

DAFTAR PUSTAKA

- Badan Pusat Statistik. (2022). *Indeks Pembangunan Manusia 2022*. Jakarta (ID): Badan Pusat Statistik.
- Badan Pusat Statistik. (2023). *Analisis Indikator Makro Ekonomi 2023*. Makassar: Badan Pusat Statistik Provinsi Sulawesi Selatan.
- Badan Pusat Statistik. (2023). *Indikator Kesejahteraan Rakyat 2022*. Jakarta (ID): Badan Pusat Statistik.
- Badan Pusat Statistik. (2023). *Provinsi Sulawesi Selatan Dalam Angka 2023*. Makassar: Badan Pusat Statistik Provinsi Sulawesi Selatan.
- Breiman, L. (1996). Bagging Prediktors. *Machine learning*, 24, 123-140.
- Budiantara, I.N. (2009). Spline dalam Regresi Nonparametrik dan Semiparametrik: Sebuah Pemodelan Statistika Masa Kini dan Masa Mendatang, *Jurnal Sains Dan Seni Pomits*, Vol. 3, No.1.
- Buhlmann, P., & Yu, B. (2002). Analyzing Bagging, *The Annals of Statistics*. Vol 30 No. 4, Hal 927-961.
- Craven, P., & Wahba, G. (1979). Smoothing Noisy Data with Spline Functions. Estimating The Correct Degree of Smoothing by The Method of Generalized Cross Validation, *Numer Math*, (31), 377-403.
- Dewi, R. K., & Budiantara, I. N. (2012). Faktor-Faktor yang Memengaruhi Angka Gizi Buruk Di Jawa Timur dengan Pendekatan Regresi Nonparametrik Spline. *Jurnal Sains Dan Seni ITS*, 1(1), 177–182.
- Draper, N.R. and Smith, H. (1998). *Applied Regression Analysis*. Third Edition. John Wiley & Sons.6
- Eubank, R.L. (1999). *Nonparametric Regression and Spline Smoothing*. Second Edition. New York. Marcel Dekker, Inc.
- Foster, J., Greer, J., and Thorbecke, E. (1984). A Class of Decomposable Poverty Measures. *Econometrica*, 52: 761-766.
- Friedman JH. (1991). *Multivariate Adaptive Regression Spline*. California (US): Stanford University.
- ..., J.H. and Silverman, B.W. (1989). Flexible Parsimony Smoothing and Additive Modeling. *Technometrics*, 31, 3-39.



- Ferezagia, D. V. (2018). Analisis Tingkat Kemiskinan di Indonesia. *Jurnal Sosial Humaniora Terapan*, 1(1), 1-6.
- Ghozali, I. (2016). *Aplikasi Analisis Multivariate dengan Program IBM SPSS 23* (VIII). Semarang: Badan Penerbit Universitas Diponegoro.
- Hardle, W. (1990). *Applied Nonparametric Regression*. Cambridge University Press, Cambridge U.K.
- Hasanah, R., Syaparuddin, S., & Rosmeli, R. (2021). Pengaruh angka harapan hidup, rata-rata lama sekolah dan pengeluaran perkapita terhadap tingkat kemiskinan pada Kabupaten/Kota di Provinsi Jambi. *e-Jurnal Perspektif Ekonomi dan Pembangunan Daerah*, 10(3), 223-232.
- Insany, A. N., Nur'aeni, & Fajri, M. (2019). Pemodelan IPM Di Kawasan Timur Indonesia Menggunakan Multivariate Adaptive Regression Spline (MARS). *Natural Science: Journal of Science and Technology*, 8(2), 94–98.
- Jusuf, H., Otok, B. W., & Ningrum, A. R. (2016). Ketepatan Klasifikasi Status Diabetes Melitus dengan Pendekatan Multivariate Adaptive Regression Spline. *J Statistika*, 9(1), 19-22.
- Kharisma, R. D. L., Juhari, J., & Rosa, R. A. (2021). Multivariate adaptive regression splines and bootstrap aggregating multivariate adaptive regression splines of poverty in Central Java. *Cauchy: Jurnal Matematika Murni dan Aplikasi*, 6(4), 238-245.
- Khotijah, L. (2020). *Pemodelan Regresi Nonparametrik Truncated Spline pada Indeks Pembangunan Manusia di Jawa Timur*. Skripsi, Universitas Islam Negeri Maulana Malik Ibrahim, Malang.
- Maulana, R., Pitoyo, A. J., & Alfana, M. A. F. (2022). Analisis Pengaruh Kemiskinan dan Kondisi Ekonomi Terhadap Indeks Pembangunan Manusia di Provinsi Jawa Tengah Tahun 2013-2017. *Media Komunikasi Geografi*, 23(1), 12-24.
- Mirah, M. R., Kindangen, P., & Rorong, I. P. F. (2021). Pengaruh tingkat partisipasi angkatan kerja terhadap pertumbuhan ekonomi dan kemiskinan provinsi sulawesi utara. *Jurnal Pembangunan Ekonomi Dan Keuangan Daerah*, 21(1), 85-100.



