	= 150.80 mm ²
Luas tulangan tekan	A_s'	=	2 D 8	= 100.53 mm ²
Luas tulangan sengkang	A_{vs}	=	2 D 8	= 100.55 mm ²

2. Momen Retak Pertama (M_{cr})

Pada kondisi retak pertama, momen retak (M_{crack}) terjadi pada saat serattarik penampang balok mencapai modulus keruntuhan (F_r). Oleh SNI 2847.2013 pasal 9.5.2.3 diberikan persamaan sebagai berikut

$$M_{crack} = \frac{I_g \cdot f_r}{y_t}$$

Diketahui:

Hasil uji modulus keruntuhan $f_r = 0.7 \times F_c^{0.5} = 3.21$ MPa

Momen inersia penampang bruto :

$$I_g = \frac{b h^3}{12}$$

$$= 114268833.1 \text{ mm}^4$$

$$y_{\text{bawah}} = h - y_{\text{atas}} = 98.29 \text{ mm}$$

$$M_{\text{crack}} = \frac{I_g f_r}{y_t}$$

$$= \frac{114268833.1 \cdot 3.21}{99.25}$$

$$= 3728524.315 \text{ N.mm}$$

M_{crack}	=	3.7285	kN.m
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Nilai P_{crack} diperoleh dengan cara substitusi M_{crack} ke

persamaan : $M = 0.8019 + 0.6 P$

$$3.7285 = 0.8019 + 0.6P$$

Diperoleh

P_{cr}	=	4.877 kN
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3. Momen Leleh (Myield)

Direncanakan menggunakan tulangan :

$$A_s = 3 \quad D \quad 13 = 150.80 \text{ mm}^2$$

$$A_s' = 2 \quad D \quad 8 = 100.53 \text{ mm}^2$$

Awal tulangan leleh

$$= \frac{E_s}{E_c} = 9.3 \quad ; \quad n_f = \frac{E_f}{E_c} = 0.97$$

$$k = 0.44065$$

$$kd = 81.364 \text{ mm}$$

Regangan tulangan tarik dari ujung atas balok

$$\epsilon_y = \frac{f_y}{E_s} = \frac{280}{200000} \quad \boxed{\epsilon_y = 0.0014}$$

Regangan beton bagian atas

$$\begin{aligned} \epsilon_c &= \epsilon_s \left(\frac{kd}{d - kd} \right) \\ &= 0.0014 \left(\frac{81.36}{158.00 - 81.36} \right) \end{aligned} \quad \boxed{\epsilon_c = 0.001537}$$

Regangan tulangan tekan

$$\begin{aligned} \epsilon_{s'} &= \epsilon_c \left(\frac{kd - d'}{kd} \right) \\ &= 0.0015 \frac{81.36 - 42.00}{81.36} \end{aligned} \quad \boxed{\epsilon_{s'} = 0.002265}$$

$$\begin{aligned} f_{s'} &= E_s \epsilon_{s'} \\ &= 200000 \cdot 0.0007 \\ &= 148.67 \text{ MPa} \end{aligned}$$

bila nilai $f_{s'}$ lebih kecil dari nol gunakan nol

$$\boxed{f_{s'} = 148.67 \text{ MPa}}$$

Gaya tekan beton

$$\begin{aligned} C_c &= 0.5 f_c b kd \\ &= 0.5 \cdot 20 \cdot 150.00 \cdot 81.36 \end{aligned}$$

$$\boxed{C_c = 128087.53 \text{ N}}$$

Gaya tekan baja

$$\begin{aligned} C_s &= A_s' f_s' \\ &= 100.53 \cdot 148.67 \end{aligned}$$

$$\boxed{C_s = 14946.20 \text{ N}}$$

$$\begin{aligned} T &= C_c + C_s \\ &= 128087.53 + 8797.99 \end{aligned}$$

$$\boxed{T = 143033.72 \text{ N}}$$

$$T = A_s f_y$$

$$= 120725.72 \text{ N}$$

Nilai selisih T harus mendekati nol

$$C_c + C_s - A_s f_y = 0$$

$$143033.72 - 120725.72 = -22308.006$$

$$= -22308.01$$

$$\mathbf{k = 0.4016}$$

Jarak gaya (c) dari ujung atas (y)

$$y = \frac{C_s d' + C_c \cdot 0.33 kd}{T}$$

$$y = \frac{14946.20 \cdot 42.00 + 128087.53 \cdot 27.12}{143033.72}$$

$$y = 28.676 \text{ mm}$$

Jarak pusat total gaya tekan ke pusat tulangan tarik

$$J_d = d - y$$

$$= 158.0 - 28.676$$

$$\mathbf{J_d = 120.82 \text{ mm}}$$

Persamaan momen dan kurvatur

$$M_y = A_s f_y J_d$$

$$= 5632381.53 \text{ N.mm}$$

$$\mathbf{M_y = 15.31 \text{ kN.m}}$$

$$\mathbf{15.31 = 0.8019 + 0.6 P \text{ kN.m}}$$

$$M_y = M_{\text{maks pada tengah bentang}}$$

$$15.31 = 0.8019 + 0.6 P$$

$$14.51 = 0.6 P$$

$$\mathbf{P = 24.18 \text{ kN}}$$

4. Momen Ultimit (Mu)

$$M_u = \Phi M_n$$

$$M_u = \Phi * A_s * f_y * \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur} \quad \Phi = 0.9$$

dimana :

