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# LAMPIRAN

**Lampiran 1. Syntax ARL Bagan Kendali MEWMA**

```

Title 'Bagan Kendali\MEWMA2000';
proc iml;
create control var {count};
do i= 1 to 10000;
Flag = 0; /*Flag to stop iterations*/
count=0; /*Count variable to measure ARL*/
D=0; /*Value holder for calculated values*/
var=2; /*number of variables in simulation*/
do while (Flag=0);
m={0, 3};
l={1 1.44,1.44 2};
s={1 .9, .9 1};
lamda=.8;
/*Begin observation generation*/
seed = 0;
n = 1;
sigma =l#s;
p = nrow(sigma);
b = repeat(m`,n,1);
q = root(sigma);
z =normal(repeat(seed,n,p));
y =z*q + b;
out=y;
j=count+1;
k=2*j;
/*Calculation of test statistic*/
beta= 1-lamda;
gam= (1-lamda)**k;
del = ((lamda * (1-gam))/(2-lamda));
sig = del * sigma;
siginv = inv(sig);

```

```
h = 10.17; /*MEWMA critical value*/
B=lamda * y;
C = beta * Z;
Z= C + B;
Ti2 = Z * siginv * Z`;
count = count + 1;
flag = (Ti2 > h);
if count > 9999 then flag = 1;
end;
append var {count};
end;
quit;
proc means data = control MEAN; /*Calculation of ARL*/
var count; output out = stats;
run;
```

**Lampiran 2. Syntax ARL Bagan Kendali MCUSUM**

```

Title 'Bagan Kendali MCUSUM2000';
proc iml;
create control var {count};
do i= 1 to 10000;
Flag = 0; /*Flag to stop iterations*/
count=0; /*Count variable to measure ARL*/
D=0; /*Value holder for calculated values*/
var=2; /*number of variables in simulation*/
do while (Flag=0);
m={0, 3}; /*Mean or observation vector*/
l={1 1.44, 1.44 2}; /*Covariance matrix*/
s={1 .9, .9 1}; /*Correlation values*/
/*Begin observation generation*/
seed = 0;
n = 1;
sigma =l#s;
p = nrow(sigma);
b = repeat(m`,n,1);
q = root(sigma);
z =normal(repeat(seed,n,p));
y =z*q + b;
out=y;
j=count+1;
k=2*j;
fir={0, 0}; /*Fast initial response values (not used in simulation)*/
R=D+(y)-fir`;
if R > 0 then D=R;
else D=0;
MCt = R;
h = 12.20; /*Critical value for test*/
count = count + 1;

```

```
flag = (MCt > h);  
if count > 9999 then flag = 1;  
end;  
append var {count};  
end;  
quit;  
proc means data = control MEAN; /*Calculation of ARL*/  
var count; output out = stats;  
run;
```

**Lampiran 3.** Perbandingan jarak mahalanobis dengan nilai chi-kuadrat

| No. | $d_i^2$ | $\chi_{\alpha,2}^2$ | No. | $d_i^2$ | $\chi_{\alpha,2}^2$ | No. | $d_i^2$ | $\chi_{\alpha,2}^2$ |
|-----|---------|---------------------|-----|---------|---------------------|-----|---------|---------------------|
| 1   | 0,00882 | 0,00355             | 38  | 0,34888 | 0,28538             | 75  | 0,74805 | 0,61355             |
| 2   | 0,00983 | 0,01067             | 39  | 0,35428 | 0,29358             | 76  | 0,75494 | 0,62321             |
| 3   | 0,00983 | 0,01781             | 40  | 0,37326 | 0,30181             | 77  | 0,75955 | 0,63292             |
| 4   | 0,02601 | 0,02498             | 41  | 0,38862 | 0,31008             | 78  | 0,76524 | 0,64268             |
| 5   | 0,04558 | 0,03217             | 42  | 0,39635 | 0,31837             | 79  | 0,76857 | 0,65248             |
| 6   | 0,05292 | 0,03939             | 43  | 0,39635 | 0,32671             | 80  | 0,77684 | 0,66233             |
| 7   | 0,05714 | 0,04664             | 44  | 0,40079 | 0,33508             | 81  | 0,78942 | 0,67224             |
| 8   | 0,07646 | 0,05391             | 45  | 0,40553 | 0,34348             | 82  | 0,79138 | 0,68219             |
| 9   | 0,07646 | 0,06121             | 46  | 0,40553 | 0,35192             | 83  | 0,80223 | 0,69219             |
| 10  | 0,07772 | 0,06854             | 47  | 0,44396 | 0,36039             | 84  | 0,82372 | 0,70224             |
| 11  | 0,08215 | 0,07589             | 48  | 0,45659 | 0,36890             | 85  | 0,83067 | 0,71234             |
| 12  | 0,08585 | 0,08327             | 49  | 0,46925 | 0,37745             | 86  | 0,83563 | 0,72249             |
| 13  | 0,14648 | 0,09068             | 50  | 0,47600 | 0,38603             | 87  | 0,85098 | 0,73269             |
| 14  | 0,14995 | 0,09811             | 51  | 0,48107 | 0,39465             | 88  | 0,85722 | 0,74295             |
| 15  | 0,15184 | 0,10558             | 52  | 0,48622 | 0,40331             | 89  | 0,86165 | 0,75326             |
| 16  | 0,16062 | 0,11307             | 53  | 0,49830 | 0,41201             | 90  | 0,86286 | 0,76362             |
| 17  | 0,16391 | 0,12058             | 54  | 0,52771 | 0,42074             | 91  | 0,86711 | 0,77404             |
| 18  | 0,16507 | 0,12813             | 55  | 0,53952 | 0,42951             | 92  | 0,90915 | 0,78451             |
| 19  | 0,16692 | 0,13571             | 56  | 0,54191 | 0,43832             | 93  | 0,92268 | 0,79504             |
| 20  | 0,17809 | 0,14331             | 57  | 0,55019 | 0,44717             | 94  | 0,92561 | 0,80562             |
| 21  | 0,17809 | 0,15095             | 58  | 0,55154 | 0,45606             | 95  | 0,92990 | 0,81626             |
| 22  | 0,18419 | 0,15861             | 59  | 0,57083 | 0,46499             | 96  | 0,93077 | 0,82695             |
| 23  | 0,18615 | 0,16630             | 60  | 0,57758 | 0,47396             | 97  | 0,93222 | 0,83770             |
| 24  | 0,20329 | 0,17402             | 61  | 0,57790 | 0,48297             | 98  | 0,93491 | 0,84852             |
| 25  | 0,21343 | 0,18177             | 62  | 0,58344 | 0,49202             | 99  | 0,94955 | 0,85938             |
| 26  | 0,21403 | 0,18956             | 63  | 0,58857 | 0,50111             | 100 | 0,95251 | 0,87031             |
| 27  | 0,21801 | 0,19737             | 64  | 0,59607 | 0,51024             | 101 | 0,95755 | 0,88130             |
| 28  | 0,24960 | 0,20521             | 65  | 0,59859 | 0,51942             | 102 | 0,97395 | 0,89235             |
| 29  | 0,26673 | 0,21309             | 66  | 0,62422 | 0,52863             | 103 | 0,99384 | 0,90346             |
| 30  | 0,27086 | 0,22099             | 67  | 0,64999 | 0,53789             | 104 | 0,99404 | 0,91464             |
| 31  | 0,27587 | 0,22893             | 68  | 0,67471 | 0,54719             | 105 | 1,01006 | 0,92587             |
| 32  | 0,29464 | 0,23690             | 69  | 0,67471 | 0,55654             | 106 | 1,01795 | 0,93717             |
| 33  | 0,30020 | 0,24490             | 70  | 0,67797 | 0,56593             | 107 | 1,01998 | 0,94854             |
| 34  | 0,30020 | 0,25293             | 71  | 0,69870 | 0,57536             | 108 | 1,02256 | 0,95996             |
| 35  | 0,30890 | 0,26099             | 72  | 0,70293 | 0,58484             | 109 | 1,02256 | 0,97146             |
| 36  | 0,31760 | 0,26909             | 73  | 0,71691 | 0,59437             | 110 | 1,03171 | 0,98302             |
| 37  | 0,32366 | 0,27722             | 74  | 0,71901 | 0,60394             | 111 | 1,03171 | 0,99465             |

