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Desain Penampang Benda Uji

Data perencanaan

Kuat tekan beton	f_c	= 20	MPa
Tegangan leleh baja	f_y	= 336.75	MPa
Modulus Elastis Beton	E_c	= 21019	MPa
Modulus Elastis Baja	E_s	= 200000	MPa

Asumsi tinggi penampang yang disyaratkan ACI untuk lendutan :

$$\text{Panjang bentang } L_n = 3.0 \text{ m} = 3000 \text{ mm}$$

$$h = \frac{L_n}{16}$$

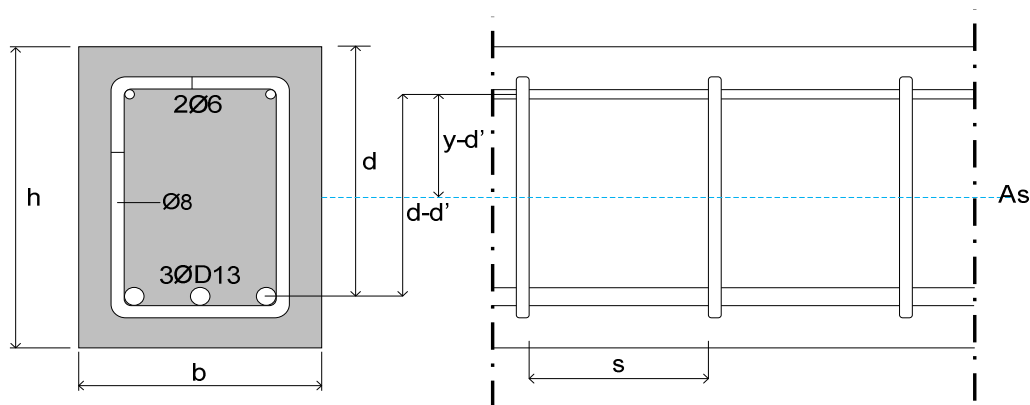
$$= 187.5 \text{ mm} \approx 200 \text{ mm}$$

$$\text{Tinggi Efektif Balok } d = 150 \text{ mm}$$

$$r = b/d, \text{ ----- dimana : } r = 0.25 \text{ \& } 0.6$$

$$b = 90 \text{ mm} \approx 150 \text{ mm}$$

Perhitungan momen desain luar akibat beban (M_u)



$$M_u = \Phi M_n$$

$$M_u = \Phi * A_s * f_y * \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur } \Phi = 0.9$$

dimana :

$$\rho_{\max} = 0.75 \rho_b$$

$$\rho_b = \beta_1 * \frac{0.85 f_c}{f_y} * \frac{600}{600 + f_y} \quad \text{untuk } \beta_1 = 0.85 \text{ dimana } f_c < 28 \text{ Mpa}$$

$$= 0.85 * \frac{0.85 * 20}{336.75} * \frac{600}{600 + 336.75}$$

$$= 0.042910171 * 0.6405 = 0.027484497$$

$$= 0.75 * 0.027484497 = 0.020613373$$

$$A_s = \rho_b * b * d$$

$$= 0.020613373 * 150 * 150$$

$$= 463.8008848 \text{ mm}^2$$

$$a = \frac{A_s * f_y}{0.85 * f_c * b}$$

$$= \frac{463.800885 * 336.75}{0.85 * 3000} = 61.2489992 \text{ mm}$$

$$M_u = 0.90 * 463.8008848 * 336.75 * \left(150 - \frac{61.2489992}{2} \right)$$

$$\begin{aligned}
 &= 140566.453 * 44.3755004 \\
 &= 6237706.699 \text{ Nmm} \\
 &= \boxed{6.2377067} \text{ kNm}
 \end{aligned}$$

$$Mu = 0.35 P + 0.81$$

$$P = \frac{6.2377067 - 0.81}{0.35} = \boxed{15.5077334} \text{ kN}$$

Momen tahanan nominal yang diperlukan :

$$\begin{aligned}
 Mn &= \frac{Mu}{\phi} = \frac{6237706.699}{0.9} \\
 &= 6930785.221 \text{ Nmm} \\
 &= \boxed{6.93078522} \text{ kNm}
 \end{aligned}$$

$$Mn = 0.35 P + 0.81$$

$$Pu = \frac{6.93078522 - 0.81}{0.35} = \boxed{17.4879578} \text{ kN}$$

Asumsikan angka penulangan $\rho = 0.35$ $\rho_b = 0.00961957$

$$\begin{aligned}
 As &= \rho b * b * d \\
 &= 0.00961957 * 150 * 150 \\
 &= 216.440413 \text{ mm}^2
 \end{aligned}$$