- Moisen, G. G., & Frescino, T. S. (2002). Comparing five modelling techniques for predicting forest characteristics. *Ecological modelling*, 157(2-3), 209-225.
- Nash, M., & Bradford, D. (2001). *Parametric and Non Parametric Logistic Regression for Prediction of Precense/Absence of an Amphibian*. Las Vegas, Nevada.
- Pratiwi, D. A., Budiantara, I. N., & Wibowo, W. (2017). Pendekatan Regresi Semiparametrik Spline untuk Memodelkan Rata-Rata Umur Kawin Pertama (UKP) di Provinsi Jawa Timur. *Jurnal Sains Dan Seni ITS*, 6(1), 129–136.
- Pudjianto, B. & Syawie, M. (2015). Kemiskinan dan Pembangunan Manusia. *Sosio Informa*, 1(3), 231-246
- Sanusi, W., Syam, R., & Adawiyah, R. (2019). Model regresi nonparametrik dengan pendekatan spline (studi kasus: Berat badan lahir rendah di rumah sakit ibu dan anak siti fatimah makassar). *Journal of Mathematics, Computations, and Statistics*, 2(1), 70-81.
- Sari, S. K. P., Santoso, R., & Suparti, S. (2017). Prediksi Simpanan Berjangka Pada Bank Umum Dan BPR Menggunakan Metode Arima dengan Outliers dan Arima *Bootstrap*. *Jurnal Gaussian*, 6(3), 459-468.
- Sugiyanto, F. X. (2022). Mengukur Kesejahteraan Rakyat. *Media dan Anlisis Magister Ilmu Ekonomi Fakultas Ekonomika dan Bisnis Universitas Diponegoro*. Diakses 28 September 2023, <https://mie.feb.undip.ac.id/archives/17447>
- Utami, I. P. (2016). *Pemodelan Resiko Kejadian Malnutrisi pada Pasien Anak Penderita Penyakit ISPA dengan Pendekatan MARS*. Surabaya: Unair.
- Walpole. R.E. (1995). Pengantar Statistika edisi ke-3. *Jakarta: Gramedia Pustaka Utama*.
- Wang, Y., Guo, W. and Brown, M.B. (2000). Spline Smoothing for Bivariate Data with Application to Association Between Hormones. *Statistica Sinica* 10, 377-397.



LAMPIRAN



Lampiran 1. Data

Kabupaten/Kota	y_1	y_2	x_1	x_2	x_3	x_4	x_5
Kepulauan Selayar	12.24	68.35	68.81	76.21	69.93	3.67	45.38
Bulukumba	7.39	70.34	68.51	82.85	65.27	3.81	41.75
Bantaeng	9.07	69.69	70.88	74.22	75.36	15.45	40.27
Jeneponto	13.73	65.13	66.81	70.89	75.26	3.81	43.14
Takalar	8.25	68.31	67.64	77	64.46	4.64	45.35
Gowa	7.36	70.99	70.7	79.1	73.16	4.59	43.92
Sinjai	8.8	68.33	67.68	80.84	63.34	4.87	44.55
Maros	9.43	71	69.28	80.45	61.37	9.13	45.37
Pangkajene dan Kepulauan	13.92	69.79	67.12	74.64	74.66	4.93	46.79
Barru	8.4	71.53	69.35	81.48	62.36	5.11	47.94
Bone	10.58	67.01	67.57	75.63	67.48	5.23	45.26
Soppeng	7.49	69.7	70.2	82.28	61.9	6.18	44.98
Wajo	6.57	70.26	67.82	73.13	61.13	2.38	43.66
Sindereng Rappang	5.11	72.06	70.41	77.99	57.63	4.86	46.72
Pinrang	8.79	71.97	70.15	77.94	57.72	4.52	46.25
Enrekang	12.39	73.39	71.17	83.45	72.05	3.71	47.77
Luwu	12.49	71.36	70.75	79.38	67.74	5.69	47.35
Tana Toraja	12.18	69.88	73.72	78.28	85.11	5.12	44.62
Luwu Utara	13.22	70.51	69.03	76.3	72.23	4.54	44.21
Luwu Timur	6.81	73.92	70.94	80.35	71.51	1.99	48.17
Toraja Utara	11.65	70.36	73.65	83.76	68.84	5.27	54.43
Makassar	4.58	83.12	72.4	80.77	59.27	5.40	42.94
Parepare	5.41	78.54	71.57	79.57	63.62	5.93	45.13
Palopo	7.78	78.91	71.18	82.62	63.65	5.83	44.32



