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LAMPIRAN

Perhitungan Kapasitas Momen - Balok Normal (NB)

1 . Data Perencanaan

Kuat tekan beton	$f_c = 30.02$	Mpa
Lebar Penampang	$b = 150$	mm
Tinggi Penampang	$h = 250$	mm
Tinggi Efektif	$d = 210.5$	mm
Tegangan Leleh Baja	$F_y = 406.86$	Mpa
Modulus Elastisitas Baja	$E_s = 200000$	Mpa
Jarak tulangan tekan serat luar	$d' = 39.5$	mm
Modulus Elastisitas Beton	$E_c = 25752$	Mpa

2 . Momen Retak Pertama (M_{cr})

Pada kondisi retak pertama, momen retak (M_{crack}) terjadi pada saat serat tarik penampang balok mencapai modulus keruntuhan (f_r). Oleh SNI 2847.2013 pasal 9.5.2.3 diberikan persamaan sebagai berikut

$$M_{cr} = \frac{f_r \cdot I_g}{y_t}$$

Diketahui :

$$\text{Hasil uji modulus pecah } f_r \quad 0.7 \times F_c^{0.5} = 3.86 \text{ Mpa}$$

Momen inersia (I_b) penampang bruto :

$$I_g = \frac{bh^3}{12} = 195312500 \text{ mm}^4$$

$$y = \frac{1}{2} h = 125 \text{ mm}$$

$$M_{cr} = \frac{4 \times 2E+08}{125} = 6031250 \text{ Nmm} = \mathbf{6.03 \text{ kNm}}$$

Nilai P_{crack} diperoleh dengan cara substitusi M_{crack} ke persamaan :

$$M = 1 + 0.6 P$$

$$6 = 1 + 0.6 P$$

diperoleh

$$P_{cr} = \frac{5}{1} = 8.7 \text{ kN} = \mathbf{8702.1 \text{ N}}$$

3 . Momen Leleh (M_{yield})

Direncanakan menggunakan tulangan :

$$\text{Luas } 3 \text{ } \Phi \text{D } 13 \text{ As} = 398.20 \text{ mm}^2$$

$$\text{Luas } 2 \text{ } \Phi \text{ } 8 \text{ As}' = 100.53 \text{ mm}^2$$

Awal tulangan leleh

$$n = \frac{E_s}{E_c} = \frac{200000}{25751.5398} = 7.766526$$

$$r = \frac{\left(\frac{As}{b \cdot d} \right)}{\frac{398.197}{150 \cdot 210.5}} = 0.01261 \qquad r' = \frac{\left(\frac{As'}{b \cdot d} \right)}{\frac{100.531}{150 \cdot 210.5}} = 0.00318$$

$$\begin{aligned} (r+r')^2 \cdot n^2 &= 0.00025 \cdot 60.31892 = 0.01505 \\ 2(r+r') \cdot d'/d \cdot n &= 2.0 \cdot 0.00066 \cdot 7.76653 = 0.01021 \\ (r+r') \cdot n &= 0.01580 \cdot 7.76653 = 0.12267 \end{aligned}$$

$$\begin{aligned} k &= \left[(r+r')^2 \cdot n^2 + 2(r+r') \cdot d'/d \cdot n \right]^{0.5} - (r+r') \cdot n \\ &= \left[0.02526 \right]^{0.5} - 0.12267 = 0.03626 \\ kd &= 0.03626 \cdot 210.5 \\ &= 7.63261 \text{ mm} \end{aligned}$$