Digunakan tulangan 3 ϕ D 13

$$As = 398.196869 \text{ mm}^2 > As = 216.440413 \text{ mm}^2 \dots\dots\dots\text{OK}$$

$$\rho = \frac{As}{bd} = \frac{398.196869}{22500} = 0.01769764$$

$$\rho_{min} = \frac{200}{fy} = \frac{1.4}{336.75} = 0.00409503$$

Periksa baja yang disyaratkan :

$$0.75 \rho_b = 0.02061337 > \rho = 0.01769764 > \rho_{min} = 0.00409503 \dots\dots\dots\text{OK}$$

Syarat bahwa tulangan melesah :

$$\rho_{maks} = 0.02061337 > \rho = 0.01769764 \dots\dots\dots\text{Tulangan Melesah}$$

$$\begin{aligned}
 a &= \frac{As * fy}{0.85 * f'c * b} \\
 &= \frac{398.196869 * 336.75}{0.85 * 3000} = 52.58541 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 Mn &= As * fy * \left(d - \frac{a}{2} \right) \text{ digunakan nilai } a = 61.249 \text{ mm} \\
 &= 398.196869 * 336.75 * 123.707295 \\
 &= 16588257.02 \text{ Nmm} \\
 &= \boxed{16.588257} \text{ kNm}
 \end{aligned}$$

$$Mu = 0.35 P + 0.81 = 16.588257$$

$$P = \frac{16.58825702 - 0.81}{0.35} = \boxed{45.0807343} \text{ kN}$$

$$Mn = 6.93078522 > Mu = 6.2377067 \text{ kNm} \dots\dots\dots\text{Analisis Tulangan Tunggal}$$

$$\text{persentasi desain lebih} = \frac{6.93078522 - 6.2377067}{6.237706699} = 11.111 \%$$

Perencanaan kekuatan geser

Gaya geser maksimum:

Pada pengujian diharapkan retak akibat lentur mendahului retak akibat geser. Untuk memastikan tidak terjadi kegagalan geser sebelum kegagalan lentur terjadi, maka beban geser terbesar .

$$\begin{aligned} V_u &= 0.50 P + 1.08 \text{ kN} \\ &= 0.50 * 15.5077334 + 1.08 \\ &= 8.83386671 \text{ kN} = 17.6677334 \text{ kN} \end{aligned}$$

Kekuatan beton menahan geser:

$$\begin{aligned} V_c &= \left(\frac{\sqrt{f_c}}{6} \right) * b_w * d \\ &= 0.7454 * 150 * 150 \\ &= 16771 \text{ MPa} = 16.771 \text{ kN} \end{aligned}$$

$$\begin{aligned} \Phi V_c &= 0.85 * V_c && \text{faktor reduksi untuk geser} && \Phi = 0.85 \\ &= 14.2549334 \text{ kN} \end{aligned}$$

Periksa :

$$V_u = 17.6677334 > 1/2 \Phi V_c = 7.12746668 \text{ kN} \quad \dots\dots\dots \text{Diperlukan sengkang}$$

Desain sengkang

$$\begin{aligned} V_s &= \frac{V_u - \Phi V_c}{\Phi} = \frac{17.6677334 - 14.2549334}{0.85} \\ &= 4.0150589 \text{ kN} \end{aligned}$$

Periksa :

$$V_s < \frac{2}{3} \sqrt{f_c} * b_w * d = 67082.0393 \text{ Mpa} = 67.082 \text{ kN}$$

$$V_s = V_u - V_c = 17.6677334 - 16.771 = 0.89722359 \text{ kN}$$

$$V_s = 0.89722359 < 67.082 \text{ kN} \quad \dots\dots\dots \text{Penampang tidak diperbesar}$$