Lampiran 2. Hasil Model Terbaik MARS Respon Persentase Penduduk Miskin

```

LEARNING SAMPLE STATISTICS
=====

```

VARIABLE	MEAN	SD	N	SUM
Y1	9.3183	2.8304	24.0000	223.6400
X1	69.8892	1.9381	24.0000	1677.3400
X2	78.7138	3.4353	24.0000	1889.1300
X3	67.2938	6.7226	24.0000	1615.0500
X4	5.2775	2.5633	24.0000	126.6600
X5	45.4279	2.7160	24.0000	1090.2700


```

Ordinal Response
-----

```

	min	Q25	Q50	Q75	max
Y1	4.5800	7.3600	8.7900	12.1800	13.9200


```

Ordinal Predictor Variables: 5
-----

```

	min	Q25	Q50	Q75	max
X1	66.8100	67.8200	70.1500	70.9400	73.7200
X2	70.8900	76.2100	79.1000	80.8400	83.7600
X3	57.6300	61.9000	65.2700	72.0500	85.1100
X4	1.9900	3.8100	4.8700	5.4000	15.4500
X5	40.2700	43.9200	45.1300	46.7200	54.4300


```

Forward Stepwise Knot Placement
=====

```

BasFn(s)	GCV	IndBsFns	EfPrms	Variable	Knot	Parent	BsF
0	8.3597	0.0	1.0				
1	6.3293	1.0	4.0	X3	57.6300		
3 2	7.9329	3.0	8.0	X4	3.6700		
5 4	10.9009	5.0	12.0	X2	82.8500		
6	15.3779	6.0	15.0	X1	66.8100		
7	26.6806	7.0	18.0	X5	40.2700		
9 8	94.9532	8.0	21.0	X1	69.0300		


```

Model 1 of 8
Estimated optimal model = response mean.
Model 2 of 8
Estimated optimal model = response mean.
Model 3 of 8
Estimated optimal model = response mean.
Model 4 of 8
Model 5 of 8
Model 6 of 8
Model 7 of 8
Model 8 of 8

```

Piecewise Linear GCV = 6.0243, #efprms = 3.5000

```

Final Model (After Backward Stepwise Elimination)
=====

```

Basis Fun	Coefficient	Variable	Parent	Knot
0	5.0422			
1	0.3371	X3		57.6300
3	-2.2314	X4		3.6700
7	0.4891	X5		40.2700
8	-0.9538	X1		69.0300



Piecewise Linear GCV = 5.8237, #efprms = 11.0000

ANOVA Decomposition on 4 Basis Functions

```
=====
```

fun	std. dev.	-gcv	#bsfns	#efprms	variable
1	2.2185	14.8517	1	2.5000	X3
2	0.9244	6.1164	1	2.5000	X4
3	1.3003	7.5470	1	2.5000	X5
4	1.3499	7.6079	1	2.5000	X1

Piecewise Cubic Fit on 4 Basis Functions, GCV = 6.6210

Relative Variable Importance

```
=====
```

	Variable	Importance	-gcv
	3 X3	100.0000	14.8517
	1 X1	44.4562	7.6079
	5 X5	43.6896	7.5470
	4 X4	18.0060	6.1164
	2 X2	0.0000	5.8237

