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LAMPIRAN

Lampiran 1. Pembuktian $E(\text{Res}(X|C)|C) = 0$

$$\begin{aligned} E(\text{Res}(X|C)|C) &= E\left(\frac{X - E(X|C)}{\sigma(X|C)} \middle| C\right) \\ &= \frac{1}{\sigma(X|C)} \cdot E(X - E(X|C)|C) \\ &= \frac{1}{\sigma(X|C)} \cdot E(X|C) - E(E(X|C)|C) \\ &= \frac{1}{\sigma(X|C)} \cdot E(X|C) - E(X|C) \\ &= \frac{1}{\sigma(X|C)} \cdot 0 \end{aligned}$$

$$E(\text{Res}(X|C)|C) = 0$$

Lampiran 2. Pembuktian $\text{Var}(\text{Res}(X|C)|C) = 1$

$$\begin{aligned} \text{Var}(\text{Res}(X|C)|C) &= E((\text{Res}(X|C) - E(\text{Res}(X|C)|C))^2|C) \\ &= E(\text{Res}(X|C)|C) - E(E(\text{Res}(X|C)|C)^2|C) \\ &= 0 - E(\text{Res}(X|C)^2|C) \\ &= E(\text{Res}(X|C)^2|C) \\ &= E\left(\left(\frac{X - E(X|C)}{\sigma(X|C)}\right)^2 \middle| C\right) \\ &= \frac{1}{(\sigma(X|C))^2} \cdot E((X - E(X|C))^2|C) \\ &= \frac{1}{(\sigma(X|C))^2} \cdot (\sigma(X|C))^2 \end{aligned}$$

$$\text{Var}(\text{Res}(X|C)|C) = 1$$

Lampiran 3. Pembuktian

$$\text{Res}\left(\frac{P_{i,t}}{P_{i,s}} \middle| \mathcal{P}_i(s)\right) = \frac{\frac{P_{i,t}}{P_{i,s}} - \widehat{f_{s \rightarrow t}^P}}{\sigma_{s \rightarrow t}^P} \sqrt{P_{i,s}}$$

$$\begin{aligned}
\text{Res}\left(\frac{P_{i,t}}{P_{i,s}} \middle| \mathcal{P}_i(s)\right) &= \frac{\frac{P_{i,t}}{P_{i,s}} - E\left(\frac{P_{i,t}}{P_{i,s}} \middle| \mathcal{P}_i(s)\right)}{\sigma\left(\frac{P_{i,t}}{P_{i,s}} \middle| \mathcal{P}_i(s)\right)} \\
&= \frac{\frac{P_{i,t}}{P_{i,s}} - \widehat{f}_{s \rightarrow t}^P}{\sqrt{\text{var}\left(\frac{P_{i,t}}{P_{i,s}} \middle| \mathcal{P}_i(s)\right)}} \\
&= \frac{\frac{P_{i,t}}{P_{i,s}} - \widehat{f}_{s \rightarrow t}^P}{\sqrt{\frac{(\widehat{\sigma}_{s \rightarrow t}^P)^2}{P_{i,s}}}} \\
&= \frac{\frac{P_{i,t}}{P_{i,s}} - \widehat{f}_{s \rightarrow t}^P}{\widehat{\sigma}_{s \rightarrow t}^P} \sqrt{P_{i,s}}
\end{aligned}$$

Lampiran 4. Pembuktian

$$\begin{aligned}
\text{Res}\left(\frac{I_{i,t}}{I_{i,s}} \middle| \mathcal{J}_i(s)\right) &= \frac{\frac{I_{i,t}}{I_{i,s}} - \widehat{f}_{s \rightarrow t}^I}{\widehat{\sigma}_{s \rightarrow t}^I} \sqrt{I_{i,s}} \\
\text{Res}\left(\frac{I_{i,t}}{I_{i,s}} \middle| \mathcal{J}_i(s)\right) &= \frac{\frac{I_{i,t}}{I_{i,s}} - E\left(\frac{I_{i,t}}{I_{i,s}} \middle| \mathcal{J}_i(s)\right)}{\sigma\left(\frac{I_{i,t}}{I_{i,s}} \middle| \mathcal{J}_i(s)\right)} \\
&= \frac{\frac{I_{i,t}}{I_{i,s}} - \widehat{f}_{s \rightarrow t}^I}{\sqrt{\text{var}\left(\frac{I_{i,t}}{I_{i,s}} \middle| \mathcal{J}_i(s)\right)}} \\
&= \frac{\frac{I_{i,t}}{I_{i,s}} - \widehat{f}_{s \rightarrow t}^I}{\sqrt{\frac{(\widehat{\sigma}_{s \rightarrow t}^I)^2}{I_{i,s}}}} \\
&= \frac{\frac{I_{i,t}}{I_{i,s}} - \widehat{f}_{s \rightarrow t}^I}{\widehat{\sigma}_{s \rightarrow t}^I} \sqrt{I_{i,s}}
\end{aligned}$$

Lampiran 5. Pembuktian

$$\mathbf{Res} \left(Q_{i,s}^{-1} \middle| \mathcal{P}_i(s) \right) = \frac{Q_{i,s}^{-1} - \hat{q}_s^{-1}}{\hat{\rho}_s^P} \sqrt{P_{i,s}}$$

$$\begin{aligned} \mathbf{Res} \left(Q_{i,s}^{-1} \middle| \mathcal{P}_i(s) \right) &= \frac{Q_{i,s}^{-1} - E \left(Q_{i,s}^{-1} \middle| \mathcal{P}_i(s) \right)}{\sigma \left(Q_{i,s}^{-1} \middle| \mathcal{P}_i(s) \right)} \\ &= \frac{Q_{i,s}^{-1} - \hat{q}_s^{-1}}{\sqrt{\text{var} \left(Q_{i,s}^{-1} \middle| \mathcal{P}_i(s) \right)}} \\ &= \frac{Q_{i,s}^{-1} - \hat{q}_s^{-1}}{\sqrt{\frac{(\hat{\rho}_s^P)^2}{P_{i,s}}}} \\ &= \frac{Q_{i,s}^{-1} - \hat{q}_s^{-1}}{\hat{\rho}_s^P} \sqrt{P_{i,s}} \end{aligned}$$

Lampiran 6. Pembuktian

$$\mathbf{Res} \left(Q_{i,s} \middle| \mathcal{J}_i(s) \right) = \widehat{\mathbf{Res}}(Q_{i,s}) = \frac{Q_{i,s} - \hat{q}_s}{\hat{\rho}_s^I} \sqrt{I_{i,s}}$$

$$\begin{aligned} \mathbf{Res} \left(Q_{i,s} \middle| \mathcal{J}_i(s) \right) &= \frac{Q_{i,s} - E \left(Q_{i,s} \middle| \mathcal{J}_i(s) \right)}{\sigma \left(Q_{i,s} \middle| \mathcal{J}_i(s) \right)} \\ &= \frac{Q_{i,s} - \hat{q}_s}{\sqrt{\text{var} \left(Q_{i,s} \middle| \mathcal{J}_i(s) \right)}} \\ &= \frac{Q_{i,s} - \hat{q}_s}{\sqrt{\frac{(\hat{\rho}_s^I)^2}{I_{i,s}}}} \\ &= \frac{Q_{i,s} - \hat{q}_s}{\hat{\rho}_s^I} \sqrt{I_{i,s}} \end{aligned}$$