Hitung jarak sengkang teoritis

$$\text{Jarak dari tumpuan } d = \text{tinggi efektif balok} = 150 \text{ mm}$$

$$\text{direncanakan menggunakan tulangan sengkang} = \Phi 8$$

$$A_v = 50.265 \text{ mm}^2$$

$$\begin{aligned} s &= \frac{A_v * f_y * d}{V_s} = \frac{50.265 * 336.75 * 150}{897.2235933} \\ &= 2829.88009 \text{ mm} \end{aligned}$$

$$\text{jarak maksimum } s = d/2 = 75 \text{ mm}$$

$$A_{v_{\min}} = \frac{1}{3} * \frac{b_w s}{f_y} = 11.136 < A_v = 50.265 \text{ mm}^2 \quad \dots\dots\dots \text{OK}$$

$$\text{Maka digunakan sengkang} = \Phi 8 - 90 \text{ mm} \text{ pada daerah } 1/3 \text{ bentang tepi}$$

$$= \Phi 8 - 175 \text{ mm} \text{ pada daerah } 2/3 \text{ bentang tengah}$$

Kontrol Inersia penampang terhadap lendutan

Radius modulus atau angka ekuivalen

$$n = \frac{E_s}{E_c} = \frac{200000}{21019.039} = 9.51518288$$

$$\text{Luas } 3 \Phi D 13 \quad A_s = 398.196869 \text{ mm}^2$$

$$\text{Luas } 2 \Phi 8 \quad A_s' = 100.530965 \text{ mm}^2$$

$$b = 150 \text{ mm}$$

$$d = 150 \text{ mm}$$

$$d' = 32 \text{ mm}$$

$$M_a = 6237706.699 \text{ Nmm}$$

Momen Inersia Penampang

$$\begin{aligned} I_g &= 1/12 * b * h^3 \\ &= 0.08333333 * 150 * 8000000 \\ &= 100000000 \text{ mm}^4 \end{aligned}$$

Letak sumbu netral untuk penampang retak (x)

$$\frac{b * x^2}{2} + (n-1) * A_s * (x - d') - n * A_s * (d - x) = 0$$

$$\frac{150 * x^2}{2} + (9.51518288 - 1) * 100.530965 * (x - 32) - 9.5152 * 398.196869 * (150 - x) = 0$$

$$398.196869 * (150 - x) = 0$$

$$\frac{150 * x}{2} + (19.0303658 - 1) * 100.530965 * (x - 32) = 9.5152 * 398.196869 * (150 - x)$$

$$9.5152 * 398.196869 * (150 - x)$$

$$75 x^2 + 1812.61007 x - 58003.5222 = 568337.405 - 3788.91603 x$$

$$75 x^2 - 74.687 x = 8351.21236$$

$$x + 37.344 = \sqrt{8351.21236 + (37.3435073)^2}$$

$$x + 37.344 = 98.7205647$$

$$x = 61.3770574 \text{ mm}$$

Momen inersia penampang retak:

$$I_{cr} = (1/3 * b * x^3) + ((n-1) * A_s' * (x - d')^2) + (n * A_s * (d - x)^2)$$

$$1/3 * b * y^3 = 0.33333333 * 150 * 231216.163 = 11560808.13$$

$$(n-1) * A_s' * (x - d')^2 = 8.5152 * 100.530965 * 863.0115 = 738771.978$$

$$n * A_s * (d - x)^2 = 9.51518288 * 398.196869 * 7854.02596 = 29758244.86$$

$$I_{cr} = 11560808.13 + 738771.978 + 29758244.86$$

$$I_{cr} = 42057824.97 \text{ mm}^4$$

Modulus keruntuhan lentur beton:

$$f_r = 0.7 * \sqrt{f_c} = 0.70 * 4.5 = 3.13$$

$$M_{cr} = \frac{f_r * I_g}{y_{beton}} \text{ dimana } f_r = 0.70 \sqrt{f_c}$$

$$M_{cr} = \frac{3.1305 * 42057825}{61.37705738} = 2145130.83 \text{ Nmm}$$

$$I_e = (M_{cr}/M_a)^3 * I_g + 1 - (M_{cr}/M_a)^3 * I_{cr}$$

$$(M_{cr}/M_a)^3 * I_g = 0.04067115 * 100000000 = 4067115.46$$

$$1 - (M_{cr}/M_a)^3 * I_{cr} = 1 - 0.04067115 * 42057825 = 40347284.7$$

$$I_e = 44414400.13 \text{ mm}^4$$

Kontrol Inersia Penampang terhadap retak :

$$I_{cr} = 42057824.97 < I_e = 44414400.129 < I_g = 100000000 \text{ mm}^4 \text{OK !!!}$$