ORDINARY LEAST SQUARES RESULTS

```
=====
```

N: 24.0000 R-SQUARED: 0.7774
 MEAN DEP VAR: 9.3183 ADJ R-SQUARED: 0.7306
 UNCENTERED R-SQUARED = R-0 SQUARED: 0.9819

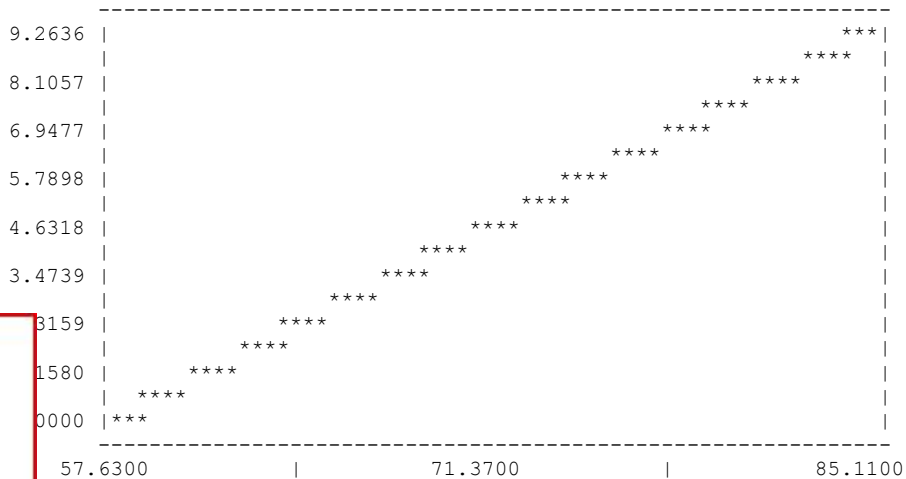
PARAMETER	ESTIMATE	S.E.	T-RATIO	P-VALUE
Constant	5.0422	0.8121	6.2090	.577728E-05
Basis Function 1	0.3371	0.0477	7.0627	.101275E-05
Basis Function 3	-2.2314	0.7290	-3.0607	0.0064
Basis Function 7	0.4891	0.1223	4.0003	0.0008
Basis Function 8	-0.9538	0.2363	-4.0356	0.0007