**Lanjutan Lampiran 3.**

| No. | $d_i^2$ | $\chi_{\alpha,2}^2$ | No. | $d_i^2$ | $\chi_{\alpha,2}^2$ | No. | $d_i^2$ | $\chi_{\alpha,2}^2$ |
|-----|---------|---------------------|-----|---------|---------------------|-----|---------|---------------------|
| 112 | 1,04545 | 1,00634             | 149 | 0,74805 | 0,61355             | 186 | 1,04545 | 1,00634             |
| 113 | 1,06086 | 1,01811             | 150 | 0,75494 | 0,62321             | 187 | 1,06086 | 1,01811             |
| 114 | 1,06086 | 1,02994             | 151 | 0,75955 | 0,63292             | 188 | 1,06086 | 1,02994             |
| 115 | 1,06734 | 1,04185             | 152 | 0,76524 | 0,64268             | 189 | 1,06734 | 1,04185             |
| 116 | 1,06734 | 1,05382             | 153 | 0,76857 | 0,65248             | 190 | 1,06734 | 1,05382             |
| 117 | 1,06834 | 1,06587             | 154 | 0,77684 | 0,66233             | 191 | 1,06834 | 1,06587             |
| 118 | 1,07967 | 1,07799             | 155 | 0,78942 | 0,67224             | 192 | 1,07967 | 1,07799             |
| 119 | 1,08100 | 1,09019             | 156 | 0,79138 | 0,68219             | 193 | 1,08100 | 1,09019             |
| 120 | 1,09610 | 1,10246             | 157 | 0,80223 | 0,69219             | 194 | 1,09610 | 1,10246             |
| 121 | 1,10235 | 1,11480             | 158 | 0,82372 | 0,70224             | 195 | 1,10235 | 1,11480             |
| 122 | 1,10319 | 1,12723             | 159 | 0,83067 | 0,71234             | 196 | 1,10319 | 1,12723             |
| 123 | 1,11317 | 1,13973             | 160 | 0,83563 | 0,72249             | 197 | 1,11317 | 1,13973             |
| 124 | 1,13359 | 1,15230             | 161 | 0,85098 | 0,73269             | 198 | 1,13359 | 1,15230             |
| 125 | 1,13807 | 1,16496             | 162 | 0,85722 | 0,74295             | 199 | 1,13807 | 1,16496             |
| 126 | 1,14480 | 1,17770             | 163 | 0,86165 | 0,75326             | 200 | 1,14480 | 1,17770             |
| 127 | 1,14665 | 1,19052             | 164 | 0,86286 | 0,76362             | 201 | 1,14665 | 1,19052             |
| 128 | 1,15100 | 1,20343             | 165 | 0,86711 | 0,77404             | 202 | 1,15100 | 1,20343             |
| 129 | 1,17662 | 1,21641             | 166 | 0,90915 | 0,78451             | 203 | 1,17662 | 1,21641             |
| 130 | 1,19668 | 1,22948             | 167 | 0,92268 | 0,79504             | 204 | 1,19668 | 1,22948             |
| 131 | 1,24356 | 1,24264             | 168 | 0,92561 | 0,80562             | 205 | 1,24356 | 1,24264             |
| 132 | 1,24905 | 1,25589             | 169 | 0,92990 | 0,81626             | 206 | 1,24905 | 1,25589             |
| 133 | 1,26171 | 1,26922             | 170 | 0,93077 | 0,82695             | 207 | 1,26171 | 1,26922             |
| 134 | 1,26218 | 1,28264             | 171 | 0,93222 | 0,83770             | 208 | 1,26218 | 1,28264             |
| 135 | 1,26345 | 1,29616             | 172 | 0,93491 | 0,84852             | 209 | 1,26345 | 1,29616             |
| 136 | 1,26747 | 1,30976             | 173 | 0,94955 | 0,85938             | 210 | 1,26747 | 1,30976             |
| 137 | 1,27710 | 1,32346             | 174 | 0,95251 | 0,87031             | 211 | 1,27710 | 1,32346             |
| 138 | 1,28055 | 1,33726             | 175 | 0,95755 | 0,88130             | 212 | 1,28055 | 1,33726             |
| 139 | 1,28455 | 1,35114             | 176 | 0,97395 | 0,89235             | 213 | 1,28455 | 1,35114             |
| 140 | 1,28924 | 1,36513             | 177 | 0,99384 | 0,90346             | 214 | 1,28924 | 1,36513             |
| 141 | 1,28924 | 1,37921             | 178 | 0,99404 | 0,91464             | 215 | 1,28924 | 1,37921             |
| 142 | 1,30842 | 1,39340             | 179 | 1,01006 | 0,92587             | 216 | 1,30842 | 1,39340             |
| 143 | 1,31413 | 1,40768             | 180 | 1,01795 | 0,93717             | 217 | 1,31413 | 1,40768             |
| 144 | 1,32425 | 1,42207             | 181 | 1,01998 | 0,94854             | 218 | 1,32425 | 1,42207             |
| 145 | 1,33402 | 1,43657             | 182 | 1,02256 | 0,95996             | 219 | 1,33402 | 1,43657             |
| 146 | 1,33976 | 1,45116             | 183 | 1,02256 | 0,97146             | 220 | 1,33976 | 1,45116             |
| 147 | 1,36830 | 1,46587             | 184 | 1,03171 | 0,98302             | 221 | 1,36830 | 1,46587             |
| 148 | 1,37541 | 1,48069             | 185 | 1,03171 | 0,99465             | 222 | 1,37541 | 1,48069             |