Perhitungan Retak awal

Radius modulus atau angka ekuivalen

$$n = \frac{E_s}{E_c} = \frac{200000}{21019.039} = 9.51518288$$

$$\text{Luas } 3 \text{ } \phi D \text{ } 13 \text{ } A_s = 398.196869 \text{ mm}^2$$

$$\text{Luas } 2 \text{ } \phi \text{ } 6 \text{ } A_s' = 56.5486678 \text{ mm}^2$$

$$b = 150 \text{ mm}$$

$$h = 200 \text{ mm}$$

$$d = 150 \text{ mm}$$

$$d' = 40 \text{ mm}$$

$$f_c = 20 \text{ Mpa}$$

$$M_a = 6237706.699 \text{ Nmm}$$

Momen Inersia Penampang

$$\begin{aligned} I_g &= \frac{1}{12} * b * h^3 \\ &= 0.08333333 * 150 * 8000000 \\ &= 100000000 \text{ mm}^4 \end{aligned}$$

$$\begin{aligned} y_{\text{dasar}} &= \frac{1}{2} h \\ &= 100 \text{ mm} \end{aligned}$$

Modulus keruntuhan lentur beton:

$$f_r = 0.7 * \sqrt{f_c} = 0.70 * 4.5 = 3.13$$

$$M_{cr} = \frac{f_r * I_g}{y_{\text{beton}}} \quad \text{dimana } f_r = 0.70 * \sqrt{f_c}$$

$$\begin{aligned} M_{cr} &= \frac{3.1305 * 100000000}{100} \\ &= 3130495.17 \text{ Nmm} \\ &= 3.13049517 \text{ kNm} \end{aligned}$$

$$M_u = 0.35 P + 0.81$$

$$P_{cr} = \frac{3.13049517 - 0.81}{0.35} = 6.6299862 \text{ kN}$$

$$\begin{aligned} \phi_{\text{crack}} &= \frac{f_r * y_{\text{dasar}}}{I_g} \\ &= \frac{3.13 * 100}{100000000} = 3E-06 \text{ rad/mm} \end{aligned}$$

Letak sumbu netral untuk penampang retak (x)

$$\frac{b * x^2}{2} + (n-1) * A_s * (x-d') - n * A_s * (d-x) = 0$$

$$\frac{150 * x^2}{2} + (9.51518288 - 1) * 56.5486678 * (x - 40) - 9.5152 * 398.196869 * (150 - x) = 0$$

$$75 x^2 + 1019.59316 x - 40783.7265 = 568337.405 - 3788.91603 x$$

$$\frac{150 * x}{2} + (19.0303658 - 1) * 56.5486678 * (x - 40) = 9.5152 * 398.196869 * (150 - x)$$

$$75 x^2 + 1019.59316 x - 40783.7265 = 568337.405 - 3788.91603 x$$

$$75 x^2 - 64.113 x = 8121.61508$$

KURVATURE

$$f_r = 4.90 \text{ Mpa (Hasil Pengujian)}$$

$$M_{cr} = \frac{4.90 * 100000000}{100}$$

$$= 4900000 \text{ Nmm}$$

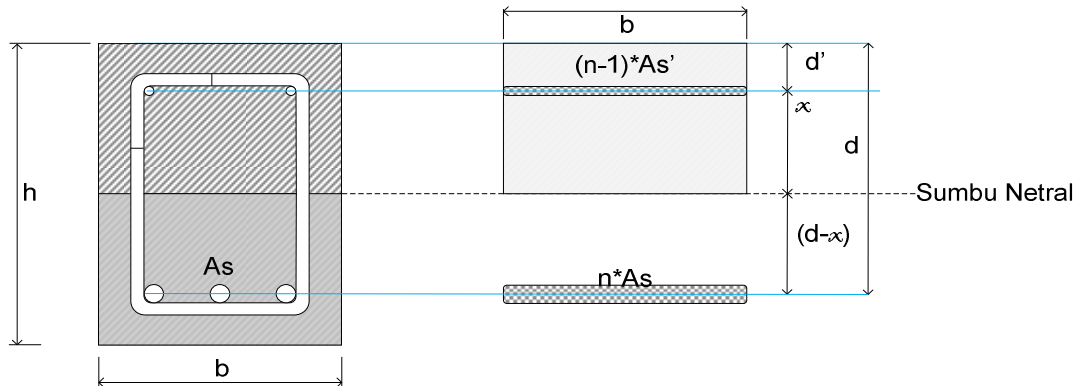
$$= 4.9 \text{ kNm}$$

$$P_{cr} = 11.6857143 \text{ kN}$$

$$\phi_{\text{crack}} = 0.0000049 \text{ rad/mm}$$

$$\begin{aligned}
 x + 32.057 &= \sqrt{8121.61508 + [32.056728]^2} \\
 x + 32.057 &= 95.6517061 \\
 x &= 63.5949782 \text{ mm}
 \end{aligned}$$