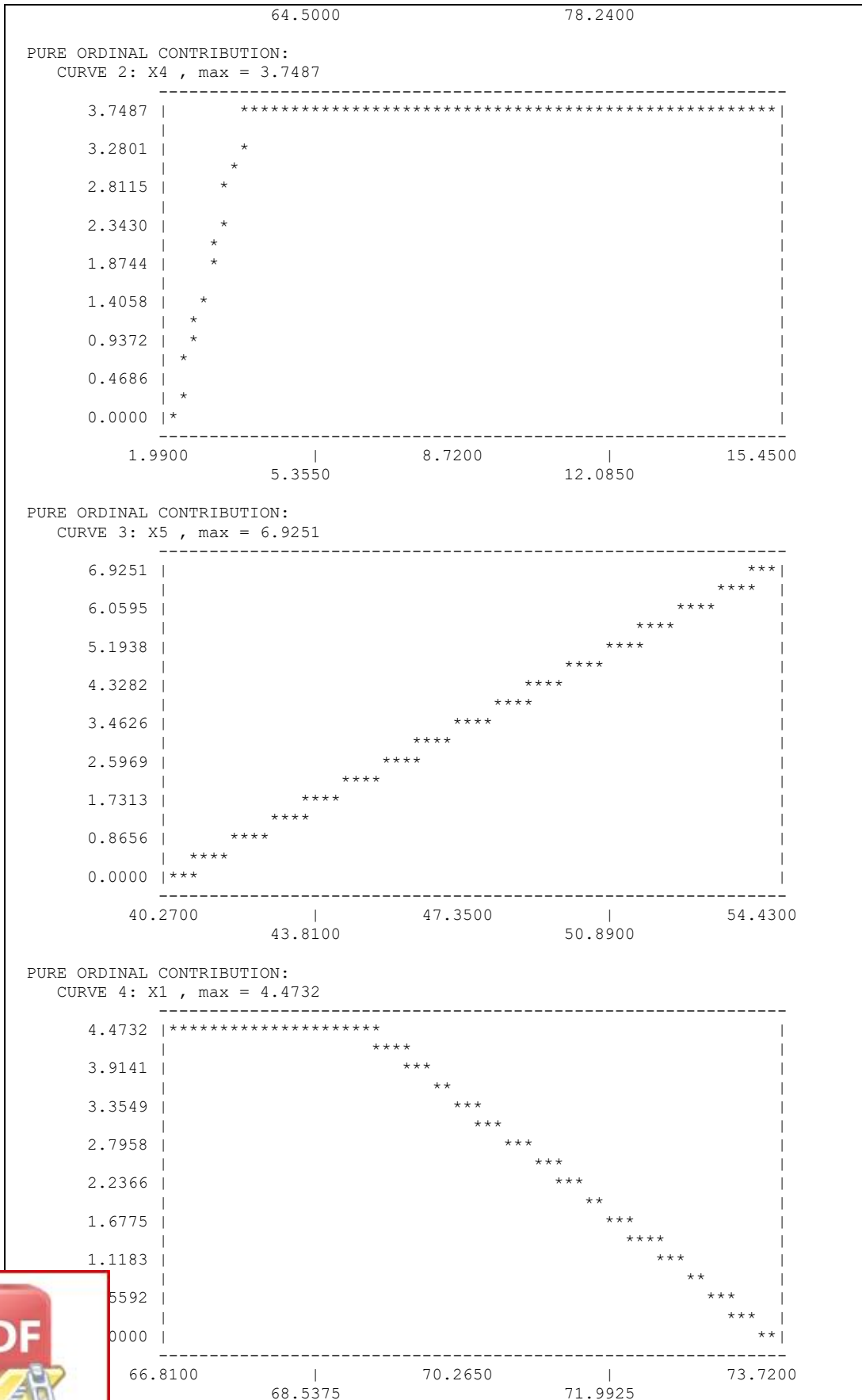
```
-----
```

F-STATISTIC = 16.5928 S.E. OF REGRESSION = 1.4691
 P-VALUE = .529950E-05 RESIDUAL SUM OF SQUARES = 41.0086
 [MDF,NDF] = [4, 19] REGRESSION SUM OF SQUARES = 143.2523

The Following Graphics Are Piecewise Linear

PURE ORDINAL CONTRIBUTION:
 CURVE 1: X3 , max = 9.2636





4 curves and 0 surfaces.

Basis Functions
=====

```
BF1 = max(0, X3 - 57.6300);  
BF3 = max(0, 3.6700 - X4 );  
BF7 = max(0, X5 - 40.2700);  
BF8 = max(0, X1 - 69.0300);
```

```
Y = 5.0422 + 0.3371 * BF1 - 2.2314 * BF3 + 0.4891 * BF7  
      - 0.9538 * BF8;
```

```
model Y1 = BF1 BF3 BF7 BF8;
```



Lampiran 3. Hasil Model Terbaik MARS Respon Indeks Pembangunan Manusia

```

LEARNING SAMPLE STATISTICS
=====
VARIABLE          MEAN          SD          N          SUM
-----
Y2                71.4354       3.9453      24.0000    1714.4500
X1                69.8892       1.9381      24.0000    1677.3400
X2                78.7138       3.4353      24.0000    1889.1300
X3                67.2938       6.7226      24.0000    1615.0500
X4                 5.2775       2.5633      24.0000     126.6600
X5                45.4279       2.7160      24.0000    1090.2700

Ordinal Response
      min          Q25          Q50          Q75          max
-----
Y2        65.1300       69.6900       70.3600       71.9700       83.1200

Ordinal Predictor Variables: 5
      min          Q25          Q50          Q75          max
-----
X1        66.8100       67.8200       70.1500       70.9400       73.7200
X2        70.8900       76.2100       79.1000       80.8400       83.7600
X3        57.6300       61.9000       65.2700       72.0500       85.1100
X4         1.9900         3.8100         4.8700         5.4000        15.4500
X5        40.2700       43.9200       45.1300       46.7200       54.4300

Forward Stepwise Knot Placement
=====
BasFn(s)   GCV   IndBsFns  EfPrms  Variable          Knot          Parent  BsF
-----
0          16.2420  0.0    1.0
2 1         8.6019  2.0    5.0    X1                72.4000
4 3         4.9011  3.0    8.0    X1                70.7500
5          6.3995  4.0   11.0    X3                57.6300
7 6         9.0740  5.0   14.0    X1                71.1800
9 8        18.6661  7.0   18.0    X2                82.8500
10         63.1916  8.0   21.0    X5                40.2700

Model 1 of 8
Estimated optimal model = response mean.
Model 2 of 8
Estimated optimal model = response mean.
Model 3 of 8
Model 4 of 8
Model 5 of 8
Model 6 of 8
Model 7 of 8
Model 8 of 8

Estimated optimal model = response mean.

Piecewise Linear GCV = 16.2420, #efprms = 1.0000

Final Model (After Backward Stepwise Elimination)
=====
Basis Fun  Coefficient  Variable  Parent  Knot
-----
0          73.6424
1         -16.9724    X1        72.4000
2          -1.0921    X1        72.4000
3           6.2320    X1        70.7500

Piecewise Linear GCV = 5.2224, #efprms = 8.5000
    
```