Regangan tulangan tarik dari ujung atas balok

$$\epsilon_y = \frac{F_y}{E_s} = \frac{406.86}{200000} = 0.002$$

Regangan beton bagian atas

$$\begin{aligned} \epsilon_c &= \epsilon_s \cdot \left(\frac{kd}{d - kd} \right) \\ &= 0.002 \cdot \frac{7.63261}{210.5 - 7.63261} = 7.65E-05 \end{aligned}$$

$$f'_c = E_c \cdot \epsilon_c = 25752 \cdot 7.65E-05 = 1.97097 \text{ Mpa}$$

Regangan tulangan tekan

$$\begin{aligned} \epsilon_{s'} &= \epsilon_c \left(\frac{kd - d'}{kd} \right) \\ &= 7.65E-05 \left(\frac{7.63261 - 40}{7.63261} \right) = 0.00032 \end{aligned}$$

$$\begin{aligned} f'_s &= \epsilon_{s'} \cdot E_y = 0.00032 \cdot 200000 \\ &= 63.9115 \text{ Mpa} \end{aligned}$$

Gaya tekan beton

$$\begin{aligned} C_c &= 0.5 \cdot f'_c \cdot b \cdot kd \\ &= 0.5 \cdot 1.97097 \cdot 150 \cdot 7.63261 \\ &= 1128.2707 \text{ N} \end{aligned}$$

Gaya tekan baja

$$\begin{aligned} C_s &= A_s' \cdot f'_s = 100.5310 \cdot 63.9115 \\ &= 6425.08836 \text{ N} \\ T &= C_c + C_s = 1128.2707 + 6425.0884 \\ &= 7553.3591 \text{ N} \\ T &= A_s \cdot f_y \\ &= 162010.378 \text{ N} \end{aligned}$$

$$\begin{aligned} C_c + C_s - A_s \cdot f_y &= 0 \\ 7553.359 - 162010.378 &= -154457.019 \end{aligned}$$

Jarak gaya (c) dari ujung atas (y)

$$\begin{aligned} y &= \left(\frac{(C_s \cdot d') + (C_c \cdot 1/3 Kd)}{T} \right) = \frac{253790.99 + 2870.550}{7553.359} \\ &= 33.9797881 \text{ mm} \end{aligned}$$

Jarak pusat total gaya tekan ke pusat tulangan tarik

$$\begin{aligned} jd &= d - y = 210.5 - 33.9798 \\ &= 176.520 \text{ mm} \end{aligned}$$

Persamaan momen dan kurvatur

$$\begin{aligned} M_y &= A_s \cdot f_y \cdot jd \\ &= 398.197 \cdot 406.86 \cdot 176.520 \\ &= 28598106.3 \text{ Nmm} \\ &= \boxed{28.598 \text{ KN.m}} \end{aligned}$$

$$M_y = 1 \cdot P_y + 1$$

$$P_y = \boxed{46.31 \text{ KN}}$$

4 . Momen Ultimit (Mu)

$$Mu = \Phi Mn$$

$$Mu = \Phi * As * fy * \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur } \Phi = 0.9$$

dimana :

$$\rho_{\max} = 0.75 \rho_b$$

$$\rho_b = \beta_1 * \frac{0.85 f_c}{f_y} * \frac{600}{600 + f_y} \quad \text{untuk } \beta_1 = 0.85 \quad \text{dimana } f_c \text{ kecil atau sama dengan } 30 \text{ Mpa}$$

$$= 0.85 * \frac{0.85 * 30}{406.86} * \frac{600}{600 + 406.9}$$

$$= 0.0533 * 0.5959 = 0.0318$$

$$\rho_{\max} = 0.75 * 0.03177 = 0.02383$$

$$As = \rho_b * b * d$$

$$= 0.02383 * 150 * 210.5$$

$$= 752.2987 \text{ mm}^2$$

$$a = \frac{As * f_y}{0.85 * f_c * b}$$

$$= \frac{752.2987 * 406.86}{0.85 * 4503} = 79.9677 \text{ mm}$$

$$Mu = 0.90 * 752.299 * 406.86 * \left(210.5 - \frac{79.9677}{2} \right)$$

$$= 275472.236 * 170.5162$$

$$= 46972468.98 \text{ Nmm}$$

$$= \boxed{46.972 \text{ kNm}}$$

$$Mu = 0.6Pu + 1$$

$$Pu = \frac{46.16}{0.6}$$

$$\boxed{Pu = 76.94 \text{ KN}}$$

Perhitungan Kapasitas Momen - Balok PET (PB)