Momen inersia penampang retak:



$$\begin{aligned}
 I_{cr} &= (1/3 * b * x^3) + ((n-1) * A_s' * (x-d')^2) + (n * A_s * (d-x)^2) \\
 1/3 * b * y^3 &= 0.33333333 * 150 * 257198.522 = 12859926.09 \\
 (n-1) * A_s' * (x-d')^2 &= 8.5152 * 56.5486678 * 556.722996 = 268074.508 \\
 n * A_s * (d-x)^2 &= 9.51518288 * 398.196869 * 7465.82779 = 28287394.61 \\
 I_{cr} &= 12859926.09 + 268074.508 + 28287394.61 \\
 I_{cr} &= 41415395.21 \text{ mm}^4
 \end{aligned}$$

Modulus keruntuhan lentur beton:

$$\begin{aligned}
 f_r &= 0.7 * \sqrt{f_c} = 0.70 * 4.5 = 3.13 \\
 M_{cr} &= \frac{f_r * I_g}{y_{beton}} \quad \text{dimana } f_r = 0.70 \sqrt{f_c} \\
 M_{cr} &= \frac{3.1305 * 41415395.2}{63.59497819} \\
 &= 2038693.91 \text{ Nmm} \\
 &= \boxed{2.03869391} \text{ kNm} \\
 M_u &= 0.35 P + 0.81 \\
 P_{cr} &= \frac{2.03869391 - 0.81}{0.35} = \boxed{3.51055402} \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 I_e &= (M_{cr}/M_a)^3 * I_g + 1 - (M_{cr}/M_a)^3 * I_{cr} \\
 (M_{cr}/M_a)^3 * I_g &= 0.03491252 * 100000000 = 3491252.22 \\
 1 - (M_{cr}/M_a)^3 * I_{cr} &= 1 - 0.03491252 * 41415395.2 = 39969479.3 \\
 I_e &= 43460731.52 \text{ mm}^4
 \end{aligned}$$

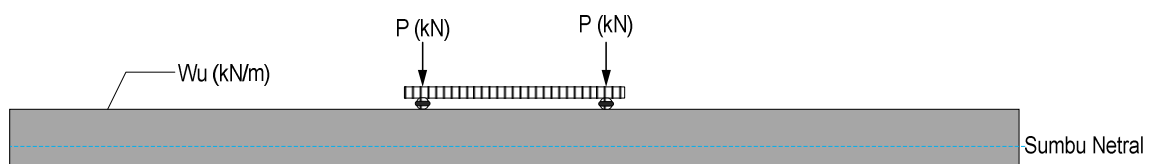
Kontrol Inersia Penampang terhadap retak :

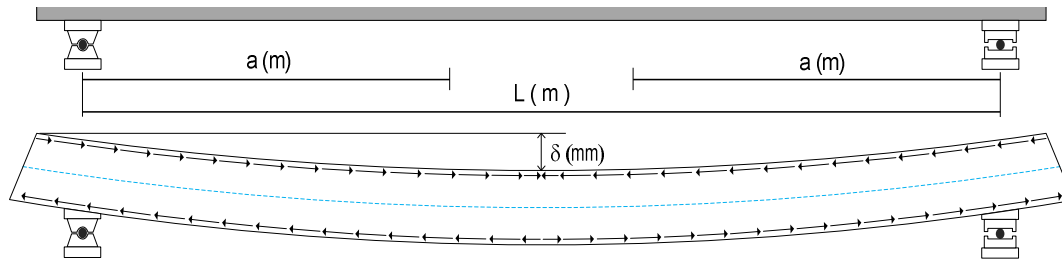
$$I_{cr} = 41415395.21 < I_e = 43460731.52 < I_g = 100000000 \text{ mm}^4 \text{OK !!!}$$