ANOVA Decomposition on 3 Basis Functions

fun	std. dev.	-gcv	#bsfns	#efprms	variable
1	3.5691	16.2420	3	7.5000	X1

Piecewise Cubic Fit on 3 Basis Functions, GCV = 6.3289

Relative Variable Importance

Variable	Importance	-gcv
1 X1	100.0000	16.2420
2 X2	0.0000	5.2224
3 X3	0.0000	5.2224
4 X4	0.0000	5.2224
5 X5	0.0000	5.2224

ORDINARY LEAST SQUARES RESULTS

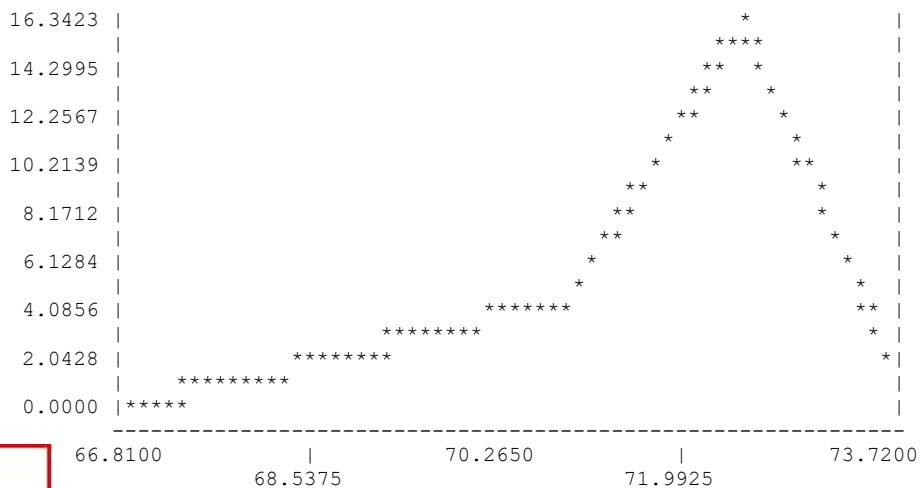
N: 24.0000 R-SQUARED: 0.8540
 MEAN DEP VAR: 71.4354 ADJ R-SQUARED: 0.8321
 UNCENTERED R-SQUARED = R-0 SQUARED: 0.9996

PARAMETER	ESTIMATE	S.E.	T-RATIO	P-VALUE
Constant	73.6424	0.9838	74.8567	.999201E-15
Basis Function 1	-16.9725	2.3392	-7.2556	.509390E-06
Basis Function 2	-1.0921	0.2773	-3.9382	0.0008
Basis Function 3	6.2320	1.1474	5.4313	.257146E-04

F-STATISTIC = 38.9863 S.E. OF REGRESSION = 1.6168
 P-VALUE = .151943E-07 RESIDUAL SUM OF SQUARES = 52.2785
 [MDF,NDF] = [3, 20] REGRESSION SUM OF SQUARES = 305.7213

The Following Graphics Are Piecewise Linear

PURE ORDINAL CONTRIBUTION:
 CURVE 1: X1 , max = 16.342



and 0 surfaces.

functions



```
=====  
BF1 = max(0, X1 - 72.4000);  
BF2 = max(0, 72.4000 - X1 );  
BF3 = max(0, X1 - 70.7500);  
  
Y = 73.6424 - 16.9724 * BF1 - 1.0921 * BF2 + 6.2320 * BF3;  
  
model Y2 = BF1 BF2 BF3;  
>
```