1 . Data Perencanaan

Kuat tekan beton	$f'_c = 18.38$ Mpa
Lebar Penampang	$b = 150$ mm
Tinggi Penampang	$h = 250$ mm
Tinggi Efektif	$d = 210.5$ mm
Tegangan Leleh Baja	$F_y = 406.86$ Mpa
Modulus Elastisitas Baja	$E_s = 200000$ Mpa
Jarak tulangan tekan serat luar	$d' = 39.5$ mm
Modulus Elastisitas Beton	$E_c = 20150$ Mpa

2 . Momen Retak Pertama (M_{cr})

Pada kondisi retak pertama, momen retak (M_{crack}) terjadi pada saat serat tarik penampang balok mencapai modulus keruntuhan (f_r). Oleh SNI 2847.2013 pasal 9.5.2.3 diberikan persamaan sebagai berikut

$$M_{cr} = \frac{f_r \cdot I_g}{y_t}$$

Diketahui :

$$\text{Hasil uji modulus pecah } f_r \quad 0.7 \times F_c^{0.5} = 3.001 \text{ Mpa}$$

Momen inersia (I_g) penampang bruto :

$$I_g = \frac{bh^3}{12} = 195312500 \text{ mm}^4$$

$$y = \frac{1}{2} h = 125 \text{ mm}$$

$$M_{cr} = \frac{3 \times 2E+08}{125} = 4689114 \text{ Nmm} = \mathbf{4.69 \text{ kNm}}$$

Nilai P_{crack} diperoleh dengan cara substitusi M_{crack} ke persamaan :

$$M = 1 + 0.6 P$$

$$5 = 1 + 0.6 P$$

diperoleh

$$P_{cr} = \frac{4}{1} = 6.47 \text{ kN} = \mathbf{6465.2 \text{ N}}$$

3 . Momen Leleh (M_{yield})

Direncanakan menggunakan tulangan :

$$\text{Luas } 3 \text{ } \Phi \text{D } 13 \quad A_s = 398.20 \text{ mm}^2$$

$$\text{Luas } 2 \text{ } \Phi \quad 8 \quad A_s' = 100.53 \text{ mm}^2$$

Awal tulangan leleh

$$n = \frac{E_s}{E_c} = \frac{200000}{20149.794} = 9.92566$$

$$r = \frac{\left(\frac{As}{b \cdot d} \right)}{150 \cdot 210.5} = \frac{398.197}{150 \cdot 210.5} = 0.01261 \quad r' = \frac{\left(\frac{As'}{b \cdot d} \right)}{150 \cdot 210.5} = \frac{100.531}{150 \cdot 210.5} = 0.00318$$

$$(r+r')^2 \cdot n^2 = 0.00025 \cdot 98.51872 = 0.02458$$

$$2(r+r' \cdot d/d) \cdot n = 2.0 \cdot 0.00066 \cdot 9.92566 = 0.01305$$

$$(r+r') \cdot n = 0.01580 \cdot 9.92566 = 0.15678$$

$$k = \left[\left((r+r')^2 \cdot n^2 + 2(r+r' \cdot d/d) \cdot n \right)^{0.5} - (r+r') \cdot n \right] = \left[0.03763 \right]^{0.5} - 0.15678 = 0.03720$$

$$kd = 0.03720 \cdot 210.5$$

$$= 7.83141 \text{ mm}$$

Regangan tulangan tarik dari ujung atas balok

$$\epsilon_y = \frac{F_y}{E_s} = \frac{406.86}{200000} = 0.002$$

Regangan beton bagian atas

$$\epsilon_c = \epsilon_s \cdot \left(\frac{kd}{d - kd} \right) = 0.002 \cdot \frac{7.83141}{210.5 - 7.83141} = 7.86E-05$$

$$f_c = E_c \cdot \epsilon_c = 20150 \cdot 7.86E-05 = 1.58394 \text{ Mpa}$$

Regangan tulangan tekan

$$\epsilon_{s'} = \epsilon_c \left(\frac{kd - d'}{kd} \right) = 7.86E-05 \left(\frac{7.83141 - 40}{7.83141} \right) = 0.00032$$

$$f_s = \epsilon_{s'} \cdot E_y = 0.00032 \cdot 200000 = 63.5751 \text{ Mpa}$$

Gaya tekan beton

$$C_c = 0.5 \cdot f_c \cdot b \cdot kd = 0.5 \cdot 1.58394 \cdot 150 \cdot 7.83141 = 930.337255 \text{ N}$$