**Lanjutan Lampiran 3.**

| No. | $d_i^2$ | $\chi_{\alpha,2}^2$ | No. | $d_i^2$  | $\chi_{\alpha,2}^2$ |
|-----|---------|---------------------|-----|----------|---------------------|
| 223 | 2,76545 | 3,11186             | 253 | 3,52044  | 4,51503             |
| 224 | 2,79679 | 3,14576             | 254 | 3,54670  | 4,58401             |
| 225 | 2,80754 | 3,18024             | 255 | 3,60733  | 4,65544             |
| 226 | 2,81483 | 3,21533             | 256 | 3,79996  | 4,72952             |
| 227 | 2,81579 | 3,25105             | 257 | 3,96533  | 4,80646             |
| 228 | 2,83220 | 3,28741             | 258 | 4,05175  | 4,88647             |
| 229 | 2,84706 | 3,32445             | 259 | 4,25577  | 4,96981             |
| 230 | 2,84941 | 3,36219             | 260 | 4,52979  | 5,05678             |
| 231 | 2,85229 | 3,40065             | 261 | 4,65048  | 5,14771             |
| 232 | 2,85700 | 3,43987             | 262 | 4,65668  | 5,24296             |
| 233 | 2,85722 | 3,47987             | 263 | 4,76884  | 5,34299             |
| 234 | 2,88123 | 3,52069             | 264 | 4,79643  | 5,44827             |
| 235 | 2,89289 | 3,56235             | 265 | 4,82453  | 5,55941             |
| 236 | 2,89845 | 3,60491             | 266 | 5,50305  | 5,67709             |
| 237 | 2,91011 | 3,64839             | 267 | 5,62989  | 5,80213             |
| 238 | 2,96454 | 3,69284             | 268 | 5,69322  | 5,93552             |
| 239 | 3,03058 | 3,73829             | 269 | 6,22542  | 6,07843             |
| 240 | 3,04491 | 3,78481             | 270 | 6,33453  | 6,23236             |
| 241 | 3,05325 | 3,83243             | 271 | 6,68987  | 6,39912             |
| 242 | 3,07269 | 3,88121             | 272 | 7,39105  | 6,58106             |
| 243 | 3,07910 | 3,93121             | 273 | 7,46669  | 6,78123             |
| 244 | 3,14357 | 3,98250             | 274 | 7,73393  | 7,00368             |
| 245 | 3,14969 | 4,03513             | 275 | 8,26361  | 7,25401             |
| 246 | 3,16585 | 4,08919             | 276 | 9,43389  | 7,54021             |
| 247 | 3,19794 | 4,14475             | 277 | 10,23150 | 7,87432             |
| 248 | 3,20926 | 4,20190             | 278 | 11,03456 | 8,27566             |
| 249 | 3,22114 | 4,26072             | 279 | 13,54276 | 8,77829             |
| 250 | 3,34263 | 4,32133             | 280 | 16,59996 | 9,45123             |
| 251 | 3,42964 | 4,38384             | 281 | 17,90211 | 10,47288            |
| 252 | 3,49086 | 4,44836             | 282 | 20,99174 | 12,67011            |