Lampiran 4. Hasil Pemodelan Bagging MARS Respon Persentase Penduduk Miskin

```

$Resample01
Selected 5 of 8 terms, and 3 of 4 predictors
Termination condition: Reached nk 10
Importance: x1, x5, x3, x4-unused
Number of terms at each degree of interaction: 1 4 (additive
model)
GCV 2.074656      RSS 19.4499      GRSq 0.552719      RSq 0.8097576

$Resample02
Selected 6 of 9 terms, and 4 of 4 predictors
Termination condition: Reached nk 10
Importance: x3, x4, x1, x5
Number of terms at each degree of interaction: 1 5 (additive
model)
GCV 3.588347      RSS 25.26794      GRSq 0.6235233      RSq 0.8797267

$Resample03
Selected 5 of 8 terms, and 3 of 4 predictors
Termination condition: Reached nk 10
Importance: x3, x4, x5, x1-unused
Number of terms at each degree of interaction: 1 4 (additive
model)
GCV 3.126089      RSS 29.30708      GRSq 0.5943904      RSq 0.8274817

$Resample04
Selected 6 of 9 terms, and 4 of 4 predictors
Termination condition: Reached nk 10
Importance: x3, x4, x5, x1
Number of terms at each degree of interaction: 1 5 (additive
model)
GCV 1.584528      RSS 11.15771      GRSq 0.8073496      RSq 0.9384538
.
.
.
$Resample16
Selected 8 of 9 terms, and 4 of 4 predictors
Termination condition: Reached nk 10
Importance: x3, x5, x4, x1
Number of terms at each degree of interaction: 1 7 (additive
model)
GCV 0.2970955      RSS 1.002697      GRSq 0.9673066      RSq 0.994994
14.12947
- 0.3375309 * max(0, 69.03 - x1)
- 0.4358623 * max(0, x1 - 69.03)
- 0.4473715 * max(0, 74.66 - x3)
- 6.389547 * max(0, x3 - 74.66)
+ 0.4009327 * max(0, x4 - 6.18)
- 0.8170762 * max(0, 44.55 - x5)
+ 0.2101373 * max(0, x5 - 44.55)
.
.
.
$Resample50
Selected 5 of 9 terms, and 4 of 4 predictors
Termination condition: Reached nk 10
Importance: x3, x4, x1, x5
Number of terms at each degree of interaction: 1 4 (additive
model)
GCV 3.71832      RSS 26.92343      GRSq 0.7383014      RSq 0.8886915

```



Lampiran 5. Hasil Pemodelan Bagging MARS Respon Indeks Pembangunan Manusia

```

$Resample01
Selected 4 of 5 terms, and 1 of 1 predictors
Termination condition: RSq changed by less than 0.001 at 5 terms
Importance: x1
Number of terms at each degree of interaction: 1 3 (additive
model)
GCV 3.635919    RSS 43.78252    GRSq 0.8196138    RSq 0.9014525

$Resample02
Selected 4 of 5 terms, and 1 of 1 predictors
Termination condition: RSq changed by less than 0.001 at 5 terms
Importance: x1
Number of terms at each degree of interaction: 1 3 (additive
model)
GCV 4.616268    RSS 55.58756    GRSq 0.6527217    RSq 0.8102771

$Resample03
Selected 5 of 6 terms, and 1 of 1 predictors
Termination condition: Reached nk 10
Importance: x1
Number of terms at each degree of interaction: 1 4 (additive
model)
GCV 0.8084382    RSS 7.579108    GRSq 0.9595956    RSq 0.9828148

$Resample04
Selected 5 of 6 terms, and 1 of 1 predictors
Termination condition: Reached nk 10
Importance: x1
Number of terms at each degree of interaction: 1 4 (additive
model)
GCV 2.818748    RSS 26.42576    GRSq 0.784982    RSq 0.9085462
.
.
.

$Resample17
Selected 4 of 5 terms, and 1 of 1 predictors
Termination condition: RSq changed by less than 0.001 at 5 terms
Importance: x1
Number of terms at each degree of interaction: 1 3 (additive
model)
GCV 0.7036284    RSS 8.472858    GRSq 0.914197    RSq 0.9531247

72.59497
+ 6.240287 * max(0, x1 - 70.7)
- 0.6347138 * max(0, 72.4 - x1)
- 16.38992 * max(0, x1 - 72.4)
.
.
.

$Resample50
Selected 3 of 5 terms, and 1 of 1 predictors
Termination condition: RSq changed by less than 0.001 at 5 terms
Importance: x1
Number of terms at each degree of interaction: 1 2 (additive
model)
GCV 386881    RSS 35.90266    GRSq 0.4907824    RSq 0.6524999

```