Gaya tekan baja

$$C_s = A_s' \cdot f_s = 100.5310 \cdot 63.5751 = 6391.26935 \text{ N}$$

$$T = C_c + C_s = 930.3373 + 6391.2694 = 7321.6066 \text{ N}$$

$$T = A_s \cdot f_y = 162010.378 \text{ N}$$

$$C_c + C_s - A_s \cdot f_y = 0 \\ 7321.607 - 162010.378 = -154688.771$$

Jarak gaya (c) dari ujung atas (y)

$$y = \left(\frac{(C_s \cdot d') + (C_c \cdot 1/3 Kd)}{T} \right) = \frac{252455.14 + 2428.618}{7321.607} = 34.8125447 \text{ mm}$$

Jarak pusat total gaya tekan ke pusat tulangan tarik

$$jd = d - y = 210.5 - 34.8125 = 175.687 \text{ mm}$$

Persamaan momen dan kurvatur

$$\begin{aligned}
 M_y &= A_s \cdot f_y \cdot j d \\
 &= 398.197 \cdot 406.86 \cdot 175.687 \\
 &= 28463191.1 \text{ Nmm} \\
 &= \boxed{28.463 \text{ KN.m}}
 \end{aligned}$$

$$\begin{aligned}
 M_y &= 1 P_y + 1 \\
 P_y &= \boxed{46.09 \text{ KN}}
 \end{aligned}$$

4 . Momen Ultimit (Mu)

$$M_u = \Phi M_n$$

$$M_u = \Phi \cdot A_s \cdot f_y \cdot \left(d - \frac{a}{2} \right) \quad \text{faktor reduksi untuk lentur } \Phi = 0.9$$

dimana :

$$\rho_{\max} = 0.75 \rho_b$$

$$\rho_b = \beta_1 \cdot \frac{0.85 f_c}{f_y} \cdot \frac{600}{600 + f_y} \quad \text{untuk } \beta_1 = 0.85 \quad \text{dimana } f_c \text{ kecil atau sama dengan } 30 \text{ Mpa}$$

$$\begin{aligned}
 &= 0.85 \cdot \frac{0.85 \cdot 18}{406.86} \cdot \frac{600}{600 + 406.9} \\
 &= 0.0326 \cdot 0.5959 = 0.0195
 \end{aligned}$$

$$\rho_{\max} = 0.75 \cdot 0.0195 = 0.01459$$

$$A_s = \rho_b \cdot b \cdot d$$

$$= 0.01459 \cdot 150 \cdot 210.5$$

$$= 460.6013 \text{ mm}^2$$

$$a = \frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot b}$$

$$= \frac{460.6013 \cdot 406.86}{0.85 \cdot 2757} = 79.9677 \text{ mm}$$

$$\begin{aligned}
 M_u &= 0.90 \cdot 460.601 \cdot 406.86 \cdot \left(210.5 - \frac{79.9677}{2} \right) \\
 &= 168660.216 \cdot 170.5162 \\
 &= 28759293.13 \text{ Nmm} \\
 &= \boxed{28.759 \text{ kNm}}
 \end{aligned}$$

$$M_u = 0.6 P_u + 1$$

$$P_u = \frac{27.95}{0.6}$$

$$P_u = \boxed{46.58 \text{ KN}}$$

Kontrol Inersia penampang terhadap lendutan benda uji Beton Normal (NB)