**Lampiran 4.** Data PDAM Tirta Je'ne'berang Kabupaten Gowa Tahun 2020 Fase I

| Hari Ke- | Kekeruhan | Klor Bebas | Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|----------|-----------|------------|
| 1        | 3,37      | 0,48       | 38       | 4,44      | 0,44       |
| 2        | 4,20      | 0,56       | 39       | 4,81      | 0,41       |
| 3        | 4,10      | 0,75       | 40       | 4,52      | 1,50       |
| 4        | 5,25      | 0,19       | 41       | 3,95      | 0,20       |
| 5        | 4,10      | 1,33       | 42       | 3,21      | 1,97       |
| 6        | 3,52      | 1,26       | 43       | 4,13      | 0,46       |
| 7        | 4,20      | 0,75       | 44       | 3,33      | 0,22       |
| 8        | 3,91      | 1,00       | 45       | 5,95      | 0,32       |
| 9        | 4,59      | 0,27       | 46       | 4,76      | 1,07       |
| 10       | 4,87      | 0,84       | 47       | 4,12      | 1,79       |
| 11       | 3,60      | 1,12       | 48       | 4,27      | 1,35       |
| 12       | 4,80      | 0,22       | 49       | 3,50      | 0,70       |
| 13       | 3,07      | 0,23       | 50       | 3,05      | 0,10       |
| 14       | 3,78      | 0,90       | 51       | 5,42      | 1,19       |
| 15       | 4,98      | 0,40       | 52       | 4,70      | 0,82       |
| 16       | 3,99      | 1,07       | 53       | 5,16      | 1,19       |
| 17       | 4,11      | 0,43       | 54       | 4,94      | 0,10       |
| 18       | 5,59      | 0,52       | 55       | 3,06      | 0,25       |
| 19       | 4,11      | 0,46       | 56       | 4,16      | 0,30       |
| 20       | 4,09      | 0,45       | 57       | 5,06      | 0,54       |
| 21       | 6,15      | 0,50       | 58       | 5,94      | 2,79       |
| 22       | 4,63      | 0,24       | 59       | 5,50      | 1,45       |
| 23       | 4,93      | 0,59       | 60       | 8,12      | 2,60       |
| 24       | 6,88      | 1,69       | 61       | 7,23      | 0,42       |
| 25       | 6,96      | 0,94       | 62       | 5,13      | 0,86       |
| 26       | 2,50      | 0,11       | 63       | 4,69      | 0,66       |
| 27       | 3,71      | 0,11       | 64       | 4,54      | 0,54       |
| 28       | 3,45      | 0,11       | 65       | 4,26      | 0,18       |
| 29       | 4,79      | 2,30       | 66       | 3,48      | 0,12       |
| 30       | 4,68      | 0,55       | 67       | 4,48      | 0,53       |
| 31       | 4,46      | 0,49       | 68       | 3,33      | 0,86       |
| 32       | 2,14      | 0,71       | 69       | 4,23      | 0,66       |
| 33       | 3,71      | 1,39       | 70       | 2,97      | 0,21       |
| 34       | 5,14      | 0,30       | 71       | 5,08      | 0,27       |
| 35       | 3,17      | 0,14       | 72       | 4,24      | 0,40       |
| 36       | 4,55      | 1,54       | 72       | 4,24      | 0,40       |
| 37       | 4,16      | 1,58       | 73       | 2,39      | 0,95       |

| Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|
| 74       | 4,20      | 1,88       |
| 75       | 3,99      | 1,12       |
| 76       | 4,52      | 0,41       |
| 77       | 4,95      | 1,51       |
| 78       | 3,90      | 1,17       |
| 79       | 4,08      | 0,40       |
| 80       | 4,96      | 0,14       |
| 81       | 4,18      | 0,85       |
| 82       | 3,62      | 0,91       |
| 83       | 3,43      | 0,11       |
| 84       | 2,01      | 0,11       |
| 85       | 3,34      | 1,14       |
| 86       | 3,51      | 0,97       |
| 87       | 3,10      | 2,42       |
| 88       | 4,15      | 0,38       |
| 89       | 4,06      | 0,17       |
| 90       | 4,11      | 0,68       |
| 91       | 1,27      | 0,18       |
| 92       | 2,95      | 0,40       |
| 93       | 3,80      | 0,46       |
| 94       | 1,41      | 0,34       |
| 95       | 5,15      | 0,54       |
| 96       | 3,96      | 0,71       |
| 97       | 6,41      | 0,11       |
| 98       | 4,33      | 0,38       |
| 99       | 3,51      | 0,24       |
| 100      | 4,19      | 1,70       |
| 101      | 6,19      | 0,98       |
| 102      | 6,62      | 1,68       |
| 103      | 4,89      | 1,15       |
| 104      | 4,06      | 0,52       |
| 105      | 5,53      | 0,68       |
| 106      | 4,23      | 1,22       |
| 107      | 3,81      | 1,32       |
| 108      | 4,68      | 0,97       |
| 109      | 3,79      | 0,22       |
| 110      | 5,15      | 1,91       |

| Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|
| 111      | 4,91      | 0,96       |
| 112      | 4,29      | 1,10       |
| 113      | 4,38      | 1,51       |
| 114      | 3,87      | 0,81       |
| 115      | 4,08      | 0,39       |
| 116      | 4,97      | 1,17       |
| 117      | 5,76      | 1,02       |
| 118      | 6,41      | 0,47       |
| 119      | 5,51      | 0,57       |
| 120      | 5,50      | 0,46       |
| 121      | 5,85      | 0,47       |
| 122      | 5,90      | 0,31       |
| 123      | 5,26      | 1,91       |
| 124      | 4,50      | 0,43       |
| 125      | 3,10      | 0,62       |
| 126      | 4,28      | 0,52       |
| 127      | 4,64      | 1,47       |
| 128      | 5,15      | 1,00       |
| 129      | 5,78      | 0,95       |
| 130      | 3,82      | 0,78       |
| 131      | 3,79      | 0,67       |
| 132      | 3,85      | 0,46       |
| 133      | 4,25      | 0,88       |
| 134      | 3,50      | 0,48       |
| 135      | 4,00      | 0,35       |
| 136      | 3,52      | 1,82       |
| 137      | 3,03      | 0,43       |
| 138      | 2,62      | 0,91       |
| 139      | 3,64      | 1,14       |
| 140      | 2,84      | 0,37       |
| 141      | 2,74      | 0,41       |
| 142      | 3,69      | 1,48       |
| 143      | 2,44      | 1,51       |
| 144      | 2,39      | 1,37       |
| 145      | 2,67      | 0,69       |
| 146      | 2,29      | 0,50       |
| 147      | 3,13      | 0,52       |