Material yang digunakan : **GFRP**

Lokasi balok berada di **Interior**
sehingga digunakan

$$C_E = \mathbf{0.75}$$

$$\begin{aligned} f_{fu} &= C_E \cdot f_{fu}^* \\ &= 0.75 \cdot 460 \\ &= 345 \quad \text{N/mm}^2 \\ \varepsilon_{fu} &= C_E \cdot \varepsilon_{fu}^* \\ &= 0.75 \cdot 0.02 \\ &= 0.015 \quad \text{mm/mm} \end{aligned}$$

Perhitungan pre-eliminary

$$\begin{aligned} \beta_1 &= 1.05 - 0.05 \frac{f_c'}{6.9} \\ &= 1.05 - 0.05 \frac{20.99}{6.9} \end{aligned} \quad \beta_1 = \mathbf{0.8979}$$

$$\begin{aligned} A_s &= 3 \cdot D \cdot 13 \\ &= 3 \cdot \frac{1}{4} \pi \cdot 13^2 \end{aligned} \quad A_s = \mathbf{398.1969 \text{ mm}^2}$$

$$\begin{aligned} A_s' &= 2 \cdot D \cdot 8 \\ &= 2 \cdot \frac{1}{4} \pi \cdot 8^2 \end{aligned} \quad A_s' = \mathbf{100.531 \text{ mm}^2}$$

digunakan **1** lembar GFRP tebal **1.3** mm

$$\begin{aligned} A_f &= n \cdot t_f \cdot w_f \\ &= 1 \cdot 1.3 \cdot 150 \end{aligned} \quad A_f = \mathbf{195 \text{ mm}^2}$$

Nilai regangan balok sebelum balok ditempel FRP

Beban yang bekerja pada saat FRP ditempel hanya berat

$$\text{sendiri balok } n_{\text{ekivalen tulangan ke beton}} = 9.2881$$

Untuk memperkirakan nilai c dapat digunakan

$$0 = \frac{w_f c^2}{2} + (n A_s + (n - 1)) c - 1 A_s' d' - n$$

$$0 = \frac{150}{2} c^2 + 3706.8 c - 575114 - 349$$

$$0 = 75 c^2 + 3706.8 c - 610109$$

$$\text{Maka } c = 68.80536 \text{ mm}$$

berdasarkan hasil analisa awal leleh maka :

$$k = 0.44065 \quad (\text{saat kondisi awal tulangan leleh setelah retak})$$

$c = k d$ $= 68.52108 \text{ mm}$

Menentukan nilai regangan desain untuk FRP

$$\epsilon_{fd} = 0.41 \left(\frac{f_c}{n \cdot E_f \cdot t_f} \right)^{0.5} \leq 0.9 \epsilon_{fu}$$

$$= 0.41 \left(\frac{20.99}{1 \cdot 20900 \cdot 1.3} \right)^{0.5}$$

$$= 0.011396 \leq 0.9 \cdot 0.02$$

$$0.011396 \leq 0.018$$

... debonding akan terjadi sebelum FRP putus

Gunakan

$\epsilon_{fd} = 0.011396$

Perkiraan nilai c (akan dicek kembali nantinya)

nilai c perkiraan sekitar

$$c = 0.2 \quad d$$

(nilai c selanjutnya akan dicek kembali apakah sesuai atau tidak)

$$\begin{aligned} c &= 0.2 \quad d \\ &= 0.2 \quad . \quad 155.5 \\ &= 31.1 \quad \text{mm} \end{aligned}$$

coba nilai

$$c = 60.823 \quad \text{mm}$$

Menghitung tegangan yang terjadi pada tulangan dan FRP

$$\begin{aligned} f_s &= E_s \quad \epsilon_s \leq f_y \\ &= 200000 \quad . \quad 0.00467 \\ &= 933.9557102 \quad \text{N/mm}^2 \end{aligned}$$

$$f_s = 933.9557 > 280$$

$$f_s' = 185.6839882 < 280$$

gunakan

$$f_s = 280 \quad \text{N/mm}^2$$

$$f_s' = 185.6839882 \quad \text{N/mm}^2$$

$$\begin{aligned} f_{fe} &= E_f \quad \epsilon_{fe} \\ &= 20900 \quad . \quad 0.006863 \\ &= 143.4342048 \quad \text{N/mm}^2 \end{aligned}$$

$$\varepsilon'_c = \frac{1.7 f_c}{E_c}$$

$$\begin{aligned} \varepsilon'_c &= \frac{1.7 \cdot 20.99}{21532.97704} \\ &= 0.001657 \end{aligned}$$