Radius modulus atau angka ekuivalen

$$n = \frac{E_s}{E_c} = \frac{200000}{25752} = 7.7665$$

$$\text{Luas } 3 \text{ } \Phi \text{ } 13 \quad \text{As} = 398.20 \text{ mm}^2$$

$$\text{Luas } 2 \text{ } \Phi \text{ } 8 \quad \text{As}' = 100.53 \text{ mm}^2$$

$$b = 150 \text{ mm}$$

$$d = 210.5 \text{ mm}$$

$$d' = 39.5 \text{ mm}$$

$$M_a = 46972468.98 \text{ Nmm}$$

Momen Inersia Penampang

$$\begin{aligned} I_g &= \frac{1}{12} * b * h^3 \\ &= 0.083333 * 150 * 15625000 \\ &= 195312500 \text{ mm}^4 \end{aligned}$$

Letak sumbu netral untuk penampang retak (x)

$$\frac{b * x^2}{2} + (n-1) * A_s' * (x-d') - n * A_s * (d-x) = 0$$

$$\frac{150 * x^2}{2} + (7.76652588 - 1) * 100.53 * (x - 39.5) - 7.767 * 398.20 * (210.5 - x) = 0$$

$$\frac{150 * x^2}{2} + (7.76652588 - 1) * 100.53 * (x - 39.5) - 7.767 * 398.20 * (210.5 - x) = 0$$

$$\frac{150 * x^2}{2} + (7.76652588 - 1) * 100.53 * (x - 39.5) - 7.767 * 398.20 * (210.5 - x) = 0$$

$$75 x^2 + 680.245376 x - 26869.69 = 650994 - 3092.61 x$$

$$x^2 + 50.3 x = 9038.1775$$

$$x + 25.1523444 = \sqrt{9038.2 + (25.15234)^2}$$

$$x + 25.1523444 = 98.340317$$

$$x = 73.187973 \text{ mm}$$

Momen inersia penampang retak:

$$I_{cr} = \left(\frac{1}{3} * b * x^3 \right) + \left((n-1) * A_s' * (x-d')^2 \right) + \left(n * A_s * (d-x)^2 \right)$$

$$\frac{1}{3} * b * x^3 = 0.33333333 * 150 * 392030 = 2E+07$$

$$(n-1) * A_s' * (x-d')^2 = 6.7665 * 100.53 * 1134.88 = 771997$$

$$n * A_s * (d-x)^2 = 7.76652588 * 398.20 * 18854.59 = 58309832.4$$

$$I_{cr} = 19601493.23 + 771996.54 + 58309832.35$$

$$I_{cr} = 78683322.11 \text{ mm}^4$$

Modulus keruntuhan lentur beton:

$$f_r = 0.7 * \sqrt{F} = 0.70 * 30.02 = 3.84$$

$$M_c = \frac{f_r * I_g}{y_{beton}}$$

$$M_c = \frac{3.84 * 195312500}{73.18797271} = 10235138 \text{ Nmm}$$

$$I_e = \frac{(M_{cr}/M_a)^3 * I_g + 1 - (M_{cr}/M_a)^3 * I_{cr}}{1 - (M_{cr}/M_a)^3}$$

$$\frac{(M_{cr}/M_a)^3 * I_g}{1 - (M_{cr}/M_a)^3} = \frac{0.0103455 * 195312500}{1 - 0.010345} = 2020602.99$$

$$\frac{1 - (M_{cr}/M_a)^3 * I_{cr}}{1 - (M_{cr}/M_a)^3} = \frac{1 - 0.010345 * 7.9E+07}{1 - 0.010345} = 77869304.8$$

$$I_e = 79889907.79 \text{ mm}^4$$

Kontrol Inersia Penampang terhadap retak :

$$I_{cr} = 78683322.11 < I_e = 79889907.792 < I_g = 195312500 \text{ mm}^4 \text{OK !!!}$$

Untuk Perhitungan lendutan secara teoritis dilakukan yaitu :