**Lampiran 5.** *Syntax* MATLAB untuk Bagan Kendali MEWMA

```

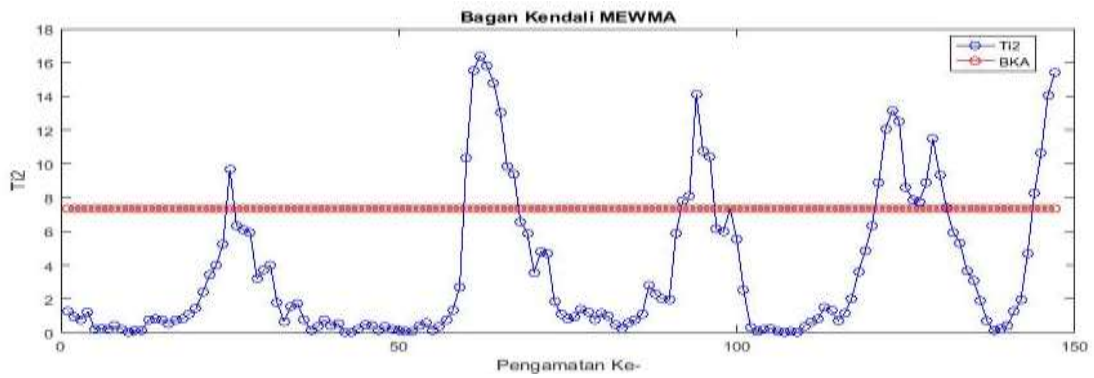
clc;
clear;
X = xlread('AnalisisData1.xlsx');
lamda=0.8;
H =10.58;
S=cov(X);
[brsX,klmX]=size(X);
t=brsX;
w=klmX;
rata=mean(X);
for i=1:t
    for j=1:2
        X(i,j)=X(i,j)-rata(j);
    end
end
v=zeros((t-1),w);
for i=1:t
    xt=X(i,:)-rata;
end
xi=X;
v=zeros((t-1),w);
for i=1:(t-1)
    v(i,:)=xi(i+1,:)-X(i,:);
end
S=(1/2)*(v'*v)/(t-1)
for p=1:3
    Z(1,p)=r*X(1,p);
end
for i=2:t
    for p=1:3
        Z(i,p)=r*X(i,p)+(1-r)*Z(i-1,p);
    end
end
for i=1:t
    Szi=(r*(1-(1-r)^(2*i))/(2-r))*S;
    iS=inv(Szi);
    Z1=Z(i,:);
    T2(i)=Z1*iS*Z1';
End
keluar=0;
d=0;

for i=1:t
    if T2(i)>H
        keluar=keluar+1;
        d=d+1;
        ygkeluar(d)=i;
    end
end

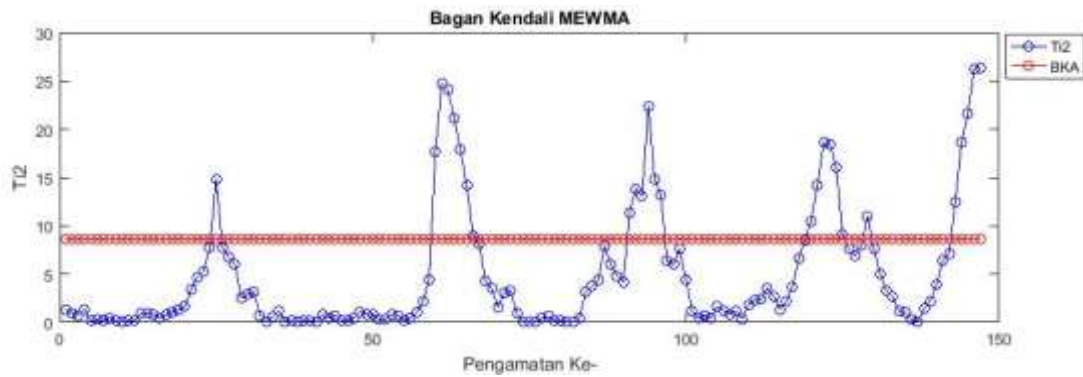
```

```
    end
end
for i=1:t
    batas(i)=H;
    x(i)=I;
end
jumlah_keluar=keluar;
A=max(T2);
plot(X);
title('Bagan Kendali MEWMA');
xlabel('Pengamatan Ke-');
ylabel('Ti2');
```