Untuk Perhitungan lendutan secara teoritis dilakukan yaitu :

dimana :

$$\begin{aligned}
 E_c &= 21019.039 \text{ Mpa} = 21.019 \text{ kN/mm}^2 \\
 a &= 1200 \text{ mm} \\
 L &= 3000 \text{ mm} \\
 q &= 0.72 \text{ kN/m} = 0.00072 \text{ kN/mm}
 \end{aligned}$$





Lendutan Kondisi sebelum retak

$$P_{cr} = \boxed{6.6299862} \text{ kN}$$

$$\delta = \frac{1}{24} * \frac{P * a}{E_c * I_g} * (3 * L^2 - 4a^2) + \frac{5}{384} * \frac{q * L^4}{E_c * I_g}$$

$$\frac{1}{24} * \frac{P * a}{E_c * I_{cr}} = 0.04166667 * \frac{7955.983435}{21.019 * 100000000} = 1.5771E-07$$

$$(3 * L^2 - 4a^2) = 3 * 9000000 - 4 * 1440000 = 21240000$$

$$\frac{5}{384} = \frac{q * L^4}{E_c * I_g} = 0.013 * \frac{0.00072 * 8.1E+13}{21.019039 * 100000000} = 0.3612796$$

$$\delta = 1.5771E-07 * 21240000 + 0.3612796$$

$$= \boxed{3.7111213} \text{ mm}$$

Lendutan Kondisi setelah retak awal leleh

$$P_y = \boxed{46.6407883} \text{ kN}$$

$$\delta = \frac{1}{24} * \frac{P * a}{E_c * I_e} * (3 * L^2 - 4a^2) + \frac{5}{384} * \frac{q * L^4}{E_c * I_e}$$

$$\frac{1}{24} * \frac{P * a}{E_c * I_e} = 0.04166667 * \frac{55968.94601}{21.019 * 41415395.2} = 2.6789E-06$$

$$(3 * L^2 - 4a^2) = 3 * 9000000 - 4 * 1440000 = 21240000$$

$$\frac{5}{384} = \frac{q * L^4}{E_c * I_e} = 0.013 * \frac{0.00072 * 8.1E+13}{21.019039 * 41415395.2} = 0.87233165$$

$$\delta = 2.6789E-06 * 21240000 + 0.87233165$$

$$= \boxed{57.7727859} \text{ mm}$$

Lendutan Kondisi setelah retak pada beban ultimit

$$P_u = \boxed{45.3889266} \text{ kN}$$

$$\delta = \frac{1}{24} * \frac{P * a}{E_c * I_e} * (3 * L^2 - 4a^2) + \frac{5}{384} * \frac{q * L^4}{E_c * I_e}$$

$$\frac{1}{24} * \frac{P * a}{E_c * I_{cr}} = 0.04166667 * \frac{54466.71192}{21.019 * 41415395.2} = 2.607E-06$$

$$(3 * L^2 - 4a^2) = 3 * 9000000 - 4 * 1440000 = 21240000$$

$$\frac{5}{384} = \frac{q * L^4}{E_c * I_{cr}} = 0.013 * \frac{0.00072 * 8.1E+13}{21.019039 * 41415395.2} = 0.87233165$$

$$\delta = 2.607E-06 * 21240000 + 0.87233165$$

$$= \boxed{56.2455497} \text{ mm}$$

Hitung lebar retak yang terjadi :

$$\beta = 1.2 \text{ untuk balok umumnya}$$

$$f_y = 336.75 \text{ Mpa}$$

$$f_s = 0.6 f_y = 202.05 \text{ Mpa}$$

$$d' = 25 \text{ mm}$$

$$A_t = 398.196869 \text{ mm}^2$$

$$\begin{aligned}
 w &= 11 \cdot \beta \cdot f_s \cdot \sqrt[3]{A_t \cdot d' \cdot 10^{-6}} \\
 11 \cdot \beta \cdot f_s &= 11 \cdot 1.2 \cdot 202.05 = 2667.1 \\
 \sqrt[3]{A_t \cdot d' \cdot 10^{-6}} &= 398.196869 \cdot 25 = \sqrt[3]{9954.92172 \cdot 10^{-6}} \\
 &= 2.1512 \text{E-}05 \\
 w &= 2667.1 \cdot 2.1512 \text{E-}05 = \boxed{0.0573736} \text{ mm}
 \end{aligned}$$