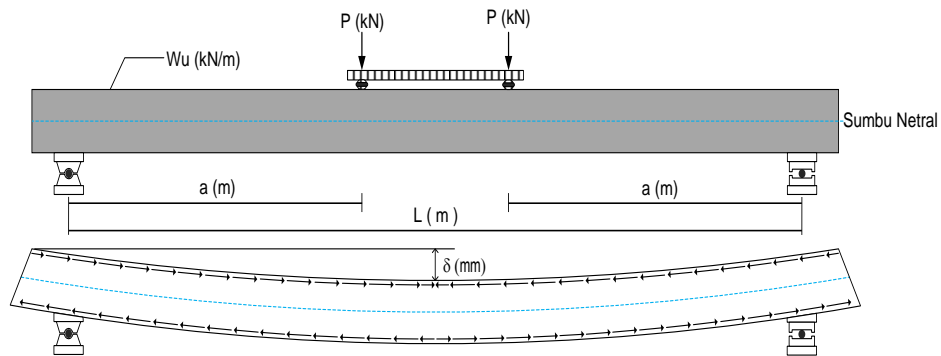
dimana :

$$E_c = 25751.5 \text{ Mpa} = 25.8 \text{ kN/mm}^2$$

$$a = 1200 \text{ mm}$$

$$L = 3000 \text{ mm}$$

$$q = 0.9 \text{ kN/m} = 0.0009 \text{ kN/mm}$$



Untuk I_{cr}

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_{cr}} \times (3L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_{cr}} \\ &= 0.042 \times \frac{1200P}{2E+09} \times 2.1E+07 + 0.013 \times \frac{72900000000}{2026216698} \\ &= 0.524129527 P + 0.46846853 \end{aligned}$$

Untuk I_g

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_g} \times (3L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_g} \\ &= 0.042 \times \frac{1200P}{5E+09} \times 2.1E+07 + 0.013 \times \frac{72900000000}{5029597609} \\ &= 0.211150092 P + 0.18872658 \end{aligned}$$

Kontrol Inersia penampang terhadap lendutan benda uji Beton PET (PB)

Radius modulus atau angka ekuivalen

$$n = \frac{E_s}{E_c} = \frac{200000}{20150} = 9.9257$$

$$\text{Luas } 3 \text{ } \Phi \text{D } 13 \quad A_s = 398.20 \text{ mm}^2$$

$$\text{Luas } 2 \text{ } \Phi \quad 8 \quad A_{s'} = 100.53 \text{ mm}^2$$

$$b = 150 \text{ mm}$$

$$d = 210.5 \text{ mm}$$

$$d' = 39.5 \text{ mm}$$

$$M_a = 28759293.13 \text{ Nmm}$$

Momen Inersia Penampang

$$\begin{aligned} I_g &= \frac{1}{12} * b * h^3 \\ &= 0.083333 * 150 * 15625000 \\ &= 195312500 \text{ mm}^4 \end{aligned}$$

Letak sumbu netral untuk penampang retak (x)

$$\frac{b * x^2}{2} + (n-1) * A_{s'} * (x-d') - n * A_s * (d-x) = 0$$

$$\frac{150 * x^2}{2} + (9.92565976 - 1) * 100.53 * (x - 39.5) - 9.926 * 398.20 * (210.5 - x) = 0$$

$$\frac{150 * x^2}{2} + (9.92565976 - 1) * 100.53 * (x - 39.5) - 9.926 * 398.20 * (210.5 - x) = 0$$

$$\frac{150 * x^2}{2} + (9.92565976 - 1) * 100.53 * (x - 39.5) - 9.926 * 398.20 * (210.5 - x) = 0$$

$$75 x^2 + 897.305189 x - 35443.55 = 831973 - 3952.37 x$$

$$x^2 + 64.66 x = \frac{11565.556}{75}$$

$$x + 32.3311455 = \sqrt{\frac{11566}{75} + (32.33115)^2}$$

$$x + 32.3311455 = 112.29808$$

$$x = 79.966937 \text{ mm}$$

Momen inersia penampang retak:

$$I_{cr} = \left(\frac{1}{3} * b * x^3 \right) + ((n-1) * A_{s'} * (x-d')^2) + (n * A_s * (d-x)^2)$$

$$\frac{1}{3} * b * x^3 = 0.33333333 * 150 * 511365 = 2.6E+07$$

$$(n-1) * A_{s'} * (x-d')^2 = 8.9257 * 100.53 * 1637.573 = 1469403$$

$$n * A_s * (d-x)^2 = 9.92565976 * 398.20 * 17038.88 = 67343902.7$$

$$I_{cr} = 25568272.92 + 1469402.8 + 67343902.7$$

$$I_{cr} = 94381578.38 \text{ mm}^4$$

Modulus keruntuhan lentur beton:

$$f_r = 0.7 * \sqrt{F} = 0.70 * 4.2872 = 3.00$$

$$M_c = \frac{f_r * I_g}{y_{beton}}$$

$$M_c = \frac{3.00 * 195312500}{79.9669373} = 7329770 \text{ Nmm}$$

$$I_e = (M_{cr}/M_a)^3 * I_g + 1 - (M_{cr}/M_a)^3 * I_{cr}$$

$$(M_{cr}/M_a)^3 * I_g = 0.0165553 * 195312500 = 3233452.8$$

$$1 - (M_{cr}/M_a)^3 * I_{cr} = 1 - 0.016555 * 9.4E+07 = 92819065.1$$

$$I_e = 96052517.88 \text{ mm}^4$$

Kontrol Inersia Penampang terhadap retak :

$$I_{cr} = 94381578.38 < I_e = 96052517.879 < I_g = 195312500 \text{ mm}^4 \text{OK !!!}$$

Untuk Perhitungan lendutan secara teoritis dilakukan yaitu :

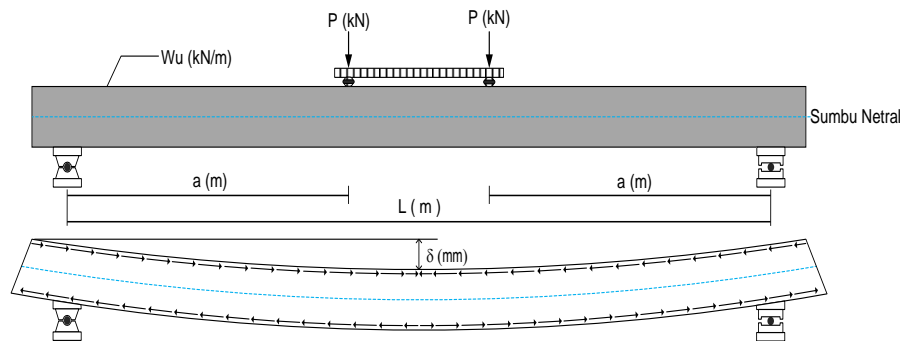
dimana :

$$E_c = 20149.8 \text{ Mpa} = 20.1 \text{ kN/mm}^2$$

$$a = 1200 \text{ mm}$$

$$L = 3000 \text{ mm}$$

$$q = 0.9 \text{ kN/m} = 0.0009 \text{ kN/mm}$$



Untuk I_{cr}

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_{cr}} \times (3L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_{cr}} \\ &= 0.042 \times \frac{1200P}{1.9E+09} \times 2.1E+07 + 0.013 \times \frac{72900000000}{1901769366} \\ &= 0.558427336 P + 0.49912401 \\ &\quad \quad \quad \mathbf{0.558427336} \end{aligned}$$

Untuk I_g

$$\begin{aligned} \delta &= \frac{1}{24} \times \frac{P \cdot a}{E_c \cdot I_g} \times (3L^2 - 4a^2) + \frac{5}{384} \times \frac{q \cdot L^4}{E_c \cdot I_g} \\ &= 0.042 \times \frac{1200P}{3.9E+09} \times 2.1E+07 + 0.013 \times \frac{72900000000}{3935506649} \\ &= 0.269850897 P + 0.24119353 \end{aligned}$$