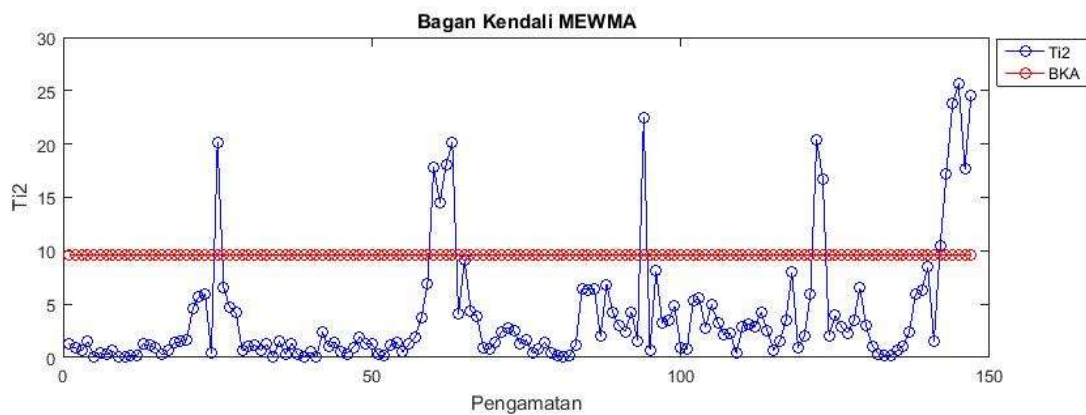
**Lampiran 6.** Output Bagan Kendali MEWMA untuk Masing -masing Pembobot  
 Pembobot  $\lambda=0,05$