Mengecek kesesuaian nilai c

$$\begin{aligned} \beta_1 &= \frac{4 \varepsilon'_c - \varepsilon_c}{6 \varepsilon'_c - 2 \varepsilon_c} \\ &= \frac{4 \cdot 0.001657 - 0.003}{6 \cdot 0.001657 - 2 \cdot 0.003} \end{aligned}$$

$$\beta_1 = 0.920294$$

$$\begin{aligned} \alpha_1 &= \frac{3 \varepsilon'_c \varepsilon_c - \varepsilon_c^2}{3 \beta_1 \varepsilon'^2 c} \\ &= 0.780069 \end{aligned}$$

$$\begin{aligned} \alpha_1 &= \frac{A_s f_s + A_f f_{fe} - A_s' f_s'}{\alpha_1 f_c \beta_1 W_f} \\ &= 53.44358 \text{ mm} \end{aligned}$$

Kontribusi tulangan terhadap kuat lentur

$$\begin{aligned} M_{ns} &= A_s f_s \frac{d - \beta_1 c}{2} \\ &= 14217013.2 \text{ N.mm} \end{aligned}$$

$$\begin{aligned}
 M_{ns} &= A_s (d - d') \\
 &= 101 \cdot 185.68 (156 - 42)
 \end{aligned}$$

$$\boxed{M_{ns}' = 2118703.42 \text{ N.mm}} = 0.2119 \text{ t.m}$$

Kontribusi FRP terhadap kuat lentur

$$\begin{aligned}
 M_{nf} &= A_f f_{fc} \frac{d_f - \beta_1 c}{2} \\
 &= 14217013.2 \text{ N.mm}
 \end{aligned}$$

$$\boxed{M_{nf} = 4811130.67 \text{ N.mm}} = 0.4811 \text{ t.m}$$

Kuat lentur nominal gabungan

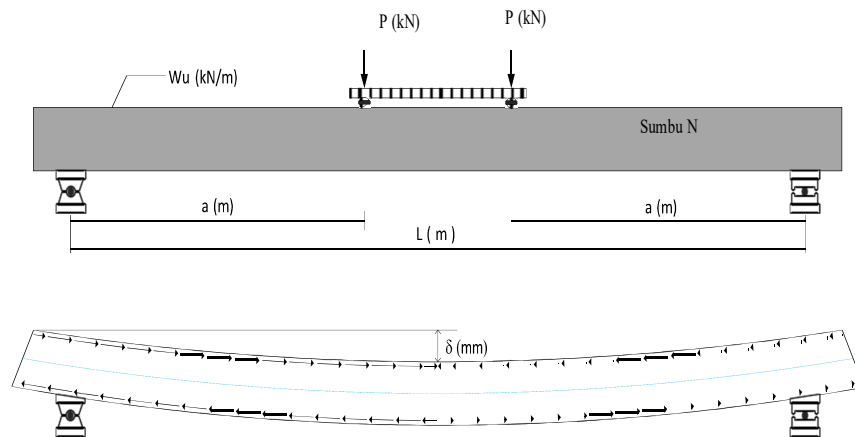
$$\begin{aligned}
 \phi M_n &= [M_{ns} + M_{ns}' + \psi_f M_{nf}] \\
 &= 1 [1.4217 + 0.2119 + 1 \cdot 0.4811131] \\
 &= 2.11 \text{ t.m}
 \end{aligned}$$

$$\begin{aligned}
 M_n &= 0.0802 + 0.6 P \\
 2.11468 &= 0.0802 + 0.6 P \\
 2.03449 &= 0.6 P \\
 P_u &= 33.91 \text{ kN}
 \end{aligned}$$

Untuk Perhitungan lendutan secara teoritis dilakukan yaitu :

Dimana :

$$\begin{aligned}
 E_c &= 21533 \text{ Mpa} = 21.5 \text{ kN/mm}^2 \\
 A &= 1200 \text{ mm} \\
 L &= 3000 \text{ mm} \\
 Q &= 0.9 = 0.0009 \text{ kN/mm}
 \end{aligned}$$



Untuk I_{cr}

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_{cr}} \times (3 \cdot L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_{cr}} \\ &= 0.042 \times \frac{1200P}{1970391430} \times 21240000 + 0.013 \times \frac{72900000000}{2026216698} \\ &= 0.538979202 \quad P + 0.468468526 \end{aligned}$$

Untuk I_g

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_g} \times (3 \cdot L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_g} \\ &= 0.0416667 \times \frac{1200P}{2153300000} \times 21240000 + 0.013 \times \frac{72900000000}{2153300000} \\ &= 0.493196489 \quad P + 0.440820485 \end{aligned}$$