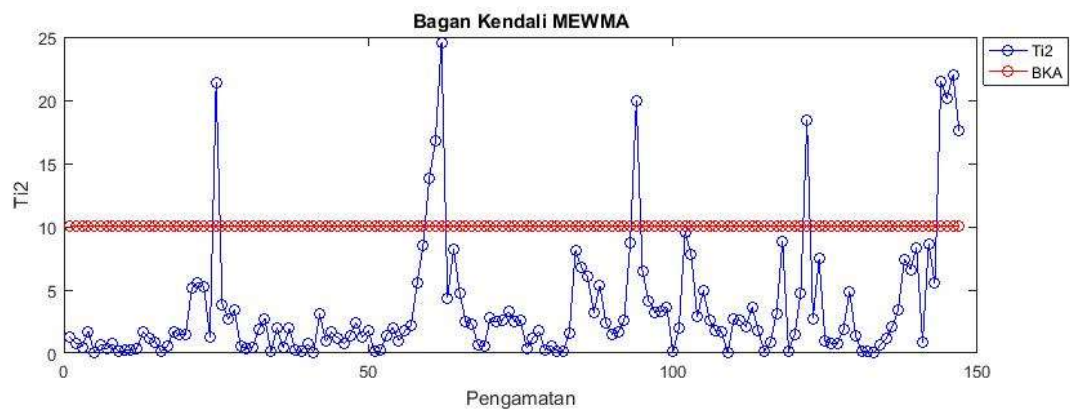
Pembobot  $\lambda=0,1$



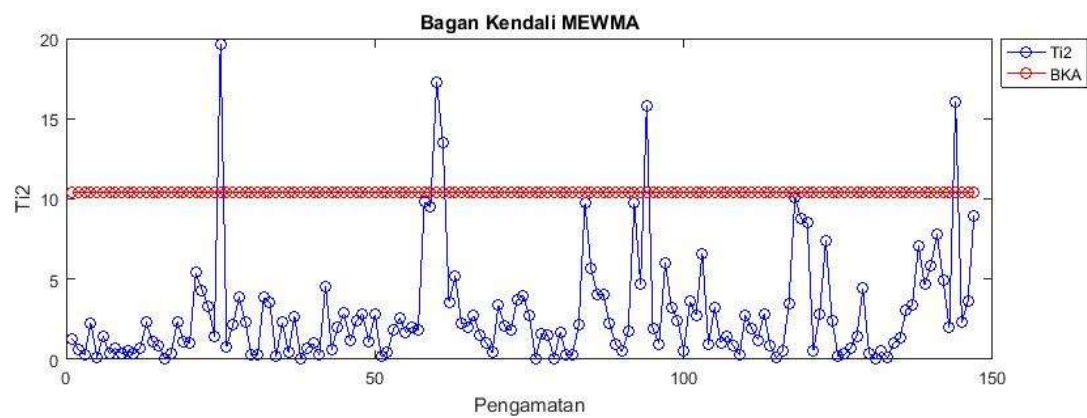
Pembobot  $\lambda=0,2$



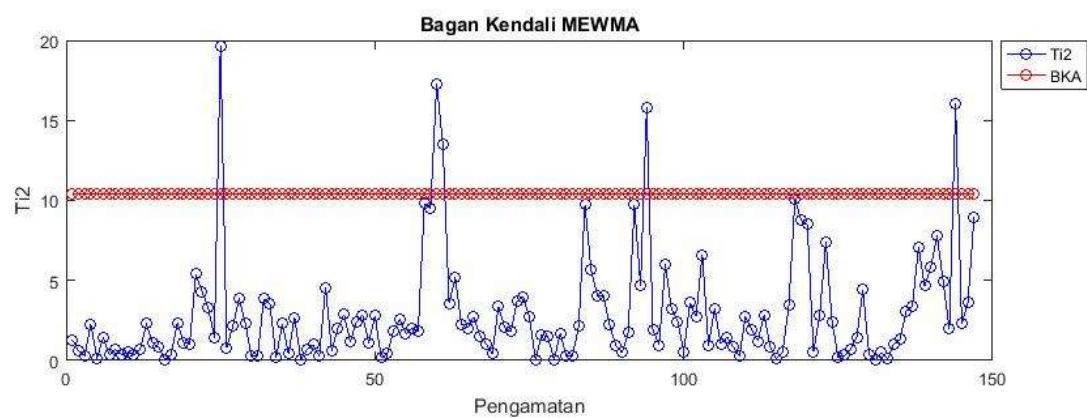
Pembobot  $\lambda=0,3$



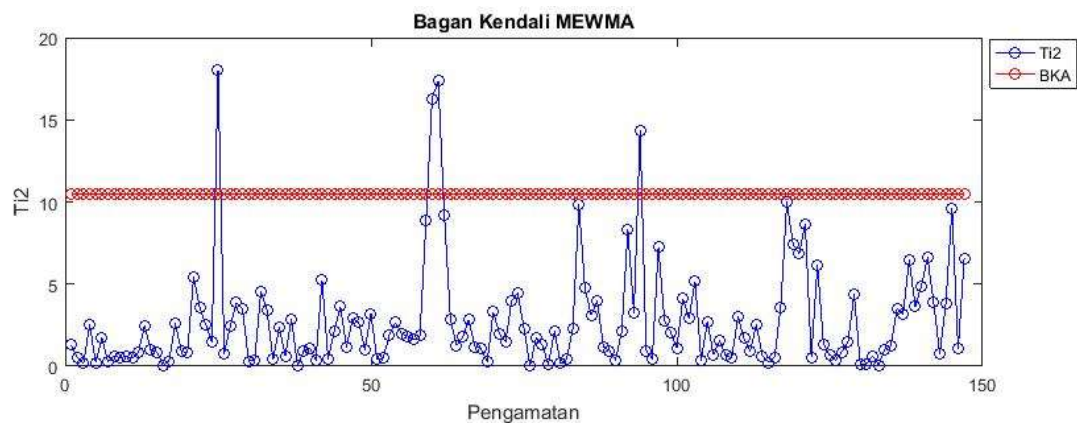
Pembobot  $\lambda=0,4$



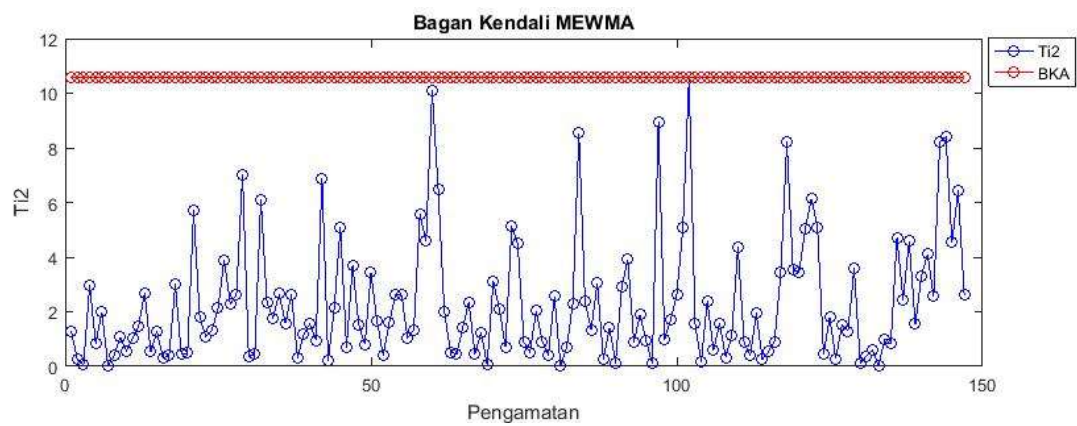
Pembobot  $\lambda=0,5$



Pembobot  $\lambda=0,6$



Pembobot  $\lambda=0,8$



**Lampiran 7. Data PDAM Tirta Je'ne'berang Kabupaten Gowa Tahun 2020 Fase II**

| Hari Ke- | Kekeruhan | Klor Bebas | Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|----------|-----------|------------|
| 1        | 3,60      | 0,99       | 38       | 2,80      | 0,24       |
| 2        | 2,26      | 0,92       | 39       | 2,17      | 0,40       |
| 3        | 2,65      | 0,40       | 40       | 1,85      | 0,15       |
| 4        | 3,75      | 0,82       | 41       | 2,13      | 0,38       |
| 5        | 2,93      | 0,52       | 42       | 1,54      | 0,22       |
| 6        | 2,29      | 0,49       | 43       | 1,76      | 0,21       |
| 7        | 2,40      | 0,18       | 44       | 1,61      | 0,20       |
| 8        | 3,19      | 0,16       | 45       | 1,57      | 1,23       |
| 9        | 3,15      | 0,17       | 46       | 1,58      | 0,44       |
| 10       | 3,17      | 1,17       | 47       | 2,16      | 0,18       |
| 11       | 3,72      | 0,71       | 48       | 1,39      | 0,18       |
| 12       | 3,93      | 0,88       | 49       | 1,50      | 0,20       |
| 13       | 3,38      | 0,36       | 50       | 1,36      | 0,15       |
| 14       | 3,60      | 0,99       | 51       | 1,39      | 0,24       |
| 15       | 2,26      | 0,92       | 52       | 1,32      | 0,11       |
| 16       | 2,65      | 0,40       | 53       | 1,61      | 0,18       |
| 17       | 3,75      | 0,82       | 54       | 1,58      | 0,17       |
| 18       | 2,93      | 0,52       | 55       | 1,47      | 0,26       |
| 19       | 2,29      | 0,49       | 56       | 1,62      | 0,23       |
| 20       | 2,40      | 0,18       | 57       | 1,46      | 0,13       |
| 21       | 3,19      | 0,16       | 58       | 1,44      | 0,34       |
| 22       | 3,15      | 0,17       | 59       | 1,63      | 0,24       |
| 23       | 3,17      | 1,17       | 60       | 1,66      | 0,20       |
| 24       | 3,72      | 0,71       | 61       | 1,43      | 0,72       |
| 25       | 3,93      | 0,88       | 62       | 1,52      | 0,64       |
| 26       | 3,38      | 0,36       | 63       | 1,84      | 0,70       |
| 27       | 3,31      | 0,81       | 64       | 1,47      | 0,68       |
| 28       | 2,78      | 0,39       | 65       | 1,47      | 0,13       |
| 29       | 2,81      | 0,14       | 66       | 1,40      | 0,43       |
| 30       | 3,51      | 0,40       | 67       | 1,59      | 0,14       |
| 31       | 3,25      | 1,10       | 68       | 4,38      | 0,23       |
| 32       | 3,89      | 1,38       | 69       | 4,70      | 0,57       |
| 33       | 1,96      | 2,41       | 70       | 5,65      | 0,57       |
| 34       | 2,58      | 1,10       | 71       | 5,16      | 0,19       |
| 35       | 3,22      | 0,31       | 72       | 4,68      | 0,19       |
| 36       | 3,51      | 0,30       | 73       | 2,99      | 0,37       |
| 37       | 1,92      | 0,14       | 74       | 2,32      | 0,15       |

| Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|
| 75       | 1,90      | 0,19       |
| 76       | 2,01      | 0,11       |
| 77       | 2,81      | 1,21       |
| 78       | 1,96      | 0,18       |
| 79       | 2,15      | 0,49       |
| 80       | 2,18      | 0,68       |
| 81       | 2,30      | 0,91       |
| 82       | 1,83      | 0,72       |
| 83       | 1,81      | 0,69       |
| 84       | 2,31      | 0,68       |
| 85       | 2,20      | 0,18       |
| 86       | 2,50      | 0,93       |
| 87       | 3,02      | 0,97       |
| 88       | 1,88      | 0,85       |
| 89       | 2,20      | 0,75       |
| 90       | 1,97      | 0,33       |
| 91       | 1,53      | 0,69       |
| 92       | 2,45      | 0,70       |
| 93       | 2,31      | 0,84       |
| 94       | 2,85      | 0,33       |
| 95       | 2,86      | 0,83       |
| 96       | 3,41      | 0,91       |
| 97       | 3,02      | 1,10       |
| 98       | 2,40      | 0,96       |
| 99       | 2,55      | 0,96       |
| 100      | 3,50      | 0,77       |
| 101      | 4,29      | 1,41       |
| 102      | 4,45      | 1,09       |
| 103      | 1,99      | 1,00       |
| 104      | 3,84      | 0,78       |
| 105      | 2,55      | 0,91       |
| 106      | 3,85      | 1,15       |
| 107      | 5,20      | 0,92       |
| 108      | 2,83      | 1,10       |
| 109      | 2,60      | 0,22       |
| 110      | 3,50      | 0,37       |
| 111      | 2,36      | 0,32       |

| Hari Ke- | Kekeruhan | Klor Bebas |
|----------|-----------|------------|
| 112      | 3,12      | 0,55       |
| 113      | 4,49      | 0,21       |
| 114      | 2,75      | 0,43       |
| 115      | 3,69      | 0,32       |
| 116      | 4,22      | 1,16       |
| 117      | 4,38      | 0,61       |
| 118      | 3,97      | 0,73       |
| 119      | 3,72      | 0,91       |
| 120      | 2,61      | 0,93       |
| 121      | 1,58      | 0,80       |
| 122      | 3,72      | 0,22       |
| 123      | 3,71      | 0,10       |
| 124      | 2,82      | 2,20       |
| 125      | 3,68      | 0,18       |
| 126      | 4,52      | 0,41       |
| 127      | 4,67      | 0,41       |
| 128      | 5,67      | 0,25       |
| 129      | 4,55      | 0,15       |
| 130      | 4,04      | 0,25       |
| 131      | 4,92      | 0,24       |
| 132      | 4,79      | 0,42       |
| 133      | 4,44      | 0,37       |
| 134      | 5,07      | 0,18       |
| 135      | 4,46      | 1,18       |

## Lampiran 8. Daftar Riwayat Hidup

### **CURRICULUM VITAE**

#### **A. Data Pribadi**

1. Nama : Ardiansyah Abubakar
2. Tempat, tanggal lahir : Tassilli, 06 Agustus 1995
3. Alamat : Dusun Tassilli Desa Pattallassang Kec.  
Pattallassang Kab. Gowa Sulawesi Selatan
4. Kewarganegaraan : Indonesia
5. Nomor HP : +6281336822560
6. Email : [ardiansyahabubakar946@gmail.com](mailto:ardiansyahabubakar946@gmail.com)
7. Bidang/Ketertarikan : Data Scientist

#### **B. Riwayat Pendidikan**

1. Tamat SMA tahun 2012 di Madrasah Aliyah Guppi Samata;
2. Sarjana (S1) tahun 2016 di Universitas Islam Negeri Alauddin Makassar Jurusan Pendidikan Matematika;
3. Magister (S2) tahun 2022 di Universitas Hasanuddin Departemen Statistika Program Studi Magister Statistika.

#### **C. Riwayat Pekerjaan**

1. 2016, Guru di Madrasah Aliyah Guppi Samata;
2. 2018, Staff Kaur Keuangan di Desa Pattallassang Kec. Pattallassang Kab. Gowa;
3. 2019, Kepala Urusan Keuangan di Desa Pattallassang Kec. Pattallassang Kab. Gowa;
4. 2021, Administrator Database Sistem Keuangan Desa Wilayah Kecamatan Pattallassang di Dinas Pemberdayaan Masyarakat dan Desa Kab. Gowa

#### **D. Karya Ilmiah**

- Abubakar, A., Nursalam., dan Mardhiah., 2016. *Pengaruh Model Pembelajaran Aptitude Treatment Interaction (ATI) Terhadap Hasil Belajar Matematika Siswa ditinjau dari Waktu Belajar dan Ukuran Kelas IX Sekolah Menengah Pertama (SMP) Negeri di Kec. Pattallassang Kab. Gowa*. Jurnal Matematika dan Pembelajaran (MaPan), Vol. 4 (1), June 2016.
- Abubakar, A., Tinungki, G. M., dan Herdiani, E.T., 2022. *Monitoring Variability Process of Water Quality PDAM Tirta Je'ne'berang using MEWMV Control Chart*, Vol. 110 (1), page 362-372, October 2022.